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# PARAMETRIC FATIGUE ANALYSIS OF USAF FIGHTER AIRCRAFT

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AIR FORCE FLIGHT DYNAMICS LABORATORY
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WRIGHT-PATTERSON AIR FORCE BASE, OHIO 45433

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# FOREWORD

This report was prepared by the University of Dayton Research Institute, Dayton, Ohio, under Air Force Contract F 33(615)-68-C-1494. The project was initiated under Project 1467, "Structural Analysis Methods", Task 146704, "Structural Fatigue Analysis." The work was administered by the Air Force Flight Dynamics Laboratory, Air Force Systems Command, Wright-Patterson Air Force Base, Ohio. Mr. Howard A. Wood, (FDTR), was the Project Engineer.

The research effort was conducted from 13 May 1968 to 1 July 1969. The report was submitted by the authors in August 1969.

This program was conducted under the general direction of Mr. Dale H. Whitford, Supervisor of Aerospace Mechanics Research.

This technical report has been reviewed and is approved.

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Chief, Solid Mechanics Branch
Structures Division

## ABSTRACT

This report contains the results of a study of the significant parameters that contribute to the fatigue life of USAF fighter aircraft. The variability of the parameters from one aircraft to another was determined in an attempt to use a mean value or a most probable distribution of some parameters so that they could be eliminated from the log sheet or recorded data. The analysis suggests that there is such a wide variation in the load factors, Mach numbers, altitudes and configurations experienced by the F-105D and F-105F aircraft that an average damage model cannot be used to predict damage to individual aircraft. A peak strain cycle counting recorder is suggested as the most practical method of monitoring fatigue damage to individual fighter aircraft. Design concepts of a counting accelerometer and three types of peak strain counters are presented.

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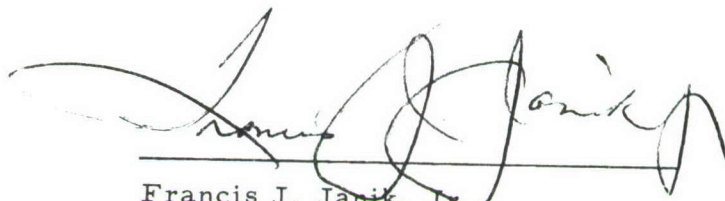
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# SECTION I

## INTRODUCTION

This report is written in support of the Air Force Fatigue Certification Program and the Aircraft Structural Integrity Program. The Fatigue Certification Program has these overall objectives: (a) to provide the Air Force with aircraft which have specified life capabilities; (b) to provide the Air Force with a rational means of scheduling aircraft for required structural modifications so that the required life can be achieved with minimum downtime and loss of combat capability; and (c) to provide the Air Force with a means to assess the life trade-off requirements for various mission mixes and subsequent long range planning for aircraft replacement. The objectives of the Structural Integrity Program are: (a) to establish, evaluate, and substantiate structural integrity of aircraft systems; (b) to continually evaluate the structural integrity program by utilizing inputs from operational usage; (c) to develop statistical techniques for the evaluation of operational usage and for logistic support (maintenance, inspection, suppliers); and (d) to develop and incorporate improved structural criteria and methods of design, evaluation, and substantiation of aircraft systems.

To achieve these objectives it is necessary to know the accumulated fatigue damage to each individual aircraft in the fleet. The Air Force document, ASD-TR-66-57, "Air Force Aircraft Structural Integrity Program Requirements", as revised in 1969, states in paragraph 2.5.2.1 that,

> "Individual aircraft or groups of aircraft can accumulate fatigue damage at widely varying rates depending on usage. These variations from the fleet average must be assessed to prevent catastrophic failures or unscheduled maintenance in the fleet."

For fighter aircraft the fatigue damage is a function of gross weight, Mach number, altitude, stores configuration, and load factor experienced. These parameters vary from flight to flight and also are dependent on the type of mission. Aircraft are currently programmed for modification on the basis of total flight hours, regardless of the utilization of the individual aircraft. This philosophy is based on the assumption that each aircraft will experience the same number of combinations of the above parameters during its life. Recorders are installed on a small percent of the fleet and from these recordings the average fatigue damage per hour is calculated. This average damage rate is then applied to each aircraft in the fleet.

In 1967, a study was conducted (Reference 1), wherein 120 flights were analyzed to determine if each aircraft was experiencing the same damage rate

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when the rate was normalized to different parameters. Since that time, data has become available on 3407 flights involving three different types of aircraft.

This report presents the analysis of these flights and defines the parameters necessary to monitor the damage on individual aircraft. Presentations are made of the expected accuracy of the fatigue damage to individual aircraft when one uses an average damage per hour, average damage per flight, average damage per weapon pass and a calculation based on the recorded load factor level with a distribution of Mach-altitude conditions. A design concept of a low cost recorder that could be installed in each aircraft is also presented.

SECTION II

ANALYSIS OF RECORDED DATA

Fatigue damage during flight of a fighter aircraft is a function of the aircraft's load factor, gross weight, stores configuration, Mach number, and altitude. This section presents an analysis of the effect of each of these parameters and an analysis of the consistency of the distribution of them from aircraft to aircraft. Each of the three aircraft, the F-5A, F-105D, and the F-105F will be analyzed and the results presented separately.

1.    F-5A AIRCRAFT

The F-5A aircraft parametric study was based on the analysis of data reported in References 2 and 3. The fatigue damage calculations were based on the loads and stresses presented in Reference 4. Reference 2, which is a VGH flight loads report, contains composited data from 1638 flights in the SEA war zone. Reference 3 contains the load factor data for the weapon passes of this same data.

The F-5A aircraft known as the "Freedom Fighter" is a light-weight single-seat fighter-bomber built by the Norair Division of the Northrop Corporation and was used in SEA as a close air support bomber. The analysis of the data by the Northrop Corporation as presented in Reference 4 was used whenever possible to perform the parametric study.

a.    Fatigue Damage Analysis

The ground rules for the fatigue analysis were the same as those used in Reference 4. As stated previously, fatigue damage is a function of the load factor, gross weight, stores configuration, Mach number, and altitude. For the F-5A aircraft the most critical location for determining the fatigue life is the wing root section at wing station 26.6. Reference 4 states that

> "...89.5 percent of the flight time occurred at altitudes below 15,000 feet and 89.3 percent of the flight time occurred in the equivalent airspeed range of 250 to 400 knots. These conditions result in a maximum Mach range from 0.4 to 0.76. Under these flight conditions the wing loads do not vary appreciably and, therefore, no attempt has been made to vary the loads to account for altitude and airspeed."

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Therefore, the fatigue damage has been reduced to a function of load factor, gross weight, and stores configuration. The data in Reference 2 that is most usable is presented in terms of percent design limit load factor (PDLLF), where

$$PDLLF = \frac{N_z W}{N_{zd} W_d} \times 100$$

where

$N_{zd}$ = design limit load factor for a configuration

$N_z$ = actual maneuver load factor

$W_d$ = design gross weight for a configuration

$W$ = actual aircraft gross weight at time of load factor experience

Therefore, to analyze the available data, damage is only a function of PDLLF and stores configuration. Figure 1 is a plot of damage per occurrence versus PDLLF for the configurations represented in the data sample. As can be observed from the figure, the amount of damage is a strong function of the stores configuration. Using the data from Figure 1 and the load experiences as reported in Reference 2, the damage by mission segment was calculated. Table I is a listing of these damages by mission segment. The data presented in Table I is the sum of all aircraft and indicates that 97.5 percent of the fatigue damage occurs during air to ground combat activities.

In order to calculate the damage on an aircraft tail number basis, we must look at the distribution of load factors and configurations by aircraft tail numbers. Table 11 of Reference 2 lists the PDLLF versus configurations for the total data sample and Table 13 lists the distribution of PDLLF by aircraft serial number. Assuming that each aircraft had the same distribution of PDLLF versus configuration as shown in Table 11 of Reference 2, the data in Table 13 of Reference 2 was used to calculate the damage by aircraft. The results of these calculations, shown in Table II of this report, were the best estimates of the damage to each individual aircraft that could be made with the data available. The listing in Table II shows that the average damage fraction was 0.000045553 per hour. Assuming that each aircraft accumulates damage at the same rate, a predicted damage for each aircraft is also presented in Table II and shows that the damage could be over- or under-predicted by 42% on two of the aircraft. The aircraft which was under-predicted by 42% had only 67 hours of recorded flight time. Two other aircraft which had 16.9 and 2.3 hours were also badly under-predicted. If one were to remove these three aircraft, i.e., numbers 3, 7, and 8, only aircraft number 1 would be poorly estimated.

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Since most of the damage is done during the weapon passes, a more reasonable method of monitoring the damage would be to determine the average damage per flight instead of per hour. Table III lists the percent of error of the predicted damage to actual damage.

Before presenting any more data, some comments are in order about the data sample that was used. The recorded data was collected in five phases. The first, third, and fifth were recorded at Bien Hoa airbase while the second and fourth were at DaNang. The aircraft were moved from one base to the other with the change in the recording phases. In analyzing the data on a per-hour or per-flight basis, it is important to know if all the aircraft were used in the same manner at each of the bases. Figure 7 of Reference 2 shows the percentage of flights within different flight length bands. This data is repeated here as Table IV and shows that the flights from Bien Hoa were generally of a shorter duration than those at DaNang. If some aircraft had a higher percentage of their flights at Bien Hoa, one would expect that the damage rate per hour would be higher for those aircraft. This is true because a great majority of the damage occurs during air-to-ground activities, which is not a function of the flight duration. The data available does not list the mission mix flown by each aircraft; therefore, no analysis was possible regarding the lengths of flights by aircraft serial number. However, since both Tables II and III show reasonably good predicted damages, it indicates that all the aircraft must have flown approximately the same mission mix. Another interesting fact about the data as pointed out in Reference 4 is that the ground gunnery passes during Phase I represented 80.9% of the maneuver load factors for all ground gunnery. These gunnery passes during Phase I, which was a 2-month period, were a result of an evaluation of the F-5/M-39 gun where approximately 50,000 rounds of ammunition were fired by each aircraft. "Thus, essentially every mission included firing all of the ammunition carried in the aircraft."[*] After the first data-collecting phase, the guns were used only as needed to fulfill the requirements of each mission. The total fatigue damage due to ground gunnery during Phase I was 0.0354, which was 50% of the total damage for the entire data sample. One can see from these figures that the evaluation of the gun greatly affects the damage rate of the data sample. This could explain why aircraft numbers 3, 7, and 8 received more damage than would be predicted by either the per-hour or per-flight average, since these three aircraft had a small number of recorded flights and most of these were probably during recording Phase I.

b. Discussion

The parametric fatigue analysis of the F-5A aircraft indicated that the great majority of the damage was due to air-to-ground activity. Therefore, an average damage rate based on a per-flight rather than a per-hour basis is a better predictor of damage, since the length of the flight has little to do with the activity in the target area. Also, since most of the damage was due to the

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[*] Reference 3

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pull-up after weapon release or due to ground gunnery, the majority of the load factors occurred when the aircraft was in a clean configuration. Gunfire passes are usually made after weapon passes. This fact reduces the importance of the earlier assumption that the distribution of configurations for each individual aircraft was the same as the distribution for the entire instrumented fleet.

It is the authors' opinion that for the data sample analyzed, the use of an average damage per flight is an adequate method for monitoring the fatigue damage on the F-5A aircraft. Some improvement in the calculation of the damage to individual aircraft could be realized by the use of a load factor recorder that segregated the occurrences into grouping by stores configuration. However, because of the large scatter factor associated with fatigue failures, even for constant amplitude cycling, an improvement on the ±30% error does not appear to be justified. This conclusion is based on the analysis of the recorded data for SEA operations. The success of the predictor based on the average damage per flight may be the result of a fortuitous combination of load factors, gross weight, and configurations. There is some reason to be suspicious of the success obtained by the average damage per flight predictor, since the cumulative frequency distribution of PDLLF, as presented in Figure 2, shows a large variation from one aircraft to another. A comparison of Figure 3, which is a cumulative frequency distribution of load factors, with Figure 2 shows the effect that weight and configuration mix has on the conversion of load factor distribution to PDLLF distributions.

From the analysis of the distribution of the damage to the individual aircraft, it appears that a substantial improvement in the confidence of the damage calculations would result from the use of some type of recorded data. The data could be in the form of load factor level as a function of (a) weight, (b) stores configuration, (c) altitude, and (d) airspeed. The use of a peak counting accelerometer that segregated the occurrences by these parameters would eliminate the costly data processing task of a time history recorder. However, the number of storage registers would be equal to the product of the number of bands of each of the parameters. For example, on the F-5A aircraft, 45 storage registers would be required if one used three weight bands, three configurations, and five load levels. These are the only important parameters for this aircraft. This number could be reduced with some sacrifice in accuracy and introduction of some conservatism. Using the F-5A as an example, one could base all of the calculations on the most damaging configuration, which happens to be Configuration 1 (see Figure 1). The data shows that 90% of the damage occurred during Configuration 1, 8.3% during Configuration 2, and 1.5% during Configuration 3. If Configuration 1 had been used for all of the damaging load cycles, then the sum of the estimated damage for all the aircraft would have been 155% of the actual damage. This is definitely conservative and less accurate than predictions based on either the per-hour or per-flight averages. However, this assumption would reduce the number of storage registers to 15, since the load factors would only be segregated by weight.

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Another approach would be to segregate the load factors by three configurations and assume a mean value for the weight which could be a function of the configuration. For the data sample analyzed it was found that the mean weight for Configuration 1 at the time of the peak load after weapon release or ground fire was 12, 979 lbs., with a standard deviation of 726 lbs. For configurations 2 and 3, the numbers were 14, 421 lbs. mean with 638 lbs. standard deviation, and 14, 667 lbs. mean with 797 lbs. standard deviation, respectively. The design gross weight for Configuration 1 was 11, 600 lbs. Therefore, an error of 726 lbs. would cause an error in the PDLL of 5. 2% at 5 g's.

$$PDLL = \frac{5(12, 979 + 726)}{7(11, 600)}$$

$$PDLL = 84.39$$

$$PDLL = \frac{5(12, 979)}{7(11, 600)}$$

$$PDLL = 79.92$$

$$Error = \frac{4.47}{84.39} = 5.2\%$$

This error of 5. 2% at the 84. 39% level for Configuration 1 would cause an underestimation of the damage per load cycle occurrence, see Figure 1, of (0. 0000190 - 0. 0000138) = 0. 0000052 which is 27. 4%. For those weights which are less than the mean by $1\sigma$, at the same load factor and configuration, the damage would be overestimated by 31. 1%. Now, if the actual weights are symmetrically distributed about the mean, over-and underestimates would be offsetting so that the cumulative damage over a long period of time would be very nearly correct. It therefore appears that the best type of load factor monitor for the F-5A would be one that segregated the load factor by three configurations and five load factor levels. This would then require 15 storage registers. The design of such a system is presented in Section IV.

Another recording system that would eliminate the problems associated with knowing the gross weight and/or configuration would be a strain amplitude cycle counter. This recorder would accumulate in storage registers the number of times that various strain amplitudes were equaled or exceeded. These strain cycle counts would then be plotted as the number of times that a given strain level was exceeded versus the strain level. From this plot a fatigue analysis could be performed with the very simple calculation of determining the life cycles at each stress level. The accuracy of this technique would depend on only two factors: (1) the ability of the analyst to determine a transfer factor from the gage location to the fatigue critical location, and (2) the effect of the variation in the 1-g trim stress. The complexity of the first factor depends on the aircraft structure, the location of the fatigue critical point, and the response of the aircraft to the various types of loads. Two approaches can be taken to the second factor. It can be assumed that the 1-g strain is a constant or that each aircraft

has the same probability of various 1-g trim stresses. The use of a constant 1-g trim stress should be adequate for most fighter aircraft since there is little variation in the trim stress for the weight range and configurations that exist at the time the damaging loads occur. For example, the fatigue analysis presented in Reference 4 for the F-5A had only a 1083 psi variation in the 1-g trim stress over the entire range of the nine configurations. Therefore, the use of a constant 1-g trim stress would mean that the assumed 1-g stress would have a deviation from an existing practice of only ±540 psi, which is well within the capability to calculate the stress from any set of parameters. The concept of an electro-mechanical-optical strain transducer which would accumulate these strain counts is presented in Section IV.

# TABLE I

## Distribution of Fatigue Damage at Wing Station 26.6
## for F5A SEA Data Sample

| Mission Segment | Wing Station 26.6 Damage | Percent Damage |
|---|---|---|
| Ascent | 0 | 0 |
| Descent | .0000625539 | .09 |
| Cruise Out | .0000219635 | .03 |
| Cruise Back | .0012011469 | 1.69 |
| Loiter | .0001375018 | .19 |
| Refuel | 0 | 0 |
| Low Angle Bomb | .0251612405 | 35.50 |
| Rocket Firing | .0011593153 | 1.63 |
| Ground Gunnery | .0427923695 | 60.38 |
| Photo | .0003380570 | .48 |
| Total | .0708741484 | 99.99 |

## Percent of Total Damage Due to Air-to-Ground Activities

| | |
|---|---|
| Low Angle Bombing | 35.50% |
| Rocket Firing | 1.63% |
| Ground Gunnery | 60.38% |
| | 97.51% |

## TABLE II

### Comparison of the Predicted Damage to Actual Damage
### from Average Damage Per Flight Hour

| A/C Number | Recorded Flight Time (hours) | Actual Damage (x 10³) Ⓑ | Predicted Damage (damage/hr x hrs) x 10³ Ⓐ | % Error |
|---|---|---|---|---|
| 1 | 184.53 | 5.89632 | 8.40594 | 42.60 |
| 2 | 153.28 | 7.11406 | 6.98240 | - 1.85 |
| 3 | 16.90 | 1.02444 | 0.76985 | -24.90 |
| 4 | 205.90 | 9.17693 | 9.37942 | 2.21 |
| 5 | 172.57 | 7.00650 | 7.86113 | 12.20 |
| 6 | 195.03 | 10.18678 | 8.88425 | -12.80 |
| 7 | 2.32 | 0.16262 | 0.10568 | -35.00 |
| 8 | 67.93 | 5.27875 | 3.09443 | -41.40 |
| 9 | 185.08 | 7.81347 | 8.43010 | 7.90 |
| 10 | 166.10 | 6.87209 | 7.56640 | 10.10 |
| 11 | 201.03 | 10.10611 | 9.15757 | - 9.40 |
| Total | 1550.67 | 70.63807 | | |

Average Damage Per Hour = .000045553

$$\% \text{ Error} = \frac{Ⓐ - Ⓑ}{Ⓑ} \times 100$$

## TABLE III

### Comparison of Predicted Damage to Actual Damage
### Based on Average Damage Per Flight

| A/C Number | Flights | Actual Damage (x $10^3$) | Predicted Damage (damage/flight x flights) $10^3$ | % Error |
|---|---|---|---|---|
| | | Ⓑ | Ⓐ | |
| 1 | 172 | 5.89632 | 7.41742 | +26 |
| 2 | 168 | 7.11406 | 7.24493 | + 1.8 |
| 3 | 23 | 1.02444 | .99186 | - 3.2 |
| 4 | 196 | 9.17693 | 8.45241 | - 7.9 |
| 5 | 187 | 7.00650 | 8.06429 | +15.1 |
| 6 | 217 | 10.18678 | 9.35803 | - 8.1 |
| 7 | 3 | 0.16262 | 0.12937 | -20.4 |
| 8 | 82 | 5.27875 | 3.53621 | -33.0 |
| 9 | 194 | 7.81347 | 8.36616 | + 7.1 |
| 10 | 183 | 6.87209 | 7.89179 | +14.8 |
| 11 | 213 | 10.10611 | 9.18553 | - 9.1 |
| Total | 1638 | 70.63807 | | |

$$\text{Average damage/flight} \quad \frac{70.63807 \times 10^{-3}}{1638} = .000043125$$

$$\% \text{ Error} = \frac{Ⓐ - Ⓑ}{Ⓑ} \times 100$$

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TABLE IV

Percentage of Combat Mission by Flight Length Duration
and by Recording Phase

| Recording Phase | Base | Duration of Flight Hours | | | | |
|---|---|---|---|---|---|---|
| | | 0-.5 | .5-1 | 1-1.5 | 1.5-2 | 2-6.5 |
| 1 | Bien Hoa | 0 | 78.4 | 21.5 | 0.1 | 0 |
| 2 | Da Nang | 0 | 12.2 | 60.5 | 26.2 | 1.1 |
| 3 | Bien Hoa | 1.6 | 84.1 | 15.3 | 0 | 0 |
| 4 | Da Nang | 0 | 6.4 | 39.1 | 30.9 | 23.6 |
| 5 | Bien Hoa | 0 | 86.2 | 13.8 | 0 | 0 |
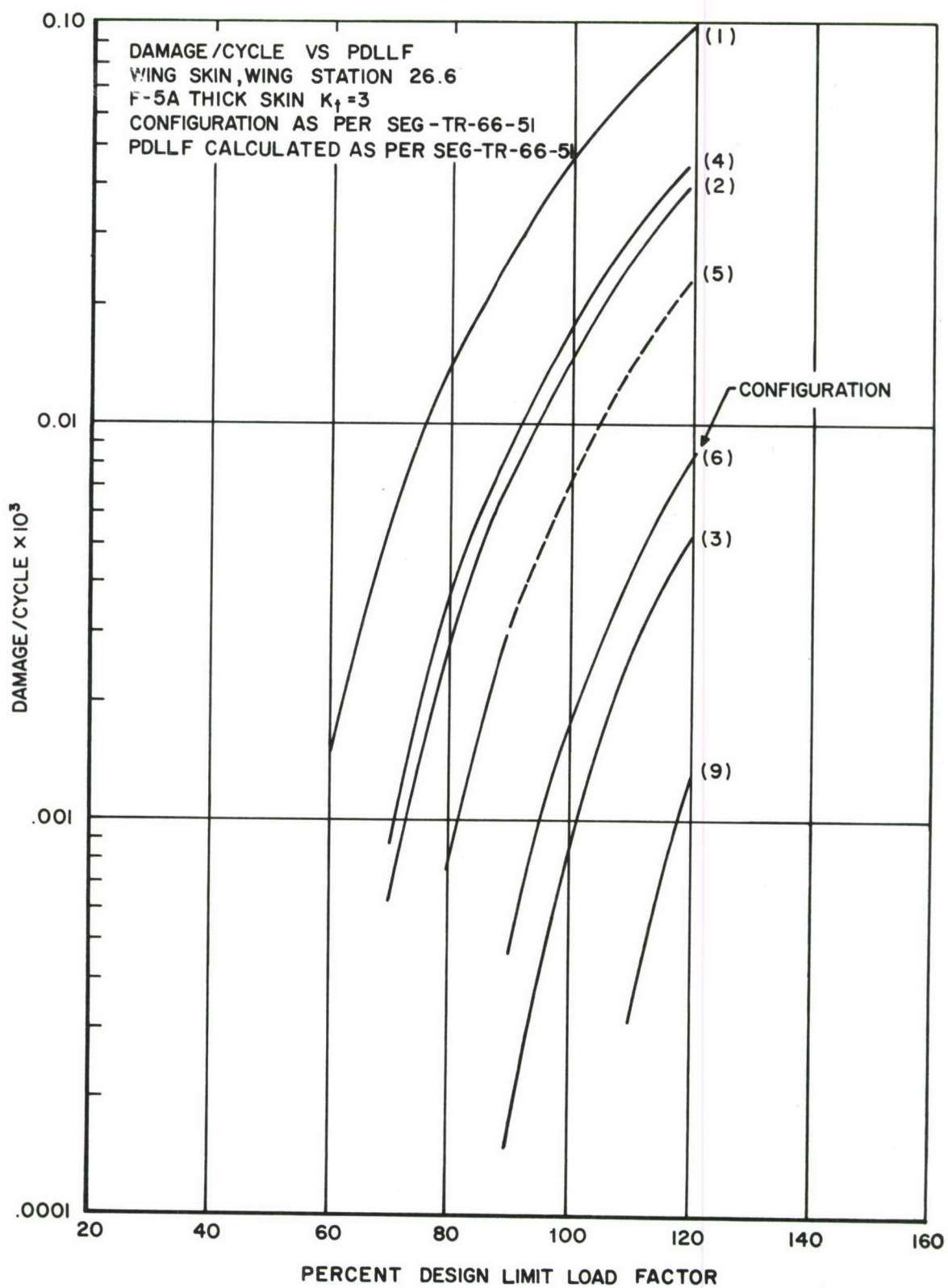
Figure 1  Fatigue Damage per Occurrence of Percent Design Limit
Load Factor for Various Stores Configurations
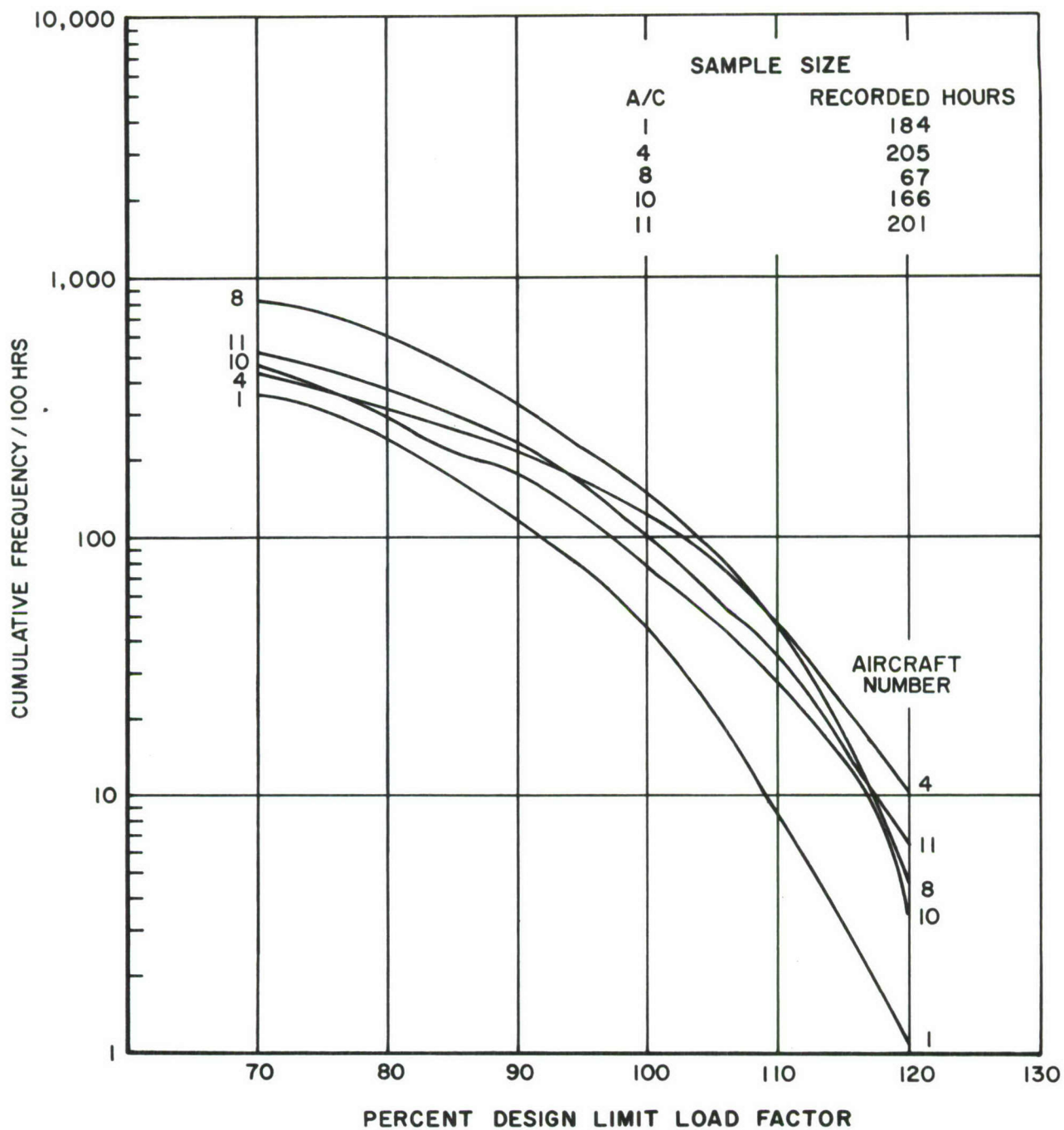
Figure 2   Cumulative Frequency Distribution of Percent Design
Limit Load Factor for Five Different F5A Aircraft

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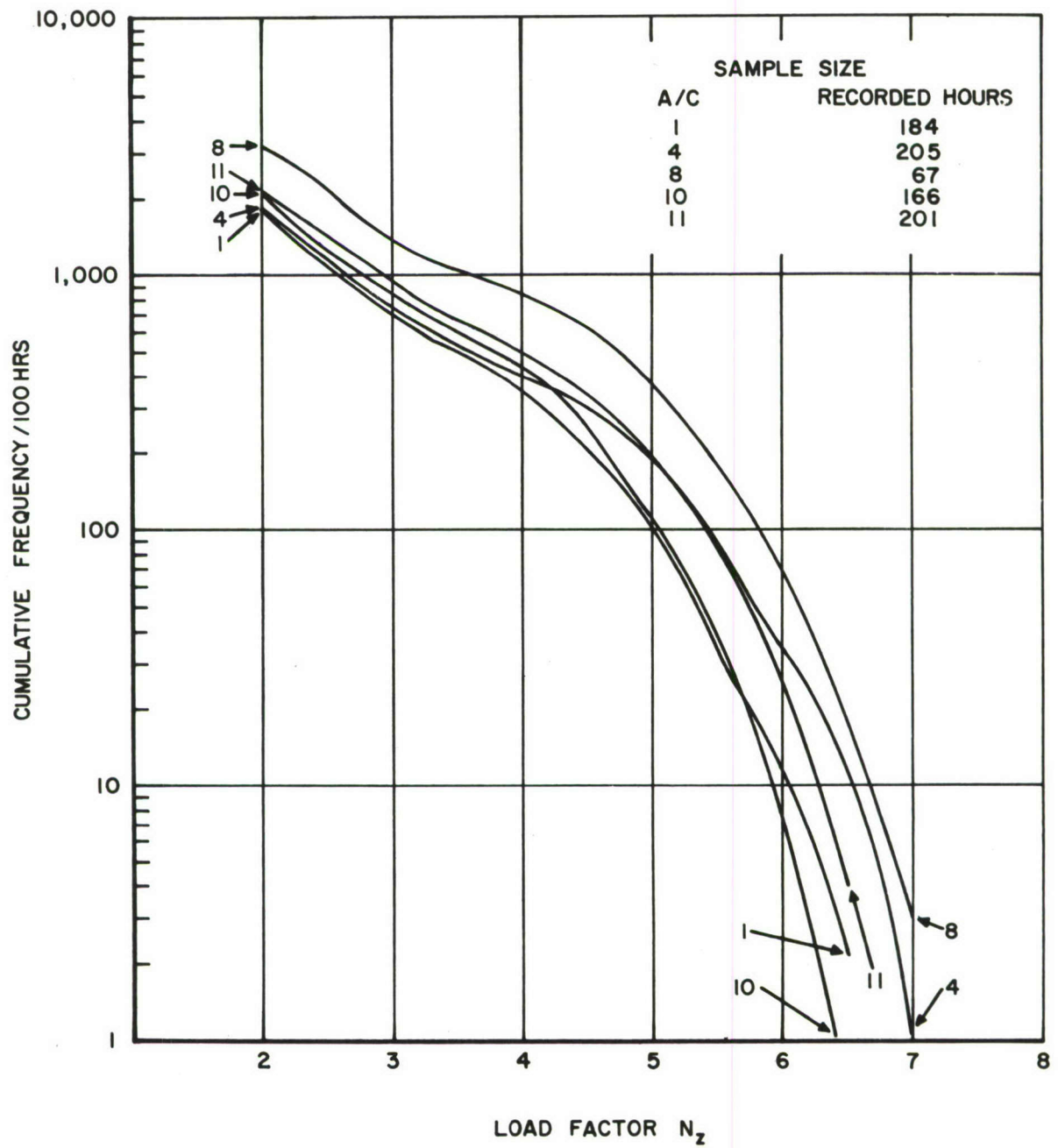
Figure 3    Cumulative Frequency Distribution of Load Factors
for Five Different F5A Aircraft

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## 2.    F-105D AIRCRAFT

The purpose of this analysis is to determine the relative importance of each of the parameters affecting fatigue damage and to determine what parameters must be known to conduct a tail number fatigue damage monitoring program for the F-105D. The fatigue damage analysis reported herein is based on a 3,056 hour VGH data sample obtained in the Southeast Asia combat zone. The data was recorded on 1,319 flights from two air bases as reported in Reference 5.

### a.    Fatigue Damage Analysis

For the purpose of this study the fatigue damage was calculated for two critical locations, the transfer spar at fuselage station 442 and the top cover skin at the access door at fuselage station 509. Stress versus center of gravity normal load factor curves were extracted from a computer program output tab obtained from Republic Aviation. These stresses were used with the S-N curves presented in Figures 4 and 5 to calculate damage rates for 185 combinations of Mach number, altitude, gross weight, and major configuration.

For purposes of classifying the data at any time during flight, five major and 23 minor configurations were defined for the aircraft. The definition of these configurations is presented in Table V. Only the classification by major configuration was utilized in this analysis.

The Mach-altitude conditions were categorized into blocks for purposes of calculating damage. The points for which damage was calculated as defined in Reference 6 are shown in Table VI. Grouping of all possible flight conditions into the Mach-altitude conditions shown was determined, in the reference, to be sufficient for computing aircraft damage.

The aircraft gross weight was defined in increments of two-thousand pounds between 34,000 and 42,000 pounds. Damages for gross-weights less than 34,000 pounds were computed at 33,000 pounds and gross weights greater than or equal to 42,000 pounds were computed at 44,000 pounds. Damage was computed for all load factors greater than or equal to 2.5 g's in 0.5 g increments. Load factors less than 2.5 g's did not cause fatigue damage to the aircraft at the two locations being monitored. The classification of the data by load factor level used in this analysis is presented in Table VII. Load factor peaks were defined during the reduction of the data according to the following criteria: (1) the incremental peak value must be at least ±1.0 g from the 1.0 g level flight condition, and (2) the trace must have a rise and fall of at least 1.0 g and 50 percent of the incremental peak value.

All damages computed for this analysis were found by treating each load factor occurrence as an independent stress cycle. The damages were then accumulated utilizing Miner's linear comulative damage rule. This rule is stated mathematically as follows:

$$D = \sum_{i=1}^{j} \frac{n_i}{N_i}$$

where      $N_i$ = Number of cycles to failure under a specified cyclic loading condition i

           $n_i$ = Number of cycles experienced at a specified loading condition

           D = Accumulated damage

           j = Number of loading conditions experienced

Failure is indicated when the accumulated damage D is equal to one.

    (1)   Parametric Analysis

        The variation of the damage rate with configuration and load factor for a typical Mach-altitude-gross weight combination is presented in Figures 6 and 7 for fuselage stations 442 and 509, respectively. Examination of these figures reveals that damage is quite dependent on major configuration. For an $N_z$ value of 4 there is an order of magnitude difference at fuselage station 509. At fuselage station 442 the difference in the damages varies by a factor of four.

        The variation of damage rate with gross weight and load factor for a typical Mach-altitude-configuration is presented in Figures 8 and 9 for fuselage stations 442 and 509, respectively. As might be expected, the fatigue damage is much more sensitive to gross weight at fuselage station 442 than at fuselage station 509. This is due to the fact that the stress at fuselage station 442 is dependent on the wing loading, whereas the stress at fuselage station 509 is only indirectly related to the wing loading.

        The variation of damage rate with load factor and gross weight for a typical Mach-altitude-configuration combination is presented in Figures 10 and 11. This is a cross-plot of the data in Figures 8 and 9. The damage rate at both aircraft locations is sensitive to load factor magnitude at all aircraft gross weights. The decrease in damage sensitivity to load factor at fuselage station 442 for the higher load factor levels reflects the effects of wing tip stalling.

        The variation of the damage rate with Mach-altitude block and load factor for a typical gross weight-configuration combination is shown in Figures 12 and 13 for fuselage stations 442 and 509, respectively. The effect of wing tip stalling is reflected in the damage rate at fuselage station 442 by the gross nonlinearity at the higher values of normal load factor.

During the data acquisition program, the mission types which the F-105D aircraft was expected to experience in the SEA combat zone were divided into six classifications. Ninety-six percent of the flight hours, 92 percent of the load factor occurrences, and 92 percent of the flights occurred during the mission type denoted as conventional bombing. Therefore, mission type was eliminated as a variable for the purposes of this analysis.

The results of the damage sensitivity study reveal that damage rate is most sensitive to normal load factor. Gross weight and configuration are also of importance along with the Mach-altitude condition.

(2) Damage Analysis by Mission Segment

The airborne portion of the flight was classified into the mission segments of ascent, maneuver, cruise, refuel, and descent. Based on the results of Reference 1, it was anticipated that a large percent of the damage experienced by the F-105D would occur during the maneuver mission segment. This was further verified for the F-105D Southeast Asia combat data sample reported in Reference 5. Computer tabs for each flight contained in the F-105D SEA data sample reported in Reference 5 were obtained from Technology Incorporated, Dayton, Ohio, and damages were computed for each of the 10,610 $N_z$ occurrences having a magnitude greater than or equal to 2.5 g's. The results are presented in Tables VIII and IX for fuselage stations 442 and 509, respectively. Approximately 99 percent of the total damage, exclusive of the ground-air-ground cycle, occurred during the maneuver mission segment (mission segment 2) at both aircraft fatigue critical locations.

(3) Analysis of Maneuver Mission Segment Data

On the basis of the data presented in Tables VIII and IX, the parametric analysis was confined to the determination of damage in the maneuver mission segment. If damage prediction techniques can be developed for this portion of the flight, the damage occurring in all other mission segments can be neglected as insignificant.

The damage in the maneuver mission segment was separated into two categories; maneuvering in the target area and pull-up after weapon release. The results of these calculations are presented in Tables X and XI for fuselage stations 442 and 509, respectively. It can be concluded that in general more than three-fourths of the total aircraft damage, exclusive of the ground-air-ground cycle, occurs during pull-up after weapon release for both fatigue critical points under consideration.

b. Damage Prediction Techniques

Based on the relative importance of the load factor occurrences during pull-up after weapon release, the primary effort was directed toward development of a method for predicting damage resulting from these occurrences.

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(1) Mach-Altitude Probability Technique

On the basis of the findings of Section II -2a and of Reference 1, a damage prediction technique based on Mach-altitude probability was investigated. The Mach-altitude probabilities as a function of load factor and configuration and independent of gross weight were determined for the pull-up data. The total data sample of pull-up occurrences was divided into four groups by aircraft tail number as defined in Table XII. The aircrafts were divided into four groups in an attempt to show that a damage model derived from a few aircraft could be used to predict the damage on the remaining aircraft in the fleet. Each group contained a representative sample by base and hours of data recorded as reported in Table 6 of Reference 5. Table XIII of this report shows the distribution of pull-up occurrences by group and by configuration. Approximately 83 percent of all pull-ups occurred in exit Configuration 3. Therefore, the exit Configuration 3 data was selected for analysis.

The Mach-altitude probabilities for Configuration 3 by group and by load factor level are presented in Table XIV. As can be seen, the probability distributions as a function of load factor are in general slightly skewed, indicating some correlation between Mach number and load factor magnitude. Representative three-dimensional Mach-altitude probability plots for the Group I and total Configuration 3 data samples are presented in Figures 14 and 15, respectively. These plots are independent of load factor level. Figure 16 shows these pull-up distributions with the altitude variable eliminated. The consistency of the data by Group is further exemplified by cross-plotting the data presented in Table XIV. These results in the form of histograms showing the probability of occurrences as a function of load factor level are presented in Figure 17.

The fatigue damage due to pull-up after weapon release for the F-105D aircraft was calculated using two different Mach-altitude probability models. The first model was based on the Mach-altitude probabilities associated with the exit Configuration 3 pull-ups experienced by the Group I aircraft. The second model was based on the total exit Configuration 3 pull-up experience.

The probability of occurrence for each Mach-altitude block was determined as a function of load factor level and independent of aircraft gross weight. The damage per occurrence as a function of Mach-altitude block and load factor level was then determined for each aircraft gross weight condition. This data was used with the probability model to calculate damage per occurrence as a function of load factor level and gross weight. This calculation is represented mathematically by the following equation:

$$D_{ki} = \sum_{j=1}^{n} P_{ij} d_{kij}$$

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$P_{ij}$  = probability of occurrence of Mach-altitude block j at load factor level i

$d_{kij}$  = damage at load factor level i, Mach-altitude block j and gross weight k

$D_{ki}$  = predicted damage per occurrence at load factor level i and aircraft gross weight k

These calculations resulted in a matrix of $D_{ki}$ as a function of gross weight and load factor. These results are presented in Tables XV and XVI for the two aircraft locations and Mach-altitude probability models. Each pull-up occurrence was then assigned a damage $D_{ki}$ and the total damage was found by summing over the total number of occurrences.

The results of these calculations are presented in Tables XVII through XX. Tables XVII and XVIII show the damage predicted using the Group I probability model for the top cover skin at fuselage station 509 and the transfer spar at fuselage station 442, respectively. The variation in the ratio of the predicted damage to the calculated damage is greater than had been expected. Tables XIX and XX show the corresponding data for the probability model constructed from the total data sample. Based on these results, it appears that the damage predicted for an individual aircraft using this technique is subject to a significant error. This can probably be attributed to the diverse experience accumulated on a fighter aircraft of this type in a combat zone.

The correlation between the ratio of the predicted damage to the actual damage and the sample size for an individual aircraft is presented in Figures 18 and 19 for the two aircraft fatigue critical locations. Each point on the curve represents the experience for a particular aircraft. The top curve on each figure connects those points for which the predicted damage was too high, the bottom curve connects those points for which the predicted damage was too low. Examination of these curves reveals that there is little improvement in the damage ratio within the range of the sample size represented.

(2)  Evaluation of Damage Prediction Techniques

Comparison of the fatigue damage predicted by the Mach-altitude probability technique with damage predictions based on per-hour, per-flight, and per pull-up calculations is presented in Tables XXI and XXII. The actual damages on which these comparisons are based are presented in Tables XXIII through XXVII. It should be noted that not all damage ratios are computed from a common basis. The per hour and per flight ratios are based on the damage for the total SEA data sample. However, the damage ratios for the pull-ups and the Mach-altitude prediction model are based on the damage due to pull-up after weapon release in exit Configuration 3.

A qualitative examination of the results presented in Tables XXI and XXII does not suggest a strong preference for any of the damage prediction techniques under consideration. Therefore, a statistical evaluation of the four techniques was attempted. First, the available data was truncated by arbitrarily eliminating those aircraft that experienced less than twenty-eight pull-ups. Next the damage ratios were assumed to be an indicator of the relative merit of the different techniques and the variance was computed independently for each of the damage prediction techniques using the formula

$$S^2 = \frac{n\Sigma(X_i)^2 - (\Sigma X_i)^2}{n(n-1)}$$

where        $S^2$  =  sample variance

                n   =  sample size

                $X_i$  =  the i th data point in sample n

The results of these calculations are presented in Table XXIX for fuselage stations 509 and 442. A significance test was made on the variances assuming that the deviations have a Gaussian distribution. For a probability of 1 in 20 ($\alpha$=.05) of concluding that there was a difference when there was not, there was no significant statistical difference in the variances. However, a qualitative comparison shows a trend which indicates that the variance in the tail number fatigue damage prediction for a fleet of aircraft can be minimized by using the Mach-altitude probability prediction technique. The relative advantage of the method is greater at fuselage station 509 than for fuselage station 442.

(3)   Refinement of Damage Prediction Techniques

Initially it was assumed that the accumulated fatigue damage could be predicted independently of air base for the SEA data sample. This assumption was based on a qualitative evaluation of the data presented in Reference 5, the results presented in Reference 1, and the desire to minimize the number of variable required for damage prediction.

Examination of the data contained in Tables XXIII through XXVIII reveals that there is a difference in the damage rates at the two bases, particularly at fuselage station 509. Therefore, the fatigue damage was calculated using the damage rates at each base on a per-hour, per-flight, and per-pull-up basis. The resulting damage ratios are presented in Table XXX. The variances for these data were calculated using the same ground rules as were employed in the previous section. The results of these calculations are shown at the bottom of Table XXX. There was no significant improvement in the variances at either aircraft location as a result of considering the samples obtained at each base to be independent.

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Due to the differences in fatigue damage prediction, utilizing the Mach-altitude probability technique, between this investigation and that reported in Reference 1, it was decided to investigate the possibility that more than one statistical population was contained in the total F-105D SEA data sample. To accomplish this a Mach-altitude probability model was formulated from the first 114 Configuration 3 pull-up occurrences. Another model was constructed from the last 114 Configuration 3 pull-ups contained in the data sample (pull-ups 1084 through 1198).

The three dimensional Mach-altitude probability plots for these two models are presented in Figures 20 and 21. Comparison of these two figures reveals some difference in the aircraft utilization. The primary difference is in the Mach 1.2 probability. Since this Mach-altitude block encompasses all altitudes, it is difficult to determine from the plots whether the difference reflects a variation in airspeed, altitude, or both. Examination of the altitude for each of the occurrences at Mach 1.2 showed them to be comparable. Therefore, it was concluded that the increase in the number of occurrences at Mach 1.2 could be attributed to an increase in the airspeed at the time of pull-up after weapon release for the last 114 pull-ups. Comparison of Figures 20 and 21 with Figure 15 reveals that the Mach-altitude probability plot for the last 114 pull-ups agrees more closely with the corresponding plot for the total Configuration 3 Mach-altitude probabilities, particularly at Mach 1.2.

The first of these models was used to predict damage for the first 114, first 228, and first 345 Configuration 3 pull-up occurrences as well as for the total data sample. The results of these calculations are presented in Table XXXI in the form of damage ratios. The variance with the corresponding sample size is shown at the bottom of each column for fuselage stations 509 and 442, respectively. Although the damage ratio deviates from one by a considerable margin for the total data sample, the variance decreases with increasing data sample size. This might be expected since fighter aircraft in combat utilization generally show a large scatter in the amount of damage accumulated on any one given flight. In addition, it should be noted that the sample size N for which the variance is calculated increases as the data sample is expanded to include more aircraft. Therefore, this difference must be accounted for in interpreting the variances.

The corresponding results for the predicted damage using the Mach-altitude probability model for the last 114 pull-ups are shown in Table XXXII. The results are similar to those obtained from the Mach-altitude probability model based on the first 114 Configuration 3 pull-ups. It is interesting to note that the actual damage predicted for the total data sample using the model from the last 114 pull-ups is considerably better at both aircraft fatigue critical locations, as would be expected from the results of comparing the Mach-altitude probability plots. However, the variance is minimized for the non-truncated data sample if the model based on the first 114 pull-ups is used. For the truncated data sample presented in Table XXXIII, the variance is smaller for the model based on the last 114 pull-ups.

The total damage due to the 1198 Configuration 3 pull-ups has now been predicted using four different Mach-altitude probability models (i.e., models based on the Group I pull-ups, the total pull-ups, the first 114 pull-ups, and the last 114 pull-ups). The damage ratios and the variances for the truncated data sample are shown in Table XXXIII for comparison.

(4) Other Maneuvering in Target Area

Approximately twenty to twenty-five percent of the fatigue damage, exclusive of the ground-air-ground cycle, resulted from load factor occurrences other than pull-up after weapon release (see Tables X and XI). This data was analyzed to see if the Mach-altitude probability damage prediction technique could be utilized for predicting this damage.

Probability distributions of the pull-up after weapon release and the pull-ups due to other maneuvering in the target area were plotted. These results are presented in Figure 22. The plot for pull-up after weapon release is for the total Configuration 3 pull-ups. The plots for the load factor occurrences due to other maneuvering in the target area are for two typical aircraft, one at each base. The distribution of the pull-ups is approximately symmetrical about a mean of 4.7 to 5.2 g's. The distribution of the non-pull-up data displays the shape of the familiar exponential exceedance curve.

It was anticipated that the Mach-altitude probability data might lend itself to division into two models according to load factor magnitude. The total Configuration 3 pull-up data sample was separated into two parts; load factor peaks $\geq 4.2$, and load factor peaks $\leq 3.7$. The corresponding Mach-altitude probability models are presented in Figure 23. As was pointed out previously, there is some correlation between Mach number and load factor magnitude.

Next, it was attempted to correlate the Mach-altitude probability distribution for the non-pull-up data, independent of load factor magnitude, with the Mach-altitude probability for pull-ups having a load factor magnitude $\leq 3.7$. The Mach-altitude probability distributions for the non-pull-up data in the maneuver mission segment for aircraft serial numbers 130 and 422 are presented in Figure 24. Comparison of Figure 24 with Figure 23 reveals some similarity, with respect to Mach number, between the two probability models.

Although this investigation showed some promise, application of the method for predicting fatigue damage due to the non-pull-up load factors was not pursued further because of the relative lack of success encountered in predicting the damage due to pull-up after weapon release.

c. Discussion

The prediction of accumulated fatigue damage on a fighter aircraft presents a formidable problem. There are a multitude of parameters that affect the fatigue life. Some of these remain constant during the life of the aircraft while others are quite sensitive to aircraft utilization.

Laboratory fatigue test results on controlled specimens subjected to cyclic loads having constant amplitude alternating and mean stresses show a significant scatter factor in fatigue life. If one were to use any of the prediction techniques presented to this point he would have to increase the scatter factor by a factor of two due to the usage.

Efforts to predict the stress level encountered during operation of fighter aircraft are complicated by the wide latitude in usage. Loads encountered on a specific mission are affected by the pilot, the type and location of the target, enemy activity, visibility and weather conditions. Mission definition is dependent on base location, intensity of the conflict and military philosophy, and is subject to continuous redefinition. Therefore, it would seem that a fighter aircraft deployed in a combat zone could be expected to experience a random input spectrum with regard to fatigue damage accumulation. Thus, in the authors' opinion, the use of statistical methods for predicting fatigue damage could not rationally be expected to yield precise results.

The relative merits of the various methods employed to predict fatigue damage to the F-105D aircraft are not easily defined. For the data sample analyzed, there was no significant difference in the ability of the various methods used. However, care must be exercised in generalizing these results to the total problem of evaluating the accumulated fatigue damage to the aircraft for all utilization. For example, the damage rate per hour would be quite sensitive to target location relative to the base. The damage rate per flight would be more sensitive to target type and the weapon delivery modes. The damage per pull-up would be sensitive to target topography and fortification as well as pilot reaction and time of day. This means that continuous flight load or strain recording would be necessary on a number of aircraft to provide a basis for establishing and revising damage rates or damage prediction models. This might be required on a squadrom basis or an even finer breakdown depending on the aircraft utilization.

Keeping these general observations in mind, the following specific remarks concerning the analysis reported herein are presented. There was some advantage in the Mach-altitude probability technique of damage prediction. This advantage was not significant for the data sample analyzed. However, the advantage might be more distinct for a more general data sample.

A comparison of the variances for the different Mach-altitude probability models presented in Table XXVII indicates that better results are obtained when the model is based on a chronological sample rather than a sample by aircraft serial number. This indicates that there was a greater inconsistency with respect to aircraft serial number than with mission variation. This was also true for the data sample reported in Reference 1. However, the basic differences between the results of this study and those of Reference 1 can apparently be attributed to the difference in the S-N curves and the Mach-altitude breakdown used in the two studies. The S-N curves used in Reference 1 attached more significance

to the damage resulting from the high load factor levels whereas the damage at the lower load factor levels was the same in both studies. The S-N data used in the Reference 1 study for life cycles less than 300 was extrapolated by the University of Dayton whereas the data for this study used data extrapolated by Republic Aviation. The study in Reference 1 placed all Mach numbers greater than .9 at .92 whereas this study placed Mach numbers greater than .95 at Mach 1.2. Reference to Figures 12 and 13 will show the significance of this Mach effect. Also the stress vs. $N_z$ data were calculated based on the SEA Weapon Configuration whereas Reference 1 used stresses based on peacetime training flights that had approximately the same configuration.

In view of the results of this study there appear to be three alternatives available for achieving, with some degree of success, the objectives of the Air Force Fatigue Certification Program and the Aircraft Structural Integrity Program.

(1) The first alternative would be the use of per-hour, per-flight or per pull-up calculations. This would require instrumentation of a portion of the fleet to provide damage rates for the remainder of the fleet. Considering the diverse utilization of fighter aircraft, this method has some obvious shortcomings as discussed previously and the confidence in the predicted damage, particularly on an aircraft serial number basis, would be low.

(2) A second alternative would be to install a peak counting accelerometer on each aircraft, together with the necessary instrumentation and logic circuitry for determining Mach number, altitude, gross weight, and configuration at the time of each load factor occurrence. The load factor occurrences would be segregated by these parameters and recorded in storage registers. The number of storage registers would be equal to the product of the number of bands required for each of the parameters. If the data were categorized by the five major configurations, 11 load factor levels, six gross weights, and the Mach-altitude breakdown of Table VI a total of 3,310 storage registers would be required. For the SEA data sample analyzed during this study, the number of storage registers could be reduced to 396 with little loss in accuracy. This number could be pared even further by accepting some sacrifice in accuracy.

Although this method of monitoring fatigue damage eliminates the cost of recording and processing VGH time history data, it still requires a fairly sophisticated instrumentation and recording system. Also, while it is relatively easy to eliminate or consolidate variables, and thus decrease the number of storage registers required, for a given data sample the judicious choice of these variables without this prior knowledge would prove a more difficult problem.

(3) The third alternative would be to eliminate the necessity for knowing parameters such as gross weight, configuration, airspeed, altitude and load factor. This could be accomplished by using a strain amplitude cycle counter.

The frequency at which selected strain levels were equaled or exceeded could be sensed and recorded in accumulating storage registers. This strain exceedance data could then be used directly with an S-N curve to determine the cumulative damage at a fatigue critical location. Since only the magnitude of the strain peaks would be measured, a constant mean stress could be assumed or the mean stress could be expressed as a function of the aircraft gross weight and configuration. However, this added breakdown of the peaks would require additional storage registers.

# TABLE V

## Major and Minor Configuration Definition for F-105D

| Major Config. | Minor Config. | Center Line Station | Inboard Station | Outboard Station |
|---|---|---|---|---|
| 1 | A | Clean | Clean | Clean |
| 1 | B | Clean | Clean | Any Store |
| 1 | C | Clean | ≤1000# Store | Clean |
| 1 | D | Clean | ≤1000# Store | ≤700# Store |
| 1 | E | Any Store | Clean | Clean |
| 1 | F | Any Store | Clean | Any Store |
| 1 | G | Any Store | ≤1000# Store | Clean |
| 1 | H | Any Store | ≤1000# Store | ≤700# Store |
| 1 | I | 650 Gal. Tank | Clean | Clean |
| 1 | J | 650 Gal. Tank | Clean | Any Store |
| 1 | K | 650 Gal. Tank | ≤1000# Store | Clean |
| 1 | L | 650 Gal. Tank | ≤1000# Store | ≤700# Store |
| 2 | M | 650 Gal. Tank | >700# Store | >700# Store |
| 2 | N | 650 Gal. Tank | >1000# Store | Clean |
| 2 | O | 650 Gal. Tank | >1000# Store | Any Store |
| 3 | P | Clean | 450 Gal. Tank | Clean |
| 3 | Q | Clean | 450 Gal. Tank | ≤700# Store |
| 3 | R | ≤1000# Store | 450 Gal. Tank | Clean |
| 3 | S | ≤1000# Store | 450 Gal. Tank | ≤700# Store |
| 4 | T | Clean | 450 Gal. Tank | >700# Store |
| 4 | U | ≤1000# Store | 450 Gal. Tank | >700# Store |
| 5 | V | >1000# Store | 450 Gal. Tank | Clean |
| 5 | W | >1000# Store | 450 Gal. Tank | Any Store |

TABLE VI

F-105D Mach-Altitude Subdivision for Damage Calculations

| Altitude | Mach Numbers | | | | | |
|---|---|---|---|---|---|---|
| | | .65 | | .85 | .92 | 1.2 |
| 1,000 | M=.70 | | 2,000 ⬡ | ⬡ | ⬡ | |
| | | | M = .90 → | | 5,000 | M=.95 |
| 7,000 | 10,000 ⬡ | | ⬡ | ⬡ | | |
| 12,000 | | | 15,000 → | ⬡ | | |
| 20,000 | ⬡ | | ⬡ | ⬡ | ⬡ | |

TABLE VII

Load Factor Definition Used for Computing F-105D Damages

| Load Factor Interval | Value for Which Damage was Computed |
|---|---|
| ≥ 2.5 - < 3.0 | 2.7 |
| ≥ 3.0 - < 3.5 | 3.2 |
| ≥ 3.5 - < 4.0 | 3.7 |
| ≥ 4.0 - < 4.5 | 4.2 |
| ≥ 4.5 - < 5.0 | 4.7 |
| ≥ 5.0 - < 5.5 | 5.2 |
| ≥ 5.5 - < 6.0 | 5.7 |
| ≥ 6.0 - < 6.5 | 6.2 |
| ≥ 6.5 - < 7.0 | 6.7 |
| ≥ 7.0 - < 7.5 | 7.2 |
| ≥ 7.5 | 7.7 |

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# TABLE VIII

## Tabulation of Damage by Mission Segment for the F-105D Transfer Spar at Fuselage Station 442 by A/C Serial Number

| 1 | 2 | 3 | 4 | 5 |
|---|---|---|---|---|
| | | Damage Summary | | |
| A/C | M.S.2 (Maneuver) | All Other M.S. | Total | $\frac{\text{Damage M.S.2}}{\text{Total Damage}} \times 100$ |
| 130 | .047292898 | .000135848 | .047428746 | 99.71 |
| 160 | .007393539 | .000046220 | .007439759 | 99.38 |
| 240 | .024659128 | .000122500 | .024781628 | 99.51 |
| 357 | .016063090 | .000020446 | .016083536 | 99.87 |
| 367 | .037294519 | .000258924 | .037553443 | 99.31 |
| 720 | .000035452 | --------- | .000035452 | 100.00 |
| 731 | .003086485 | .000023310 | .003109795 | 99.25 |
| 732 | .029523458 | .000183697 | .029707155 | 99.38 |
| 762 | .000428973 | .000003754 | .000432727 | 99.13 |
| Subtotal Base 1 | .165777542 | .000794699 | .166572241 | 99.52 |
| 68 | .024607462 | .000177036 | .024784498 | 99.29 |
| 69 | .034840997 | .000121454 | .034962451 | 99.65 |
| 132 | .042614288 | .000151869 | .042766157 | 99.64 |
| 167 | .003267466 | .000012909 | .003280375 | 99.61 |
| 205 | .030545950 | .000165749 | .030711699 | 99.46 |
| 352 | .004220838 | .000001384 | .004222222 | 99.97 |
| 378 | .045659687 | .000143400 | .045803087 | 99.69 |
| 422 | .011572689 | .000089483 | .011662172 | 99.23 |
| 424 | .003939580 | .000003434 | .003943014 | 99.91 |
| 469 | .005396200 | .000029239 | .005425439 | 99.46 |
| Subtotal Base 2 | .206665157 | .000895957 | .207561114 | 99.57 |
| Total | .372442699 | .001690656 | .374133355 | 99.55 |

## TABLE IX

Tabulation of Damage by Mission Segment for the F-105D
Top Cover Skin at Fuselage Station 509 by A/C Serial Number

### Damage Summary

| A/C | M.S. 2 (Maneuver) | All Other M.S. | Total | $\dfrac{\text{Damage M.S. 2}}{\text{Total Damage}} \times 100$ |
|---|---|---|---|---|
| 130 | .015133408 | .000144693 | .015278101 | 99.05 |
| 160 | .004614652 | .000044801 | .004659453 | 99.04 |
| 240 | .006885296 | .000103627 | .006988923 | 98.52 |
| 357 | .004427206 | .000017938 | .004445144 | 99.60 |
| 367 | .011342031 | .000322921 | .011664952 | 97.23 |
| 720 | .000008603 | --------- | .000008603 | 100.00 |
| 731 | .000729279 | .000023988 | .000747140 | 97.61 |
| 732 | .010193342 | .000205703 | .010399045 | 98.02 |
| 762 | .000060579 | .000004671 | .000065250 | 92.84 |
| Subtotal Base 1 | .053394396 | .000868342 | .054256611 | 98.41 |
| 68 | .012076296 | .000157801 | .012234097 | 98.71 |
| 69 | .014791108 | .000110809 | .014901917 | 99.26 |
| 132 | .019692062 | .000139962 | .019832024 | 99.29 |
| 167 | .001108912 | .000015433 | .001124345 | 98.63 |
| 205 | .011121770 | .000135154 | .011256924 | 98.80 |
| 352 | .003049063 | .000000493 | .003049556 | 99.98 |
| 378 | .025906307 | .000172216 | .026078523 | 99.34 |
| 422 | .003900497 | .000056418 | .003956915 | 98.57 |
| 424 | .001561174 | .000001320 | .001562494 | 99.91 |
| 469 | .001750460 | .000020006 | .001770466 | 98.87 |
| Subtotal Base 2 | .094957649 | .000809612 | .095767261 | 99.15 |
| Total | .148352045 | .001677954 | .150023872 | 98.89 |

## TABLE X

Tabulation of Damage due to Pull-up after Weapon Release for
Transfer Spar at Fuselage Station 442 on F-105D Aircraft

| A/C | Number of Pull-up | Damages M.S. 2 (Maneuver) | Pull-up after Weapon Release | $\dfrac{\text{Damage Pull-up}}{\text{Damage M.S. 2}} \times 100$ |
|---|---|---|---|---|
| 130 | 126 | .047292898 | .037451294 | 79.19 |
| 160 | 40 | .007393539 | .003290226 | 44.50 |
| 240 | 128 | .024659128 | .017532723 | 71.10 |
| 357 | 54 | .016063090 | .014507099 | 90.31 |
| 367 | 137 | .037294519 | .024853427 | 66.64 |
| 720 | 0 | .000035452 | - - - - - - | - - - |
| 731 | 15 | .003086485 | .002817961 | 91.30 |
| 732 | 148 | .029523458 | .023655876 | 80.13 |
| 762 | 4 | .000428973 | .000421885 | 98.35 |
| Subtotal Base 1 | | .165777542 | .124530491 | 75.12 |
| 68 | 130 | .024607462 | .020583639 | 83.65 |
| 69 | 116 | .034840997 | .030027328 | 86.18 |
| 132 | 123 | .042614288 | .033047298 | 77.55 |
| 167 | 12 | .003267466 | .002917203 | 89.28 |
| 205 | 138 | .030545950 | .028625917 | 93.71 |
| 352 | 9 | .004220838 | .003880182 | 91.93 |
| 378 | 149 | .045659678 | .038848251 | 85.08 |
| 422 | 77 | .011572689 | .009992032 | 86.34 |
| 424 | 11 | .003939580 | .003492819 | 88.66 |
| 469 | 31 | .005396200 | .004706186 | 87.21 |
| Subtotal Base 2 | | .206665157 | .176120855 | 85.22 |
| Total | | .372442699 | .300651346 | 80.72 |

## TABLE XI

Tabulation of Damage due to Pull-up after Weapon Release for
Top Cover Skin at Fuselage Station 509 on F-105D Aircraft

| A/C | Number of Pull-up | Damages | | $\dfrac{\text{Damage Pull-up}}{\text{Damage M.S. 2}} \times 100$ |
| | | M.S. 2 (Maneuver) | Pull-up after Weapon Release | |
|---|---|---|---|---|
| 130 | 126 | .015133408 | .012318943 | 81.40 |
| 160 | 40 | .004614652 | .002038340 | 44.17 |
| 240 | 128 | .006885296 | .004977942 | 72.30 |
| 357 | 54 | .004427206 | .004022334 | 90.85 |
| 367 | 137 | .011342031 | .007289099 | 64.27 |
| 720 | 0 | .000008603 | - - - - - | - - - |
| 731 | 15 | .000729279 | .000649082 | 89.00 |
| 732 | 148 | .010193342 | .007854239 | 77.05 |
| 762 | 4 | .000060579 | .000058955 | 97.32 |
| Subtotal Base 1 | | .053394396 | .039208934 | 73.43 |
| 68 | 130 | .012076296 | .007970412 | 66.00 |
| 69 | 116 | .014791108 | .012399450 | 83.83 |
| 132 | 123 | .019692062 | .015785158 | 80.16 |
| 167 | 12 | .001108912 | .000723382 | 65.23 |
| 205 | 138 | .011121770 | .009894261 | 88.96 |
| 352 | 9 | .003049063 | .002971337 | 97.45 |
| 378 | 149 | .025906307 | .018890256 | 72.91 |
| 422 | 77 | .003900497 | .003199132 | 82.02 |
| 424 | 11 | .001561174 | .001290189 | 82.64 |
| 469 | 31 | .001750460 | .001594274 | 91.08 |
| Subtotal Base 2 | | .094957649 | .074717801 | 78.69 |
| Total | | .148352045 | .113926735 | 76.79 |

## TABLE XII

Data Groups for Probability Analysis of Load Factor
Occurrences During Pull-up after Weapon Release

| Group | Aircraft No. |
|---|---|
| 1 | 130, 132, 357, 422 |
| 2 | 160, 240, 378, 469 |
| 3 | 731, 732, 69, 167 |
| 4 | 367, 720, 762, 68, 205, 352, 424 |

## TABLE XIII

Distribution of Pull-up Peaks by Group and Configuration

Number of Pull-up Occurrences

| Group | Configuration | | | | | Total |
|---|---|---|---|---|---|---|
| | 1 | 2 | 3 | 4 | 5 | |
| 1 | 32 | 1 | 309 | 4 | 34 | 380 |
| 2 | 26 | 1 | 290 | 7 | 24 | 348 |
| 3 | 18 | 4 | 245 | 6 | 18 | 291 |
| 4 | 32 | 6 | 354 | 0 | 37 | 429 |
| Total | 108 | 12 | 1198 | 17 | 113 | 1448 |

### TABLE XIV

## Mach-Altitude Probability Distribution for F-105D, Configuration 3 Pull-up After Weapon Release

### Mach-Altitude Blocks

| $N_z$ | .65 7 | .65 20 | .85 1 | .85 7 | .85 20 | .92 1 | .92 7 | .92 12 | .92 20 | 1.2 20 |
|---|---|---|---|---|---|---|---|---|---|---|
| **Group 1 Probabilities** | | | | | | | | | | |
| 2.7 | .500 | | | .500 | | | | | | |
| 3.2 | .182 | | | .818 | | | | | | |
| 3.7 | .210 | | | .737 | | | | | | .053 |
| 4.2 | .057 | | .029 | .629 | .029 | | .143 | | | .114 |
| 4.7 | | | | .632 | .015 | .044 | .147 | | | .161 |
| 5.2 | | | .029 | .629 | | .014 | .114 | | | .214 |
| 5.7 | | | .036 | .473 | | .091 | .182 | | | .218 |
| 6.2 | | | .039 | .500 | | .077 | .039 | | | .346 |
| 6.7 | | | | .375 | | | .188 | | | .438 |
| 7.2 | | | | | | | .200 | | | .800 |
| 7.7 | | | | | | | .500 | | | .500 |
| Totals | .029 | | .019 | .576 | .006 | .036 | .126 | | | .207 |
| **Group 2 Probabilities** | | | | | | | | | | |
| 2.7 | | | | 1.000 | | | | | | |
| 3.2 | | | | .889 | .111 | | | | | |
| 3.7 | .048 | | | .667 | | | .095 | .095 | | .095 |
| 4.2 | | | | .650 | .025 | .025 | .150 | .025 | | .125 |
| 4.7 | | | .014 | .800 | | .057 | .071 | | | .057 |
| 5.2 | .016 | .016 | | .619 | .032 | .032 | .143 | | | .143 |
| 5.7 | | | | .625 | | .075 | .225 | | | .075 |
| 6.2 | | | | .483 | | | .241 | | | .276 |
| 6.7 | | | | .100 | | .100 | .300 | .100 | | .400 |
| 7.2 | | | | .500 | | | .250 | | | .250 |
| 7.7 | | | | .333 | | | .333 | | | .333 |
| Totals | .007 | .003 | .003 | .645 | .014 | .038 | .148 | .014 | | .128 |
| **Group 3 Probabilities** | | | | | | | | | | |
| 2.7 | | | | .100 | | | | | | |
| 3.2 | .250 | | | .625 | .125 | | | | | |
| 3.7 | .063 | | | .813 | | | .063 | | | .063 |
| 4.2 | .029 | | .059 | .618 | .029 | .029 | .088 | .029 | | .118 |
| 4.7 | .021 | | | .646 | .021 | .042 | .187 | | | .083 |
| 5.2 | .019 | | | .556 | | .047 | .241 | | | .111 |
| 5.7 | | | | .543 | | .022 | .196 | | | .239 |
| 6.2 | | | | .588 | | .059 | .176 | | | .176 |
| 6.7 | | | | .429 | | .071 | .071 | | | .429 |
| 7.2 | | | | .200 | | .200 | | | | .600 |
| 7.7 | | | | | | | | | | 1.00 |
| Totals | .024 | | | .588 | .012 | .045 | .159 | .004 | | .159 |

## Mach-Altitude Blocks

| $N_z$ | .65 / 7 | .65 / 20 | .85 / 1 | .85 / 7 | .85 / 20 | .92 / 1 | .92 / 7 | .92 / 12 | .92 / 20 | 1.2 / 20 |
|---|---|---|---|---|---|---|---|---|---|---|
| **Group 4 Probabilities** | | | | | | | | | | |
| 2.7 | .250 | | | .500 | | .250 | | | | |
| 3.2 | | | .091 | .727 | | .091 | .091 | | | |
| 3.7 | .050 | | | .750 | .100 | | .050 | | | .050 |
| 4.2 | .024 | | .049 | .634 | .024 | | .220 | | | .049 |
| 4.7 | | | | .682 | .015 | .045 | .121 | | | .136 |
| 5.2 | .011 | | | .652 | | .043 | .163 | .043 | | .087 |
| 5.7 | | | | .580 | | .160 | .180 | | | .080 |
| 6.2 | | | | .545 | | .091 | .227 | | | .136 |
| 6.7 | | | | .211 | | .158 | .368 | | | .263 |
| 7.2 | | | | .333 | | | .167 | | | .500 |
| 7.7 | | | | | | | | | | 1.00 |
| Totals | .011 | | .088 | .607 | .011 | .068 | .172 | .011 | | .110 |
| **All Group Probabilities** | | | | | | | | | | |
| 2.7 | .222 | | | .667 | | .111 | | | | |
| 3.2 | .103 | | .026 | .769 | .051 | .026 | .026 | | | |
| 3.7 | .092 | | | .737 | .026 | | .053 | .026 | | .065 |
| 4.2 | .027 | | .033 | .633 | .027 | .013 | .153 | .013 | | .100 |
| 4.7 | .004 | | .004 | .694 | .012 | .048 | .127 | | | .111 |
| 5.2 | .011 | .004 | .007 | .620 | .007 | .039 | .161 | .014 | | .136 |
| 5.7 | | | .010 | .550 | | .089 | .194 | | | .157 |
| 6.2 | | | .009 | .526 | | .060 | .181 | | | .224 |
| 6.7 | | | | .289 | | .085 | .237 | .016 | | .373 |
| 7.2 | | | | .250 | | .050 | .150 | | | .550 |
| 7.7 | | | | .143 | | | .286 | | | .571 |
| Totals | .018 | .001 | .010 | .604 | .011 | .048 | .152 | .008 | | .149 |

Altitudes are in feet $\times 10^{-3}$

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## TABLE XV

### Predicted Damages, $(D_K)_i$, for Transfer Spar

### at Fuselage Station 442

#### Group 1, Configuration 3, Pull-up Probability Model

| $N_z$ | Gross Weight x $10^{-3}$ | | | | | |
|---|---|---|---|---|---|---|
| | 33 | 35 | 37 | 39 | 41 | 44 |
| 2.7 | 0.0 | 0.0356 | 0.0742 | 0.1626 | 0.1812 | 0.0933 |
| 3.2 | 0.0743 | 0.1402 | 0.2182 | 0.4317 | 0.5226 | 0.2105 |
| 3.7 | 0.2649 | 0.3871 | 0.6193 | 1.2670 | 1.8011 | 0.5908 |
| 4.2 | 0.7347 | 1.1932 | 1.9030 | 3.7938 | 5.7061 | 1.9214 |
| 4.7 | 1.9010 | 2.9068 | 4.8353 | 8.8939 | 10.4686 | 3.7459 |
| 5.2 | 4.3727 | 6.3983 | 8.0073 | 14.0436 | 23.8068 | 6.4495 |
| 5.7 | 8.8831 | 10.0655 | 15.9244 | 28.9518 | 37.3640 | 33.1591 |
| 6.2 | 15.2591 | 19.8803 | 30.4564 | 53.7918 | 89.7596 | 49.0379 |
| 6.7 | 25.1247 | 39.7110 | 52.7412 | 108.5148 | 173.6502 | 80.9299 |
| 7.2 | 54.2750 | 100.3309 | 157.4869 | 185.3413 | 290.3087 | 201.8780 |
| 7.7 | 75.7472 | 110.9637 | 150.9013 | 195.7983 | 205.3322 | 163.4993 |

#### Total Configuration 3 Pull-up Probability Model

| $N_z$ | Gross Weight x $10^{-3}$ | | | | | |
|---|---|---|---|---|---|---|
| | 33 | 35 | 37 | 39 | 41 | 44 |
| 2.7 | 0.0 | 0.0158 | 0.0497 | 0.1334 | 0.1770 | 0.0514 |
| 3.2 | 0.0705 | 0.1350 | 0.2176 | 0.4386 | 0.5637 | 0.1995 |
| 3.7 | 0.2733 | 0.4157 | 0.6724 | 1.4112 | 1.9946 | 0.6476 |
| 4.2 | 0.7303 | 1.1857 | 1.9082 | 3.8223 | 5.6889 | 1.9012 |
| 4.7 | 1.7570 | 2.6766 | 4.4594 | 8.3511 | 9.1097 | 3.0817 |
| 5.2 | 4.3895 | 5.7069 | 6.8679 | 12.2716 | 20.7205 | 4.8845 |
| 5.7 | 8.0823 | 8.8684 | 13.9157 | 25.8944 | 31.3149 | 32.6247 |
| 6.2 | 12.9191 | 15.1622 | 22.5681 | 41.3216 | 65.8760 | 40.9756 |
| 6.7 | 25.9428 | 36.9441 | 50.5491 | 101.5327 | 155.9376 | 70.4541 |
| 7.2 | 41.8744 | 73.8877 | 114.6699 | 133.5362 | 210.7528 | 147.4712 |
| 7.7 | 79.0918 | 118.7365 | 162.3092 | 214.5017 | 215.9111 | 185.0529 |

$$(D_K)_i = \sum_{j=1}^{n} P_{ij} (d_K)_{ij}$$

= predicted damage per occurrence at load factor
level i and aircraft gross weight K.

Numbers in the table are damage x $10^5$.

# TABLE XVI

Predicted Damages, $(D_K)_i$, for Top Cover Skin

at Fuselage Station 509

## Group 1, Configuration 3, Pull-up Probability Model

| $N_z$ | Gross Weight x $10^{-3}$ | | | | | |
|---|---|---|---|---|---|---|
| | 33 | 35 | 37 | 39 | 41 | 44 |
| 2.7 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 3.2 | 0.0090 | 0.0083 | 0.0090 | 0.0938 | 0.0052 | 0.0 |
| 3.7 | 0.1862 | 0.2304 | 0.2988 | 0.4697 | 0.2742 | 0.1174 |
| 4.2 | 0.5719 | 0.6742 | 0.8620 | 1.2674 | 0.9393 | 0.6176 |
| 4.7 | 1.2540 | 1.5281 | 1.8677 | 2.6329 | 1.9158 | 1.2332 |
| 5.2 | 2.5944 | 3.1411 | 3.4523 | 5.1769 | 4.2900 | 2.7303 |
| 5.7 | 4.2539 | 5.1286 | 5.7892 | 7.8724 | 6.9810 | 5.0255 |
| 6.2 | 9.1723 | 10.1891 | 13.1929 | 10.9450 | 5.0988 | 11.0083 |
| 6.7 | 17.8354 | 22.5190 | 26.4770 | 48.1508 | 41.1749 | 23.1038 |
| 7.2 | 47.0834 | 55.3134 | 70.7774 | 131.2717 | 120.4984 | 64.3467 |
| 7.7 | 52.3390 | 60.5907 | 124.6507 | 167.6208 | 144.0159 | 77.5987 |

## Total Configuration 3 Pull-up Probability Model

| $N_z$ | Gross Weight x $10^{-3}$ | | | | | |
|---|---|---|---|---|---|---|
| | 33 | 35 | 37 | 39 | 41 | 44 |
| 2.7 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 3.2 | 0.0086 | 0.0085 | 0.0112 | 0.0911 | 0.0053 | 0.0 |
| 3.7 | 0.1828 | 0.2323 | 0.3070 | 0.4919 | 0.3063 | 0.1353 |
| 4.2 | 0.5389 | 0.6385 | 0.8154 | 1.2049 | 0.8814 | 0.5753 |
| 4.7 | 1.0865 | 1.2933 | 1.5683 | 2.2009 | 1.5486 | 0.9661 |
| 5.2 | 2.1306 | 2.5156 | 2.7706 | 4.0983 | 3.4934 | 2.0776 |
| 5.7 | 3.5758 | 4.2853 | 4.8082 | 6.2907 | 5.7614 | 4.0377 |
| 6.2 | 7.2214 | 7.9838 | 10.2447 | 16.1498 | 5.3022 | 8.2150 |
| 6.7 | 16.2845 | 20.3791 | 24.1537 | 43.7488 | 36.9666 | 21.0706 |
| 7.2 | 34.5693 | 40.7783 | 52.2527 | 97.6245 | 90.2766 | 45.9856 |
| 7.7 | 55.1865 | 64.3317 | 134.5567 | 183.2314 | 161.8594 | 83.4041 |

$$(D_K)_i = \sum_{j=1}^{n} P_{ij}(d_K)_{ij}$$

= predicted damage per occurrence at load factor
level i and aircraft gross weight K.

Numbers in the table are damage x $10^5$.

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# TABLE XVII

## Damage Predicted for Pull-ups after Weapon Release
## by Group 1, Configuration 3 Probability Model

### Fuselage Station 509

| A/C | Predicted Damage | Actual Damage | No. Pull-ups | Predicted Damage / Actual Damage |
|-----|------------------|---------------|--------------|----------------------------------|
| 130 | .011101328 | .011054771 | 105 | 1.00 |
| 132 | .009941412 | .009308585 | 94 | 1.07 |
| 357 | .003434372 | .003770050 | 43 | 0.91 |
| 422 | .003933254 | .003051069 | 67 | 1.29 |
| 160 | .002678943 | .001265232 | 28 | 2.12 |
| 240 | .006356793 | .004634964 | 116 | 1.37 |
| 378 | .014935296 | .012418496 | 118 | 1.20 |
| 469 | .001513419 | .001518588 | 28 | 1.00 |
| 731 | .000926601 | .000637889 | 13 | 1.45 |
| 732 | .009410448 | .006262450 | 128 | 1.50 |
| 69 | .008092920 | .009463007 | 93 | 0.86 |
| 167 | .000638259 | .000722062 | 11 | 0.88 |
| 367 | .009620021 | .006353593 | 109 | 1.51 |
| 720 | - - - - - | - - - - - | 0 | -- |
| 762 | .000147953 | .000047762 | 3 | 3.10 |
| 68 | .011233754 | .005434180 | 112 | 2.07 |
| 205 | .007378656 | .007211458 | 112 | 1.02 |
| 352 | .001980458 | .002971337 | 9 | 0.67 |
| 424 | .000811469 | .001278468 | 9 | 0.63 |
| Total | .104135356 | .087403961 | 1198 | 1.19 |

## TABLE XVIII

Damage Predicted for Pull-ups after Weapon Release
by Group 1, Configuration 3 Probability Model

### Fuselage Station 442

| A/C | Predicted Damage | Actual Damage | No. Pull-ups | Predicted Damage / Actual Damage |
|-----|------------------|---------------|--------------|----------------------------------|
| 130 | .030695597 | .035629394 | 105 | 0.86 |
| 132 | .025075527 | .026087360 | 94 | 0.96 |
| 357 | .012272102 | .014136603 | 43 | 0.87 |
| 422 | .015274948 | .009666610 | 67 | 1.58 |
| 160 | .005837160 | .002654828 | 28 | 2.20 |
| 240 | .023035078 | .017132062 | 116 | 1.34 |
| 378 | .039599059 | .031232314 | 118 | 1.27 |
| 469 | .004423352 | .004588783 | 28 | 0.96 |
| 731 | .004000717 | .002803357 | 13 | 1.43 |
| 732 | .031093000 | .022037530 | 128 | 1.41 |
| 69 | .021704972 | .027515075 | 93 | 0.79 |
| 167 | .002250145 | .002914833 | 11 | 0.77 |
| 367 | .032601718 | .023243259 | 109 | 1.40 |
| 720 | - - - - - | - - - - - | 0 | -- |
| 762 | .000616525 | .000407993 | 3 | 1.51 |
| 68 | .032030401 | .015493040 | 112 | 2.07 |
| 205 | .023715802 | .024954671 | 112 | 0.95 |
| 352 | .002865961 | .003880182 | 9 | 0.74 |
| 424 | .002113829 | .003475942 | 9 | 0.61 |
| Total | .309205893 | .267853836 | 1198 | 1.15 |

## TABLE XIX

### Damage Predicted for Pull-ups after Weapon Release by Total Configuration 3 Probability Model

#### Fuselage Station 509

| A/C | Predicted Damage | Actual Damage | No. Pull-ups | Predicted Damage / Actual Damage |
|---|---|---|---|---|
| 130 | .010061774 | .011054771 | 105 | 0.91 |
| 132 | .007774021 | .009308585 | 94 | 0.84 |
| 357 | .002958563 | .003770050 | 43 | 0.78 |
| 422 | .003387564 | .003051069 | 67 | 1.11 |
| 160 | .002616828 | .001265232 | 28 | 2.07 |
| 240 | .005198587 | .004634964 | 116 | 1.12 |
| 378 | .012989552 | .012418496 | 118 | 1.05 |
| 469 | .001273420 | .001518588 | 28 | 0.84 |
| 731 | .000785918 | .000637889 | 13 | 1.23 |
| 732 | .007811945 | .006262450 | 128 | 1.25 |
| 69 | .006793217 | .009463007 | 93 | 0.72 |
| 167 | .000507983 | .000722062 | 11 | 0.70 |
| 367 | .007851088 | .006353593 | 109 | 1.24 |
| 720 | - - - - - | - - - - - | 0 | -- |
| 762 | .000119850 | .000047762 | 3 | 2.51 |
| 68 | .009084963 | .005434180 | 112 | 1.67 |
| 205 | .006308707 | .007211458 | 112 | 0.87 |
| 352 | .002073974 | .002971337 | 9 | 0.70 |
| 424 | .000704458 | .001278468 | 9 | 0.55 |
| Total | .088302412 | .087403961 | 1198 | 1.01 |

## TABLE XX

### Damage Predicted for Pull-ups after Weapon Release by Total Configuration 3 Probability Model

#### Fuselage Station 442

| A/C | Predicted Damage | Actual Damage | No. Pull-ups | Predicted Damage / Actual Damage |
|---|---|---|---|---|
| 130 | .026970951 | .035629394 | 105 | 0.76 |
| 132 | .020161120 | .026087360 | 94 | 0.77 |
| 357 | .010859514 | .014136603 | 43 | 0.77 |
| 422 | .013521032 | .009666610 | 67 | 1.40 |
| 160 | .005422644 | .002654828 | 28 | 2.04 |
| 240 | .019359242 | .017132062 | 116 | 1.13 |
| 378 | .033754140 | .031232314 | 118 | 1.08 |
| 469 | .003943526 | .004588783 | 28 | 0.86 |
| 731 | .003576185 | .002803357 | 13 | 1.28 |
| 732 | .026967903 | .022037530 | 128 | 1.22 |
| 69 | .018710929 | .027515075 | 93 | 0.68 |
| 167 | .001912396 | .002914833 | 11 | 0.66 |
| 367 | .027337999 | .023243259 | 109 | 1.18 |
| 720 | - - - - - | - - - - - | 0 | -- |
| 762 | .000549660 | .000407993 | 3 | 1.35 |
| 68 | .026369567 | .015493040 | 112 | 1.70 |
| 205 | .020481797 | .024954671 | 112 | 0.82 |
| 352 | .002906484 | .003880182 | 9 | 0.75 |
| 424 | .001916828 | .003475942 | 9 | 0.55 |
| Total | .264721917 | .267853836 | 1198 | 0.99 |

## TABLE XXI

### Comparison of Damage Prediction Techniques for Top Cover Skin at Fuselage Station 509 for F-105D

| A/C | Dam./Hr. * $\frac{}{\text{Actual Damage}}$ | Dam./Flt. ** $\frac{}{\text{Actual Damage}}$ | Dam./Pull-up † $\frac{}{\text{Actual Damage}}$ | M-A Predicted Dam. †† $\frac{}{\text{Actual Damage}}$ |
|---|---|---|---|---|
| 130 | .79 | .77 | .69 | .91 |
| 160 | 1.13 | 1.17 | 1.61 | 2.07 |
| 240 | 2.50 | 2.20 | 1.82 | 1.12 |
| 357 | 1.10 | .97 | .83 | .78 |
| 367 | 1.64 | 1.45 | 1.25 | 1.24 |
| 720 | 4.39 | 1.32 | -- | -- |
| 731 | 2.01 | 2.13 | 1.49 | 1.23 |
| 732 | 1.52 | 1.31 | 1.49 | 1.25 |
| 762 | 4.51 | 5.23 | 4.58 | 2.51 |
| Base 1 | 1.41 | 1.28 | 1.17 | 1.10 |
| 68 | 1.03 | 1.02 | 1.50 | 1.67 |
| 69 | .64 | .69 | .72 | .72 |
| 132 | .49 | .61 | .74 | .84 |
| 167 | 1.29 | 1.72 | 1.11 | .70 |
| 205 | 1.26 | 1.31 | 1.13 | .87 |
| 352 | .18 | .22 | .22 | .70 |
| 378 | .56 | .60 | .69 | 1.05 |
| 422 | 1.50 | 1.64 | 1.60 | 1.11 |
| 424 | .72 | .87 | .51 | .55 |
| 469 | 2.07 | 2.31 | 1.35 | .84 |
| Base 2 | .77 | .83 | .89 | .95 |
| Total | 1.00 | 1.00 | 1.00 | 1.01 |

*Damage/Hour = $(\frac{\text{total damage for data sample}}{\text{total hours of data}})(\text{hours per aircraft})$

**Damage/Flight = $(\frac{\text{total damage for data sample}}{\text{total number of flights}})(\text{flights per aircraft})$

†Damage/Pullup = $(\frac{\text{total damage for all Configuration 3 pull-ups after weapon release}}{\text{total number of Configuration 3 pull-up after weapon release}})$
(Configuration 3 pull-ups per aircraft)

††M-A Predicted Damage = Configuration 3 pull-up damage predicted using Mach-altitude model based on total of all Configuration 3 pull-ups

Actual Damage = Damage calculated using measured Mach, altitude, gross weight, configuration and load factor

= Total damage for per hour and per flight calculations

= Damage due to Configuration 3 pull-ups for per pull-up and Mach-altitude probability calculations

## TABLE XXII

### Comparison of Damage Prediction Techniques for Transfer Spar at Fuselage Station 442 for F-105D

| A/C | Dam./Hr. [*] $\frac{\text{Actual Damage}}{}$ | Dam./Flt. [**] $\frac{\text{Actual Damage}}{}$ | Dam./Pull-up [†] $\frac{\text{Actual Damage}}{}$ | M-A Predicted Dam. [††] $\frac{\text{Acutal Damage}}{}$ |
|---|---|---|---|---|
| 130 | .64 | .62 | .66 | .76 |
| 160 | 1.77 | 1.83 | 2.36 | 2.05 |
| 240 | 1.76 | 1.55 | 1.51 | 1.13 |
| 357 | .76 | .67 | ..68 | .77 |
| 367 | 1.27 | 1.13 | 1.05 | 1.18 |
| 720 | 2.66 | 8.01 | -- | -- |
| 731 | 1.20 | 1.28 | 1.04 | 1.28 |
| 732 | 1.33 | 1.15 | 1.30 | 1.22 |
| 762 | 1.70 | 1.97 | 1.64 | 1.35 |
| Base 1 | 1.14 | 1.04 | 1.03 | 1.03 |
| 68 | 1.27 | 1.26 | 1.62 | 1.70 |
| 69 | .68 | .74 | .76 | .68 |
| 132 | .57 | .70 | .81 | .77 |
| 167 | 1.10 | 1.47 | .84 | .66 |
| 205 | 1.15 | 1.20 | 1.00 | .82 |
| 352 | .32 | .40 | .52 | .75 |
| 378 | .80 | .85 | .84 | 1.08 |
| 422 | 1.27 | 1.39 | 1.55 | 1.40 |
| 424 | .72 | .86 | .58 | .55 |
| 469 | 1.68 | 1.88 | 1.36 | .86 |
| Base 2 | .88 | .96 | .97 | .96 |
| Total | 1.00 | 1.00 | 1.00 | .99 |

[*]Damage/Hour = $(\frac{\text{total damage for data sample}}{\text{total hours of data}})$(hours per aircraft)

[**]Damage/Flight = $(\frac{\text{total damage for data sample}}{\text{total number of flights}})$(flights per aircraft)

[†]Damage/Pull-up = $(\frac{\text{total damage for all Configuration 3 pull-ups after weapon release}}{\text{total number of Configuration 3 pull-ups after weapon release}})$

(Configuration 3 pull-ups per aircraft)

[††]M-A Predicted Damage = Configuration 3 pull-up damage predicted using Mach-altitude model based on total of all Configuration 3 pull-ups

Actual Damage = Damage calculated using measured Mach, altitude, gross weight, configuration and load factor data

= Total Damage for per hour and per flight calculations

= Damage due to Configuration 3 pull-ups for per pull-up and Mach-altitude probability calculations

## TABLE XXIII

### Predicted Damage per Flight Hour, F-105D
### SEA Total Data Sample at Fuselage Station 509

| A/C | Flight Time | Total Damage | $\dfrac{\text{A/C Damage}}{\text{A/C Time}}$ | Predicted Damage | $\dfrac{\text{Predicted Damage}}{\text{Actual Damage}}$ |
|---|---|---|---|---|---|
| 130 | 247.13 | .015278101 | .000061822 | .01213398 | .79 |
| 160 | 107.44 | .004659453 | .000043368 | .00527526 | 1.13 |
| 240 | 355.54 | .006988923 | .000019657 | .01745687 | 2.50 |
| 357 | 99.55 | .004445144 | .000044652 | .00488787 | 1.10 |
| 367 | 388.49 | .011664952 | .000030026 | .01907410 | 1.64 |
| 720 | .77 | .000008603 | .000011173 | .00003781 | 4.39 |
| 731 | 30.57 | .000747140 | .000024440 | .00150097 | 2.01 |
| 732 | 322.03 | .010399045 | .000032292 | .01581154 | 1.52 |
| 762 | 6.0 | .000065250 | .000010875 | .00029460 | 4.51 |
| Subtotal Base 1 | 1557.52 | .054256611 | .000034835 | .07647361 | 1.41 |
| 68 | 257.61 | .012234097 | .000047491 | .01264855 | 1.03 |
| 69 | 194.31 | .014901917 | .000076692 | .00954054 | .64 |
| 132 | 199.48 | .019832024 | .000099419 | .00979439 | .49 |
| 167 | 29.46 | .001124345 | .000038165 | .00144647 | 1.29 |
| 205 | 289.30 | .011256924 | .000038911 | .01420451 | 1.26 |
| 352 | 11.19 | .003049556 | .000272525 | .00054942 | .18 |
| 378 | 298.45 | .026078523 | .000087380 | .01465378 | .56 |
| 422 | 120.50 | .003956915 | .000032838 | .00591650 | 1.50 |
| 424 | 23.04 | .001562494 | .000067817 | .00113125 | .72 |
| 469 | 74.64 | .001770466 | .000023720 | .00366479 | 2.07 |
| Subtotal Base 2 | 1497.98 | .095767261 | .000063931 | .07355022 | .77 |
| Total | 3055.50 | .15002342 | .000049100 | .15002387 | 1.00 |

$$\text{Predicted Damage} = \left(\frac{\text{Total Damage}}{\text{Total Flight Hours}}\right)(\text{Flight Hours})$$

$$\text{Average Damage Rate} = \left(\frac{\text{Total Damage}}{\text{Total Flight Hours}}\right) = .000049$$

## TABLE XXIV

### Predicted Damage per Flight Hour, F-105D
### SEA Total Data Sample at Fuselage Station 442

| A/C | Flight Time | Total Damage | A/C Damage / A/C Time | Predicted Damage | Predicted Damage / Actual Damage |
|-----|-------------|--------------|------------------------|------------------|----------------------------------|
| 130 | 247.13 | .047428746 | .000191918 | .03026008 | .64 |
| 160 | 107.44 | .007439759 | .000069246 | .01315560 | 1.77 |
| 240 | 355.54 | .024781628 | .000069701 | .04353445 | 1.76 |
| 357 | 99.55 | .016083536 | .000161562 | .01218950 | .76 |
| 367 | 388.49 | .037553443 | .000096665 | .04756905 | 1.27 |
| 720 | .77 | .000035452 | .000046042 | .00009428 | 2.66 |
| 731 | 30.57 | .003109795 | .000101727 | .00374317 | 1.20 |
| 732 | 322.03 | .029707155 | .000092249 | .03943129 | 1.33 |
| 762 | 6.00 | .000432727 | .000072121 | .00073468 | 1.70 |
| Subtotal Base 1 | 1557.52 | .166572241 | .000106947 | .19071209 | 1.14 |
| 68 | 257.61 | .024784498 | .000096209 | .03154331 | 1.27 |
| 69 | 194.31 | .034962451 | .000179931 | .02379248 | .68 |
| 132 | 199.48 | .042766157 | .000214388 | .02442553 | .57 |
| 167 | 29.46 | .003280375 | .000111350 | .00360726 | 1.10 |
| 205 | 289.30 | .030711699 | .000106159 | .03542363 | 1.15 |
| 352 | 11.19 | .004222222 | .000377321 | .00137017 | .32 |
| 378 | 298.45 | .045803087 | .000153470 | .03654401 | .80 |
| 422 | 120.50 | .011662172 | .000096782 | .01475474 | 1.27 |
| 424 | 23.04 | .003943014 | .000171138 | .00282116 | .72 |
| 469 | 74.64 | .005425439 | .000072688 | .00913937 | 1.68 |
| Subtotal Base 2 | 1497.98 | .207561114 | .000138561 | .18342166 | .88 |
| Total | 3055.50 | .374133355 | .000122446 | .37413375 | 1.00 |

$$\text{Predicted Damage} = \left(\frac{\text{Total Damage}}{\text{Total Flight Hours}}\right)(\text{Flight Hours})$$

$$\text{Average Damage Rate} = \left(\frac{\text{Total Damage}}{\text{Total Flight Hours}}\right) = .000122$$

## TABLE XXV

Predicted Damage per Flight, F-105D
SEA Total Data Sample at Fuselage Station 509

| A/C | Number Flights | Total Damage | Predicted Damage | Predicted Damage / Actual Damage |
|---|---|---|---|---|
| 130 | 103 | .015278101 | .011724181 | .77 |
| 160 | 48 | .004659453 | .005463696 | 1.17 |
| 240 | 135 | .006988923 | .015366645 | 2.20 |
| 357 | 38 | .004445144 | .004325426 | .97 |
| 367 | 149 | .011664952 | .016960223 | 1.45 |
| 720 | 1 | .000008603 | .000113827 | 13.23 |
| 731 | 14 | .000747140 | .001593578 | 2.13 |
| 732 | 120 | .010399045 | .013659240 | 1.31 |
| 762 | 3 | .000065250 | .000341481 | 5.23 |
| Subtotal Base 1 | 611 | .054256611 | .069548297 | 1.28 |
| 68 | 110 | .012234097 | .012520970 | 1.02 |
| 69 | 91 | .014901917 | .010358257 | .70 |
| 132 | 106 | .019832024 | .012065662 | .61 |
| 167 | 17 | .001124345 | .001935059 | 1.72 |
| 205 | 130 | .011256924 | .014797510 | 1.31 |
| 352 | 6 | .003049556 | .000682962 | .22 |
| 378 | 137 | .026078523 | .015594299 | .60 |
| 422 | 57 | .003956915 | .006488139 | 1.64 |
| 424 | 12 | .001562494 | .001365924 | .87 |
| 469 | 30 | .001770466 | .004097772 | 2.31 |
| Subtotal Base 2 | 702 | .095767261 | .079906554 | .83 |
| Total | 1313 | .150023872 | .150023872 | 1.00 |

$$\text{Predicted Damage} = \left( \frac{\text{Total Damage}}{\text{Total Number of Flights}} \right) (\text{No. of Flights})$$

$$\text{Average Damage Rate} = \left( \frac{\text{Total Damage}}{\text{Total Number of Flights}} \right) = .000114$$

## TABLE XXVI

### Predicted Damage per Flight, F-105D
### SEA Total Data Sample at Fuselage Station 442

| A/C | Number Flights | Damage | Predicted Damage | Predicted Damage / Actual Damage |
|-----|----------------|--------|------------------|----------------------------------|
| 130 | 103 | .047428746 | .029237992 | .62 |
| 160 | 48 | .007439759 | .013625472 | 1.83 |
| 240 | 135 | .024781628 | .038321640 | 1.55 |
| 357 | 38 | .016083536 | .010786822 | .67 |
| 367 | 149 | .037553443 | .042295736 | 1.13 |
| 720 | 1 | .000035452 | .000283864 | 8.00 |
| 731 | 14 | .003109795 | .003974096 | 1.28 |
| 732 | 120 | .029707155 | .034063680 | 1.15 |
| 762 | 3 | .000432727 | .000851592 | 1.97 |
| Subtotal Base 1 | 611 | .166572241 | .173440904 | 1.04 |
| 68 | 110 | .024784498 | .031225040 | 1.26 |
| 69 | 91 | .034962451 | .025831624 | .74 |
| 132 | 106 | .042766157 | .030089584 | .70 |
| 167 | 17 | .003280375 | .004825688 | 1.47 |
| 205 | 130 | .030711699 | .036902320 | 1.20 |
| 352 | 6 | .004222222 | .001703184 | .40 |
| 378 | 137 | .045803087 | .038889368 | .85 |
| 422 | 57 | .011662172 | .016180248 | 1.39 |
| 424 | 12 | .003943014 | .003406368 | .86 |
| 469 | 36 | .005425439 | .010219104 | 1.88 |
| Subtotal Base 2 | 702 | .207561114 | .149272528 | .96 |
| Total | 1313 | .374133355 | .374133355 | 1.00 |

$$\text{Predicted Damage} = \left(\frac{\text{Total Damage}}{\text{Total Number of Flights}}\right)(\text{No. of Flights})$$

$$\text{Average Damage Rate} = \left(\frac{\text{Total Damage}}{\text{Total Number of Flights}}\right) = .000285$$

## TABLE XXVII

### Predicted Damage per Pull-up after Weapon Release, F-105D, Configuration 3, SEA Data Sample at Fuselage Station 509

| A/C | Number Pull-ups | Damage due to Pull-ups | Predicted Damage | Predicted Damage / Actual Damage |
|-----|-----------------|------------------------|------------------|----------------------------------|
| 130 | 105 | .011054771 | .007660590 | .69 |
| 160 | 28 | .001265232 | .002042824 | 1.61 |
| 240 | 116 | .004634964 | .008463128 | 1.83 |
| 357 | 43 | .003770050 | .003137194 | .83 |
| 367 | 109 | .006353593 | .007952422 | 1.25 |
| 720 | 0 | | | |
| 731 | 13 | .000637889 | .000948454 | 1.49 |
| 732 | 128 | .006262450 | .009338624 | 1.49 |
| 762 | 3 | .000047762 | .000218874 | 4.58 |
| Base 1 | 545 | .034026711 | .039762110 | 1.17 |
| 68 | 112 | .005434180 | .008171296 | 1.50 |
| 69 | 93 | .009463007 | .006785094 | .72 |
| 132 | 94 | .009308585 | .006858052 | .74 |
| 167 | 11 | .000722062 | .000802538 | 1.11 |
| 205 | 112 | .007211458 | .008171296 | 1.13 |
| 352 | 9 | .002971337 | .000656622 | .22 |
| 378 | 118 | .012418496 | .008609044 | .69 |
| 422 | 67 | .003051069 | .004888186 | 1.60 |
| 424 | 9 | .001278468 | .000656622 | .51 |
| 469 | 28 | .001518588 | .002042824 | 1.35 |
| Base 2 | 653 | .053377250 | .047641574 | .89 |
| Total | 1198 | .087403961 | .087403961 | 1.00 |

$$\text{Predicted Damage} = \left( \frac{\text{Total Damage}}{\text{Total Number Pull-ups}} \right)^* (\text{No. Pull-ups})$$

$$\text{Average Damage Rate} = \left( \frac{\text{Total Damage}}{\text{Total Number Pull-ups}} \right)^* = .000073$$

\* Configuration 3 Data

## TABLE XXVIII

### Predicted Damage per Pull-up After Weapon Release, F-105D, Configuration 3, SEA Data Sample at Fuselage Station 442

| A/C | Number Pull-ups | Damage due to Pull-ups | Predicted Damage | Predicted Damage / Actual Damage |
|---|---|---|---|---|
| 130 | 105 | .035629344 | .023476320 | .66 |
| 160 | 28 | .002654828 | .006260352 | 2.36 |
| 240 | 116 | .017132062 | .025935744 | 1.51 |
| 357 | 43 | .014136603 | .009614112 | .68 |
| 367 | 109 | .023243259 | .024370656 | 1.05 |
| 720 | 0 | | | |
| 731 | 13 | .002803357 | .002906592 | 1.04 |
| 732 | 128 | .022037530 | .028618752 | 1.30 |
| 762 | 3 | .000407993 | .000670752 | 1.64 |
| Base 1 | 545 | .118045026 | .121853280 | 1.03 |
| 68 | 112 | .015493040 | .025041408 | 1.62 |
| 69 | 93 | .027515075 | .020793312 | .76 |
| 132 | 94 | .026087360 | .021016896 | .81 |
| 167 | 11 | .002914833 | .002459424 | .84 |
| 205 | 112 | .024954671 | .025041408 | 1.00 |
| 352 | 9 | .003880182 | .002012256 | .52 |
| 378 | 118 | .031232314 | .026382912 | .84 |
| 422 | 67 | .009666610 | .014980128 | 1.55 |
| 424 | 9 | .003475942 | .002012256 | .58 |
| 469 | 28 | .004588783 | .006260352 | 1.36 |
| Base 2 | 653 | .149808810 | .146000352 | .97 |
| Total | 1198 | .267853836 | .267853836 | 1.00 |

$$\text{Predicted Damage} = \left(\frac{\text{Total Damage}}{\text{Total Number Pull-ups}}\right)^* (\text{No. of Pull-ups})$$

$$\text{Average Damage Rate} = \left(\frac{\text{Total Damage}}{\text{Total Number Pull-ups}}\right)^* = .000224$$

\* Configuration 3 Data

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TABLE XXIX

Variance Calculations for F-105D Truncated Data Sample

| A/C | Damage/Hr. Actual Damage | Damage/Flight Actual Damage | Damage/Pull-up Actual Damage | M-A Predicted Damage Actual Damage |
|---|---|---|---|---|
| | | **Fuselage Station 509** | | |
| 130 | .79 | .77 | .69 | .91 |
| 160 | 1.13 | 1.17 | 1.61 | 2.07 |
| 240 | 2.50 | 2.20 | 1.82 | 1.12 |
| 357 | 1.10 | .97 | .83 | .78 |
| 367 | 1.64 | 1.45 | 1.25 | 1.24 |
| 732 | 1.52 | 1.31 | 1.49 | 1.25 |
| 68 | 1.03 | 1.02 | 1.50 | 1.67 |
| 69 | .64 | .69 | .72 | .72 |
| 132 | .49 | .61 | .74 | .84 |
| 205 | 1.26 | 1.31 | 1.13 | .87 |
| 378 | .56 | .60 | .69 | 1.05 |
| 422 | 1.50 | 1.64 | 1.60 | 1.11 |
| 469 | 2.07 | 2.31 | 1.35 | .84 |
| S² = | .354 | .311 | .168 | .148 |
| | | **Fuselage Station 442** | | |
| 130 | .64 | .62 | .66 | .76 |
| 160 | 1.77 | 1.83 | 2.36 | 2.05 |
| 240 | 1.76 | 1.55 | 1.51 | 1.13 |
| 357 | .76 | .67 | .68 | .77 |
| 367 | 1.27 | 1.13 | 1.05 | 1.18 |
| 732 | 1.33 | 1.15 | 1.30 | 1.22 |
| 68 | 1.27 | 1.26 | 1.62 | 1.70 |
| 69 | .68 | .74 | .76 | .68 |
| 132 | .57 | .70 | .81 | .77 |
| 205 | 1.15 | 1.20 | 1.00 | .82 |
| 378 | .80 | .85 | .84 | 1.08 |
| 422 | 1.27 | 1.39 | 1.55 | 1.40 |
| 469 | 1.68 | 1.88 | 1.36 | .86 |
| S² = | .184 | .183 | .240 | .168 |

$$S^2 = \frac{n\Sigma(X_i)^2 - (\Sigma X_i)^2}{n(n-1)}$$

## TABLE XXX

### Variance Calculations for F-105D Damage Ratios
### Computed by Base

| A/C | Predicted Damage/Actual Damage | | |
|-----|----------------|-----------------|-------------------|
| | Damage/Hour | Damage/Flight | Damage/Pull-up |
| **Fuselage Station 509** | | | |
| 130 | .56 | .60 | .59 |
| 160 | .80 | .91 | 1.38 |
| 240 | 1.77 | 1.71 | 1.56 |
| 357 | .78 | .76 | .71 |
| 367 | 1.16 | 1.13 | 1.07 |
| 732 | 1.08 | 1.02 | 1.28 |
| 68 | 1.34 | 1.23 | 1.68 |
| 69 | .83 | .83 | .80 |
| 132 | .64 | .73 | .83 |
| 205 | 1.64 | 1.58 | 1.27 |
| 378 | .73 | .72 | .78 |
| 422 | 1.94 | 1.97 | 1.80 |
| 469 | 2.69 | 2.77 | 1.51 |
| $S^2 =$ | .394 | .393 | .163 |
| **Fuselage Station 442** | | | |
| 130 | .56 | .59 | .64 |
| 160 | 1.54 | 1.76 | 2.28 |
| 240 | 1.53 | 1.49 | 1.47 |
| 357 | .66 | .64 | .66 |
| 367 | 1.11 | 1.08 | 1.02 |
| 732 | 1.16 | 1.10 | 1.26 |
| 68 | 1.44 | 1.31 | 1.66 |
| 69 | .77 | .77 | .78 |
| 132 | .65 | .73 | .83 |
| 205 | 1.31 | 1.25 | 1.03 |
| 378 | .90 | .88 | .87 |
| 422 | 1.43 | 1.45 | 1.59 |
| 469 | 1.91 | 1.96 | 1.40 |
| $S^2 =$ | .176 | .187 | .228 |

$$S^2 = \frac{n\Sigma (X_i)^2 - (\Sigma X_i)^2}{n(n-1)}$$

## TABLE XXXI

### Damage Prediction Ratios for Mach-Altitude Probability Model
### Based on First 114 F-105D Configuration 3 Pull-ups

| A/C | Peaks 1-114 $\frac{\text{Predicted Damage}}{\text{Actual Damage}}$ | Peaks 1-228 $\frac{\text{Predicted Damage}}{\text{Actual Damage}}$ | Peaks 1-345 $\frac{\text{Predicted Damage}}{\text{Actual Damage}}$ | All Peaks $\frac{\text{Predicted Damage}}{\text{Actual Damage}}$ |
|---|---|---|---|---|
| | | Fuselage Station 509 | | |
| 130 | -- | .57 | .77 | .72 |
| 132 | 1.95 | 2.01 | 1.60 | .31 |
| 357 | -- | -- | -- | .65 |
| 422 | -- | -- | -- | .94 |
| 160 | 2.26 | 1.79 | 1.79 | 1.79 |
| 240 | -- | 1.87 | .81 | .73 |
| 378 | .94 | .98 | .84 | .70 |
| 469 | .66 | .65 | .65 | .65 |
| 731 | -- | -- | -- | 1.05 |
| 732 | 1.57 | 1.57 | 1.11 | .90 |
| 69 | .50 | .49 | .54 | .46 |
| 167 | -- | -- | -- | .48 |
| 367 | 1.03 | 1.20 | 1.20 | .79 |
| 720 | -- | -- | -- | -- |
| 762 | -- | -- | -- | 1.91 |
| 68 | -- | 1.91 | 2.03 | .94 |
| 205 | 1.50 | 1.77 | 1.67 | .71 |
| 352 | .60 | .60 | .60 | .60 |
| 424 | -- | -- | -- | .44 |
| Totals | .96 | .91 | .92 | .69 |
| Variance | .3939 N=9 | .3605 N=12 | .2695 N=12 | .1788 N=18 |
| | | Fuselage Station 442 | | |
| 130 | -- | .54 | .90 | .61 |
| 132 | 1.36 | 1.48 | 1.33 | .43 |
| 357 | -- | -- | -- | .68 |
| 422 | -- | -- | -- | 1.21 |
| 160 | 3.08 | 1.69 | 1.67 | 1.68 |
| 240 | .74 | 1.50 | .74 | .83 |
| 378 | .95 | 1.04 | 1.02 | .76 |
| 469 | .72 | .74 | .74 | .74 |
| 731 | -- | -- | -- | 1.15 |
| 732 | 1.97 | 1.57 | 1.24 | 1.00 |
| 69 | .65 | .56 | .60 | .49 |
| 167 | -- | -- | -- | .52 |
| 367 | 1.44 | 1.29 | 1.34 | .88 |
| 720 | -- | -- | -- | -- |
| 762 | -- | -- | -- | 1.22 |
| 68 | -- | 2.10 | 2.68 | 1.14 |
| 205 | 1.41 | 1.73 | 1.56 | .68 |
| 352 | .62 | .62 | .62 | .62 |
| 424 | -- | -- | -- | .48 |
| Totals | 1.07 | 1.03 | 1.03 | .75 |
| Variance | .5920 N=10 | .2718 N=12 | .3478 N=12 | .1113 N=18 |

## TABLE XXXII

### Damage Prediction Ratios for Mach-Altitude Probability Model
### Based on Last 114 F-105D Configuration 3 Pull-ups

| A/C | Peaks 1084-1198 Predicted Damage / Actual Damage | Peaks 971-1198 Predicted Damage / Actual Damage | Peaks 857-1198 Predicted Damage / Actual Damage | Peaks 1-1198 Predicted Damage / Actual Damage |
|---|---|---|---|---|
| | Fuselage Station 509 | | | |
| 130 | 2.57 | 1.70 | 1.70 | .60 |
| 132 | 1.05 | .27 | .45 | .55 |
| 357 | .82 | .95 | .95 | .95 |
| 422 | .53 | 1.23 | 1.11 | 1.29 |
| 160 | ---- | ---- | ---- | .79 |
| 240 | ---- | .89 | .89 | 1.02 |
| 378 | ---- | .80 | .77 | .71 |
| 469 | ---- | ---- | ---- | .94 |
| 731 | 1.46 | 1.46 | 1.46 | 1.46 |
| 732 | 3.24 | 1.26 | 1.31 | 1.29 |
| 69 | ---- | ---- | ---- | .60 |
| 167 | .69 | .74 | .74 | .74 |
| 367 | 1.94 | 1.42 | 1.60 | 1.17 |
| 720 | ---- | ---- | ---- | ---- |
| 762 | 2.69 | 2.69 | 2.69 | 2.69 |
| 68 | 1.01 | .89 | 1.03 | 1.40 |
| 205 | .88 | .95 | .85 | .99 |
| 352 | ---- | ---- | ---- | .08 |
| 424 | ---- | .68 | .68 | .68 |
| Totals | 1.05 | .87 | .86 | .85 |
| Variances | .8657 N=11 | .3354 N=14 | .3257 N=14 | .2999 N=18 |
| | Fuselage Station 442 | | | |
| 130 | 1.69 | 1.50 | 1.50 | .68 |
| 132 | .69 | .25 | .47 | .60 |
| 357 | .87 | .93 | .93 | .93 |
| 422 | .81 | 1.66 | 1.38 | 1.62 |
| 160 | ---- | ---- | ---- | 1.23 |
| 240 | ---- | .95 | 1.21 | 1.07 |
| 378 | ---- | 1.02 | .93 | .92 |
| 469 | ---- | ---- | ---- | .96 |
| 731 | 1.50 | 1.51 | 1.51 | 1.51 |
| 732 | 1.80 | .98 | 1.01 | 1.34 |
| 69 | ---- | ---- | ---- | .61 |
| 167 | .67 | .69 | .69 | .69 |
| 367 | 1.60 | 1.20 | 1.30 | 1.21 |
| 720 | ---- | ---- | ---- | ---- |
| 762 | 1.37 | 1.37 | 1.37 | 1.37 |
| 68 | .86 | 1.08 | 1.24 | 1.60 |
| 205 | .63 | .69 | .69 | .92 |
| 352 | ---- | ---- | ---- | .20 |
| 424 | ---- | .68 | .68 | .68 |
| Totals | .96 | .95 | .93 | .95 |
| Variances | .2076 N=11 | .1520 N=14 | .1161 N=14 | .1547 N=18 |

TABLE XXXIII

Comparison of Damage Ratios and Variance for
Four Mach-Altitude Probability Models

| A/C | Mach-Altitude Probability Models | | | |
| | Group I | Total | First 114 | Last 114 |
| --- | --- | --- | --- | --- |
| | Fuselage Station 509 | | | |
| 130 | 1.00 | .91 | .72 | .60 |
| 132 | 1.07 | .84 | .31 | .55 |
| 357 | .91 | .78 | .65 | .95 |
| 422 | 1.29 | 1.11 | .94 | 1.29 |
| 160 | 2.12 | 2.07 | 1.79 | .79 |
| 240 | 1.37 | 1.12 | .73 | 1.02 |
| 378 | 1.20 | 1.05 | .70 | .71 |
| 469 | 1.00 | .84 | .65 | .94 |
| 732 | 1.50 | 1.25 | .90 | 1.29 |
| 69 | .86 | .72 | .46 | .60 |
| 367 | 1.51 | 1.24 | .79 | 1.17 |
| 68 | 2.07 | 1.67 | .94 | 1.40 |
| 205 | 1.02 | .87 | .71 | .99 |
| Variance | .1684 | .1483 | .1215 | .0814 |
| | Fuselage Station 442 | | | |
| 130 | .86 | .76 | .61 | .68 |
| 132 | .96 | .77 | .43 | .60 |
| 357 | .87 | .77 | .68 | .93 |
| 422 | 1.58 | 1.40 | 1.21 | 1.62 |
| 160 | 2.20 | 2.04 | 1.68 | 1.23 |
| 240 | 1.34 | 1.13 | .83 | 1.07 |
| 378 | 1.27 | 1.08 | .76 | .92 |
| 469 | .96 | .86 | .74 | .96 |
| 732 | 1.41 | 1.22 | 1.00 | 1.34 |
| 69 | .79 | .68 | .49 | .61 |
| 367 | 1.40 | 1.18 | .88 | 1.21 |
| 68 | 2.07 | 1.70 | 1.14 | 1.60 |
| 205 | .95 | .82 | .68 | .92 |
| Variance | .2078 | .1667 | .1140 | .1133 |
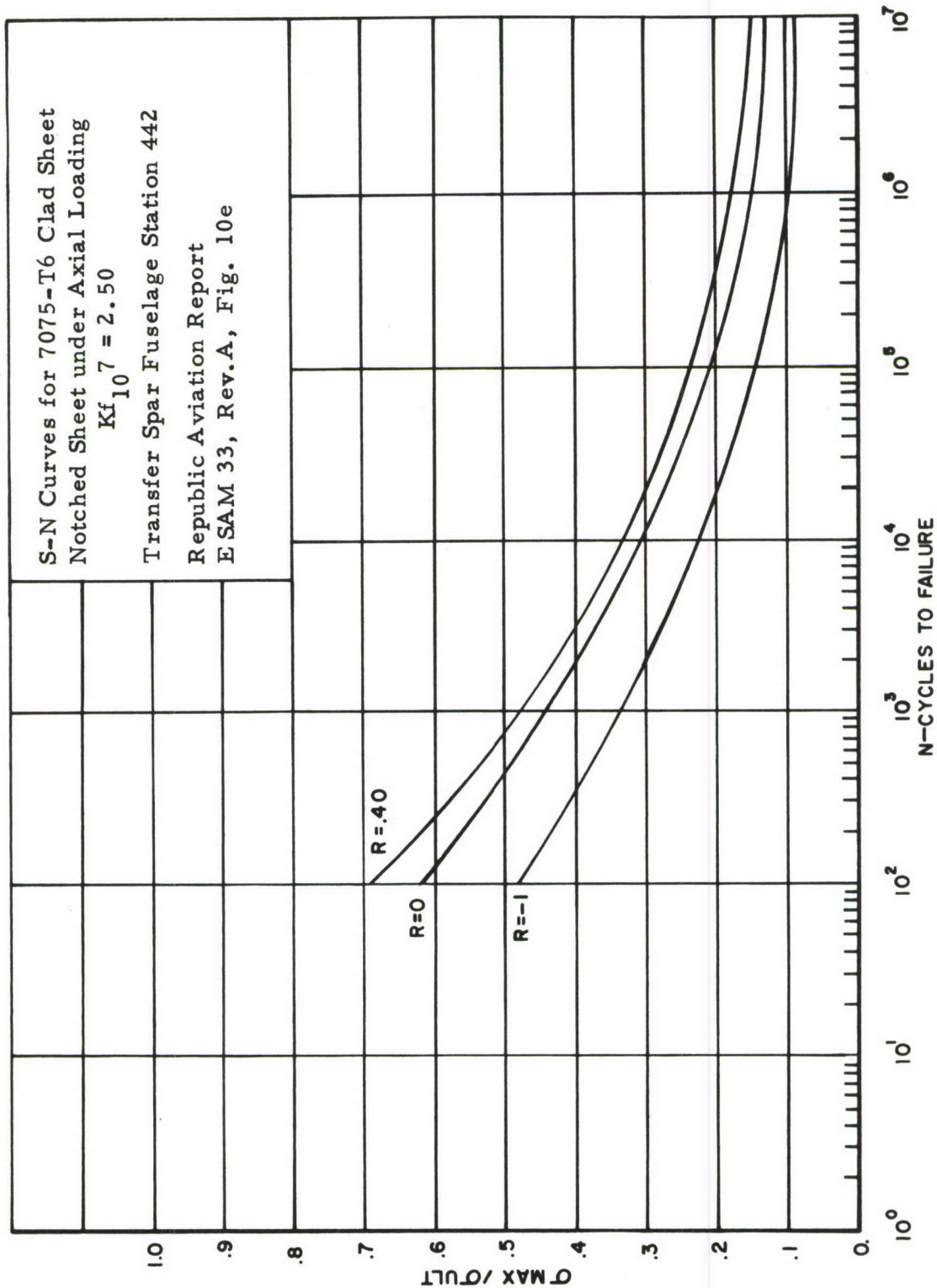
Figure 4   S-N Curves for 7075-T6 Clad Sheet Notched Sheet under Axial Loading
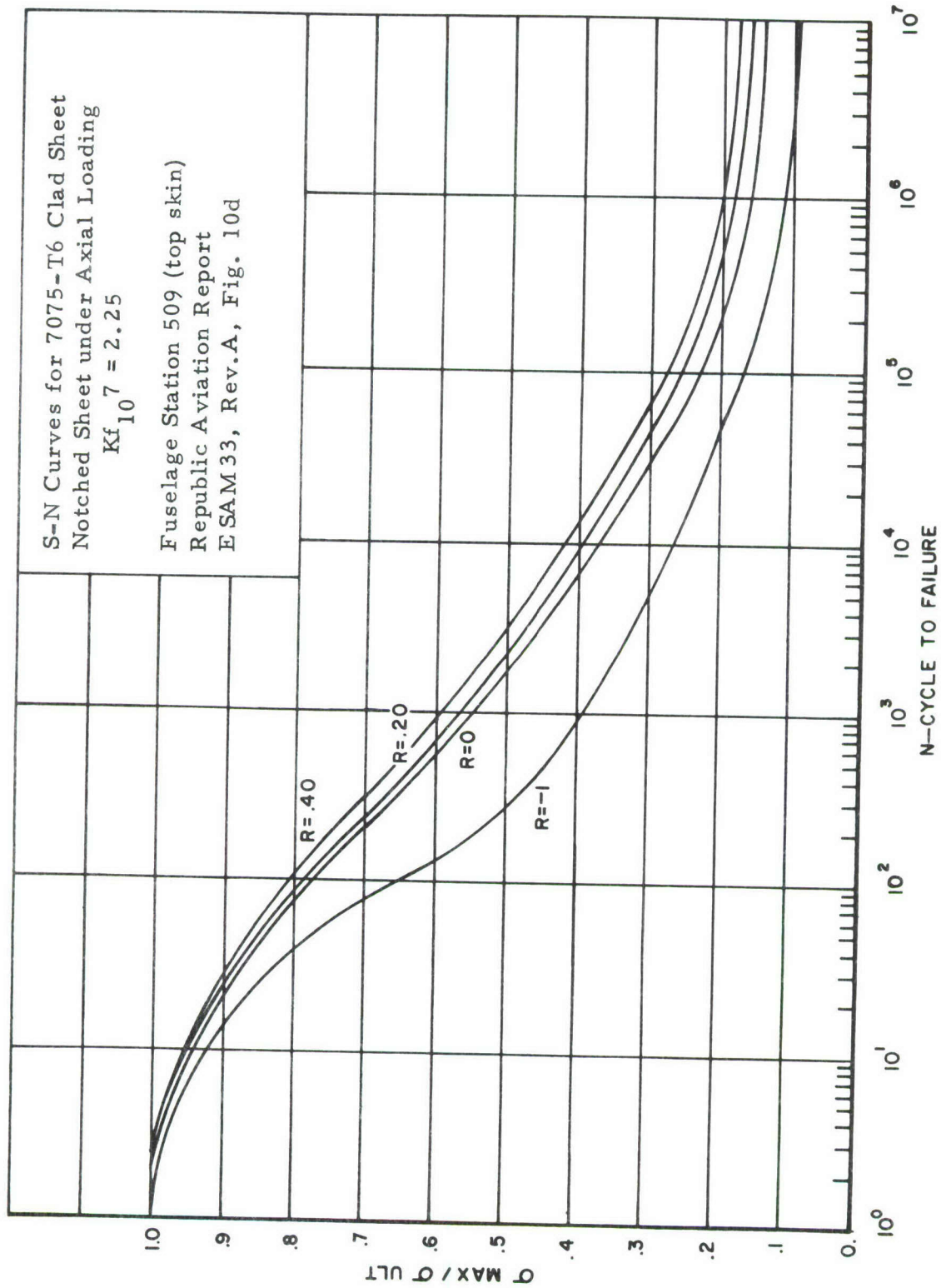$Kf_{10}{}^7 = 2.50$

Figure 5   S-N Curves for 7075-T6 Clad Sheet Notched Sheet under Axial Loading
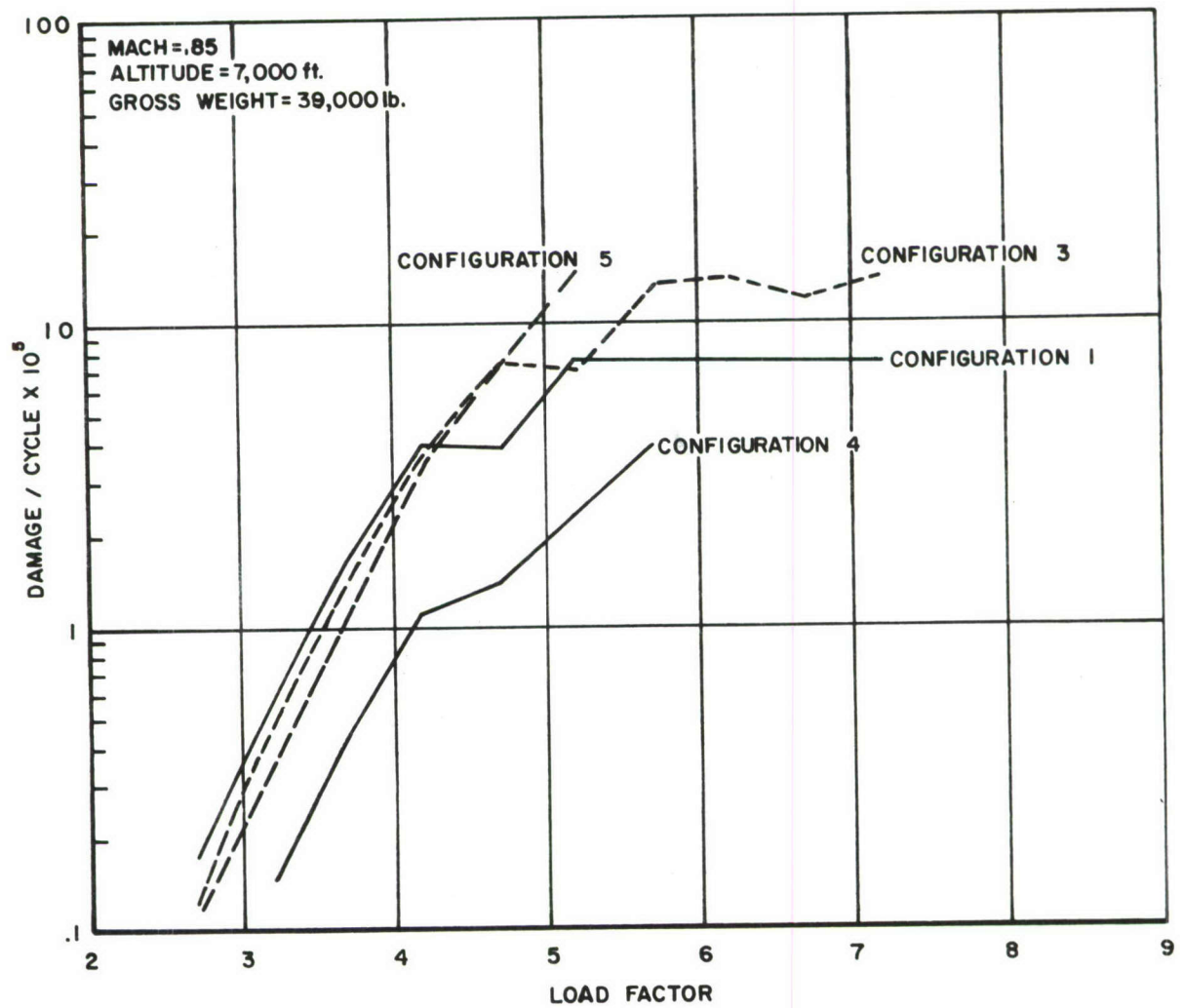$Kf_{10}{}^7 = 2.25$

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Figure 6   Damage per Cycle vs Load Factor by Configuration for the
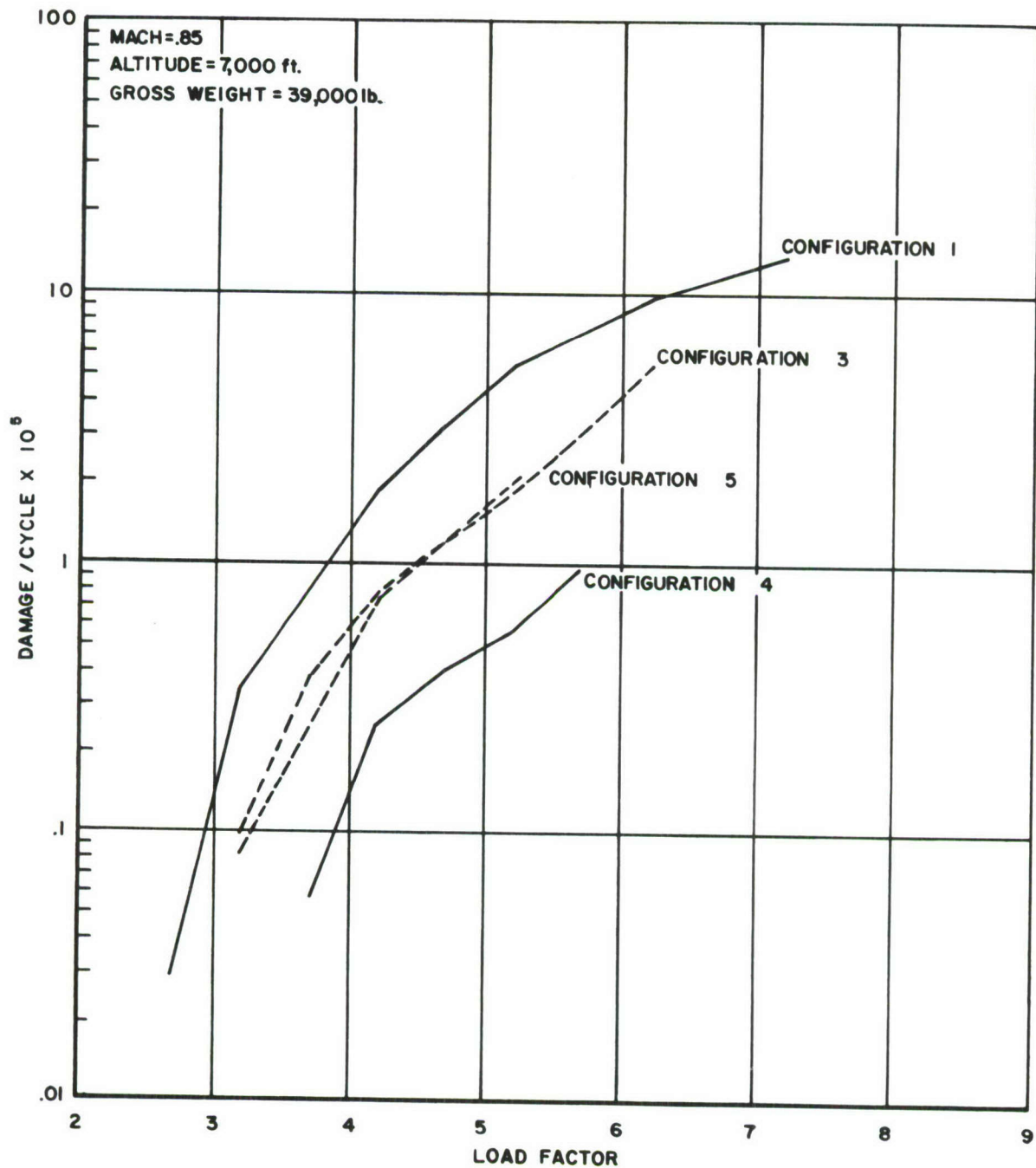F-105D Transfer Spar at Fuselage Station 442

Figure 7  Damage per Cycle vs Load Factor by Configuration for the
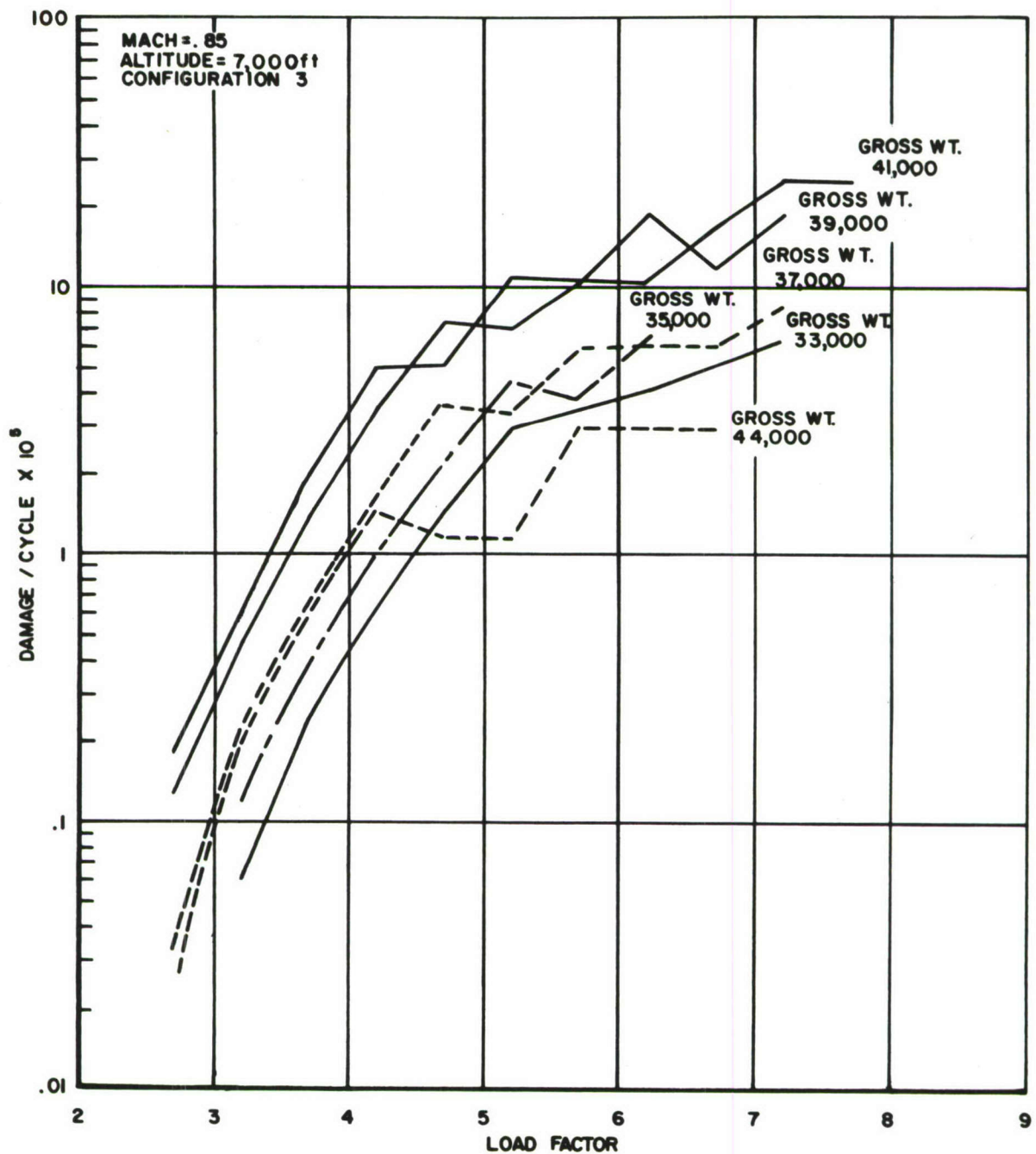F-105D Top Cover Skin at Fuselage Station 509

Figure 8    Damage per Cycle vs Load Factor by Gross Weight
for the F-105D Transfer Spar at Fuselage Station 442
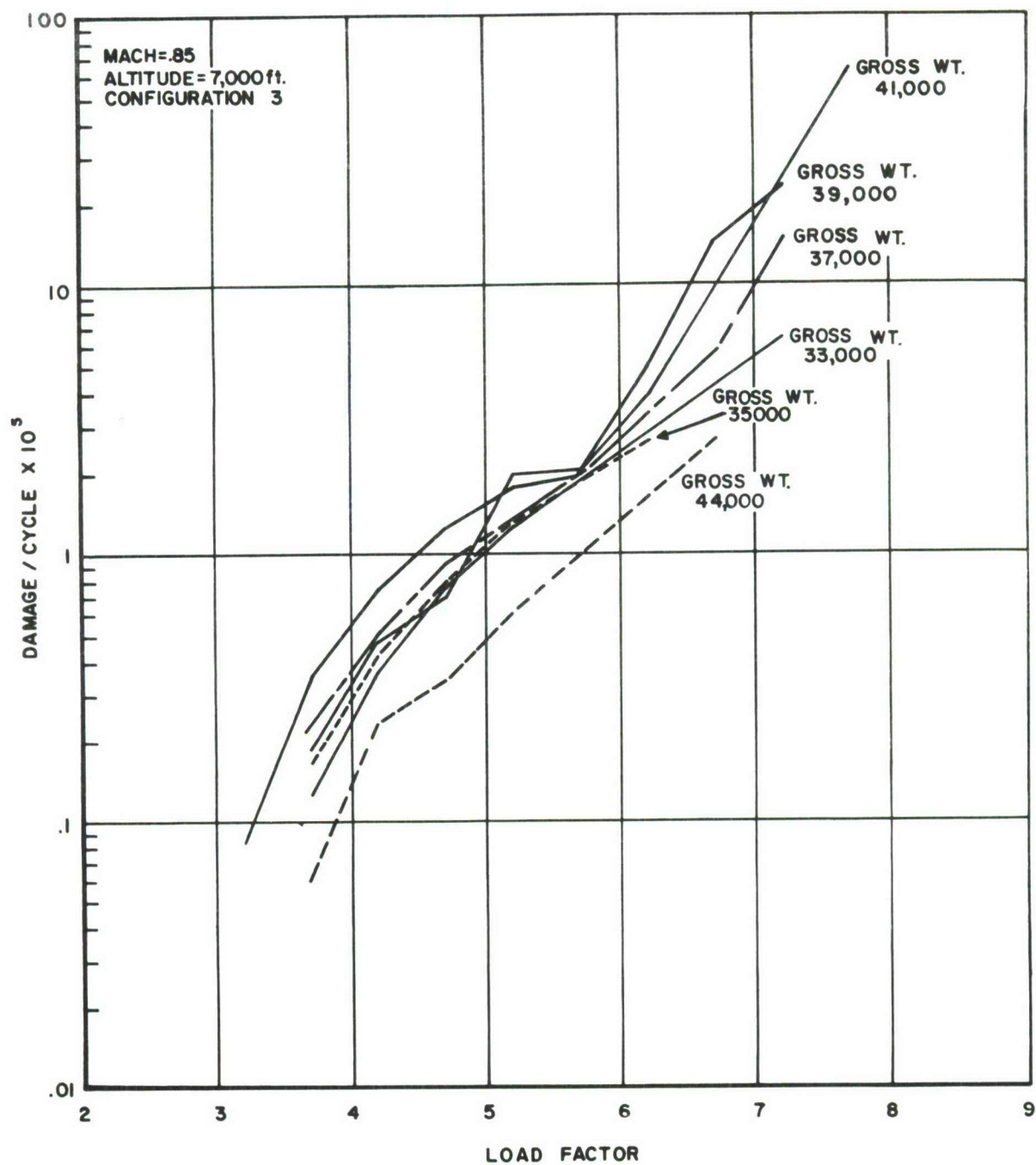
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Figure 9    Damage per Cycle vs Load Factor by Gross Weight for the
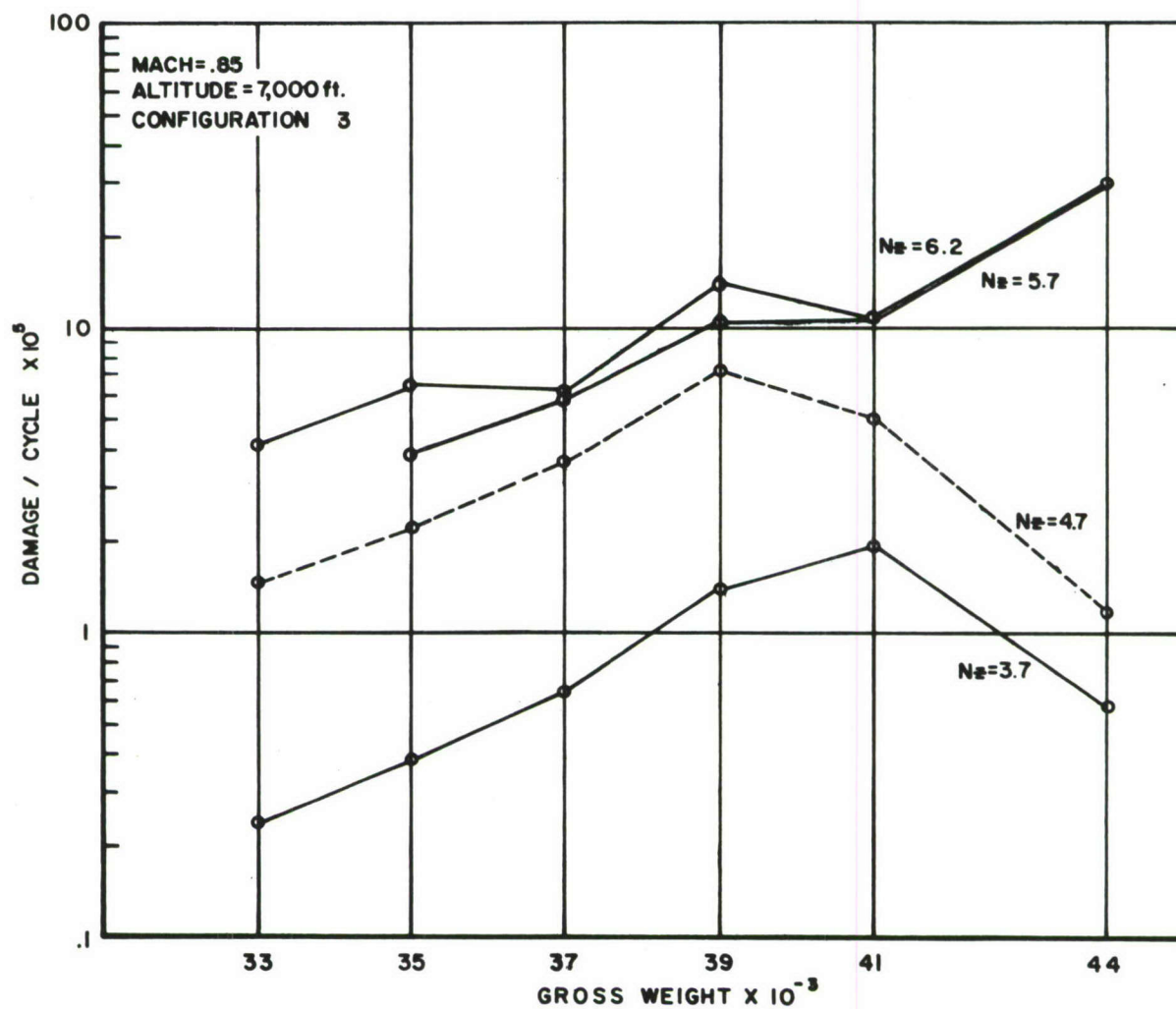F-105D Top Cover Skin at Fuselage Station 509

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Figure 10 Damage per Cycle vs Gross Weight by Load Factor for
the F-105D Transfer Spar at Fuselage Station 442
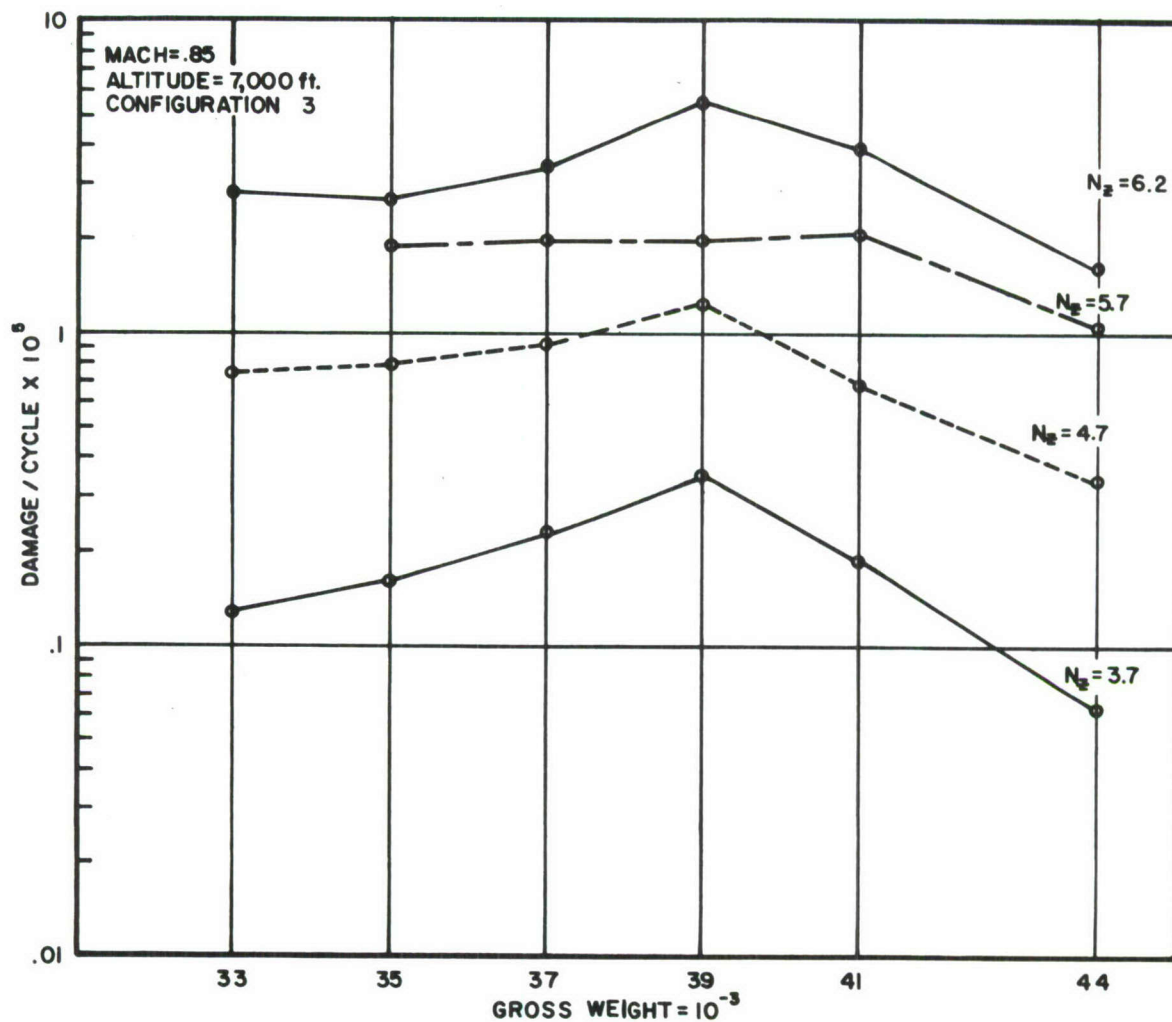
Figure 11    Damage per Cycle vs Gross Weight by Load Factor for the
Top Cover Skin at Fuselage Station 509
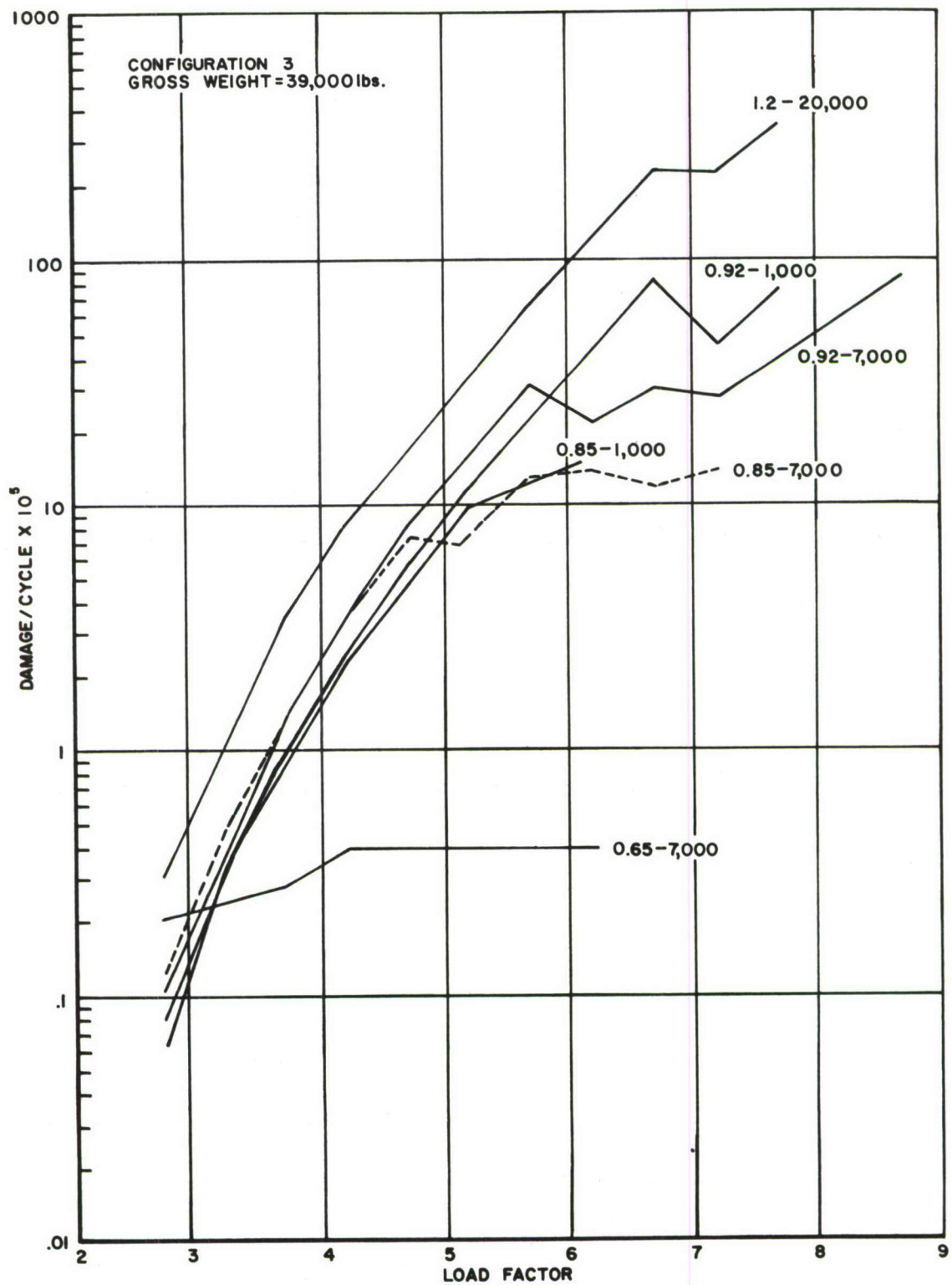
Figure 12    Damage per Cycle vs Load Factor by Mach-Altitude
Condition for the F-105D Transfer Spar at Fuselage
Station 442

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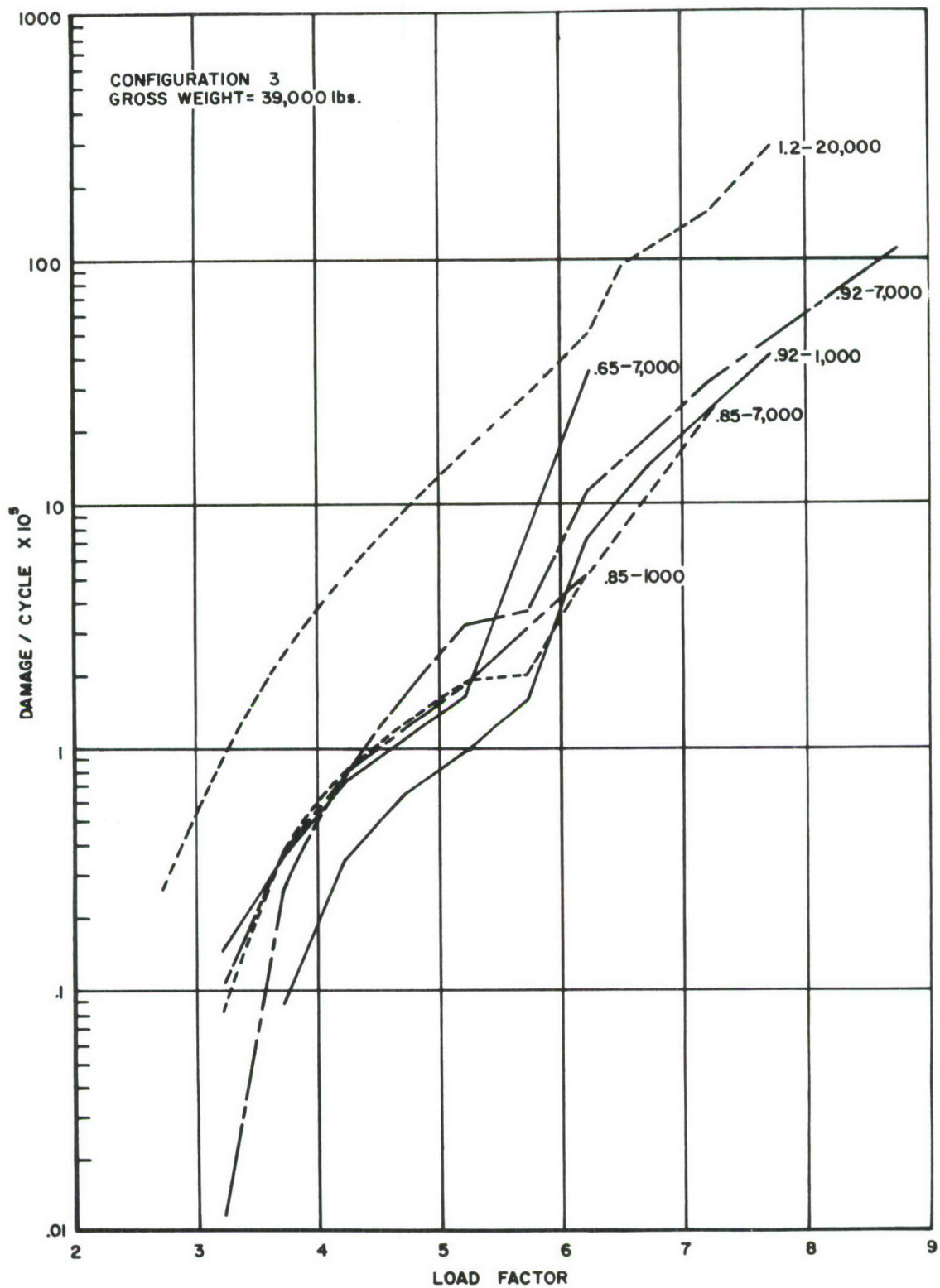
Figure 13    Damage per Cycle vs Load Factor by Mach-Altitude
Condition for the F-105D Top Cover Skin at Fuselage
Station 509

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Figure 14   Mach-Altitude Probability Plot for F-105D Pull-up After Weapon Release, Configuration 3, Group 1 Data

PROBABILITY

MACH NO.

ALTITUDE

M=.85
H=7,000
(.604)

M=.85
H=1,000
(.010)

M=.92
H=1,000
(.048)

M=.92
H=7,000
(.152)

M=1.2
H=20,000
(.149)

M=.92
H=12,000
(.008)

M=.92
H=20,000
(0)

M=.85
H=20,000
(.011)

M=.65
H=7,000
(.018)

M=.65
H=20,000
(.008)
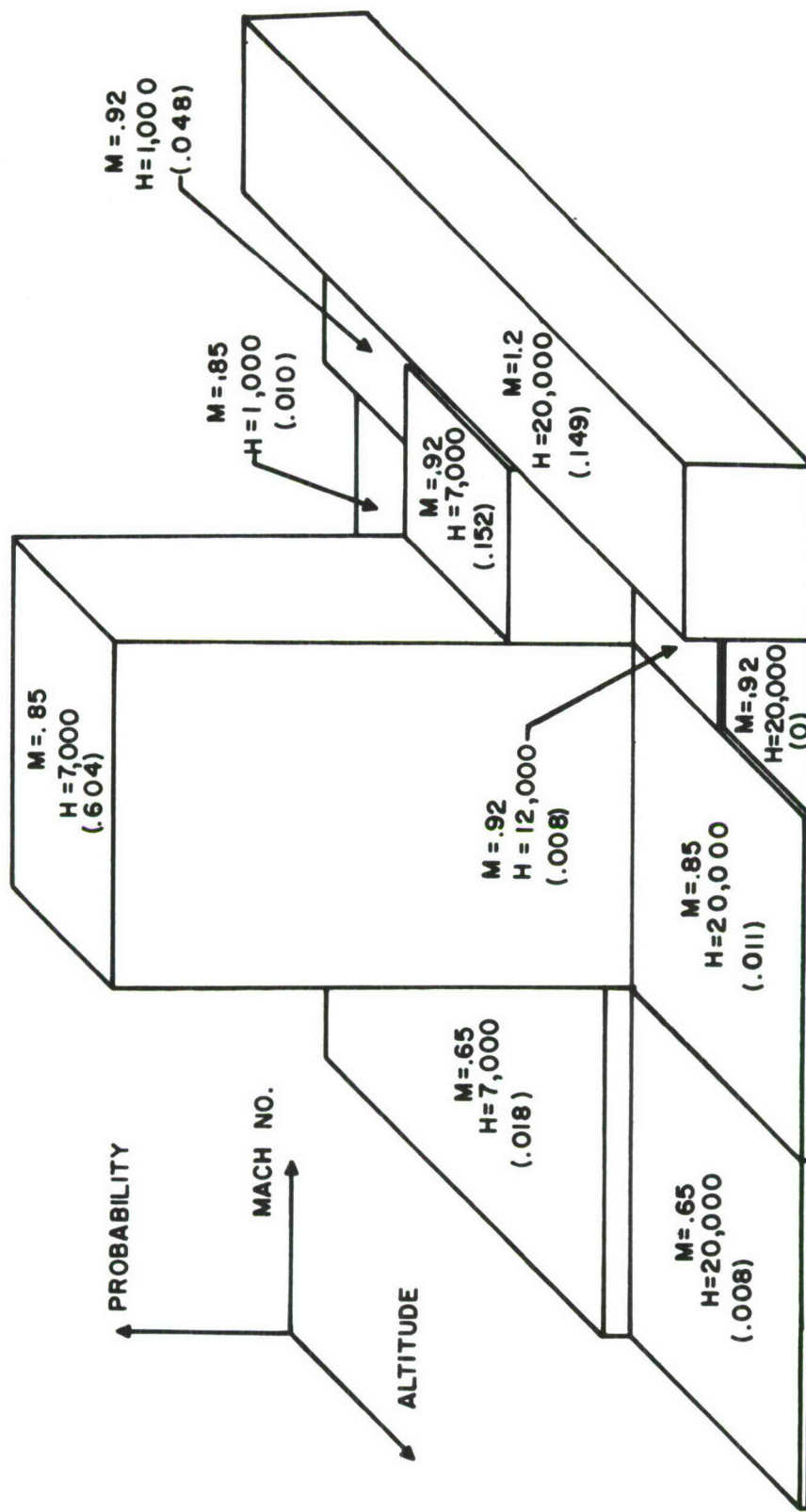
Figure 15 Mach-Altitude Probability Plot for F-105D Pull-up after Weapon Release, Configuration 3 Data

66
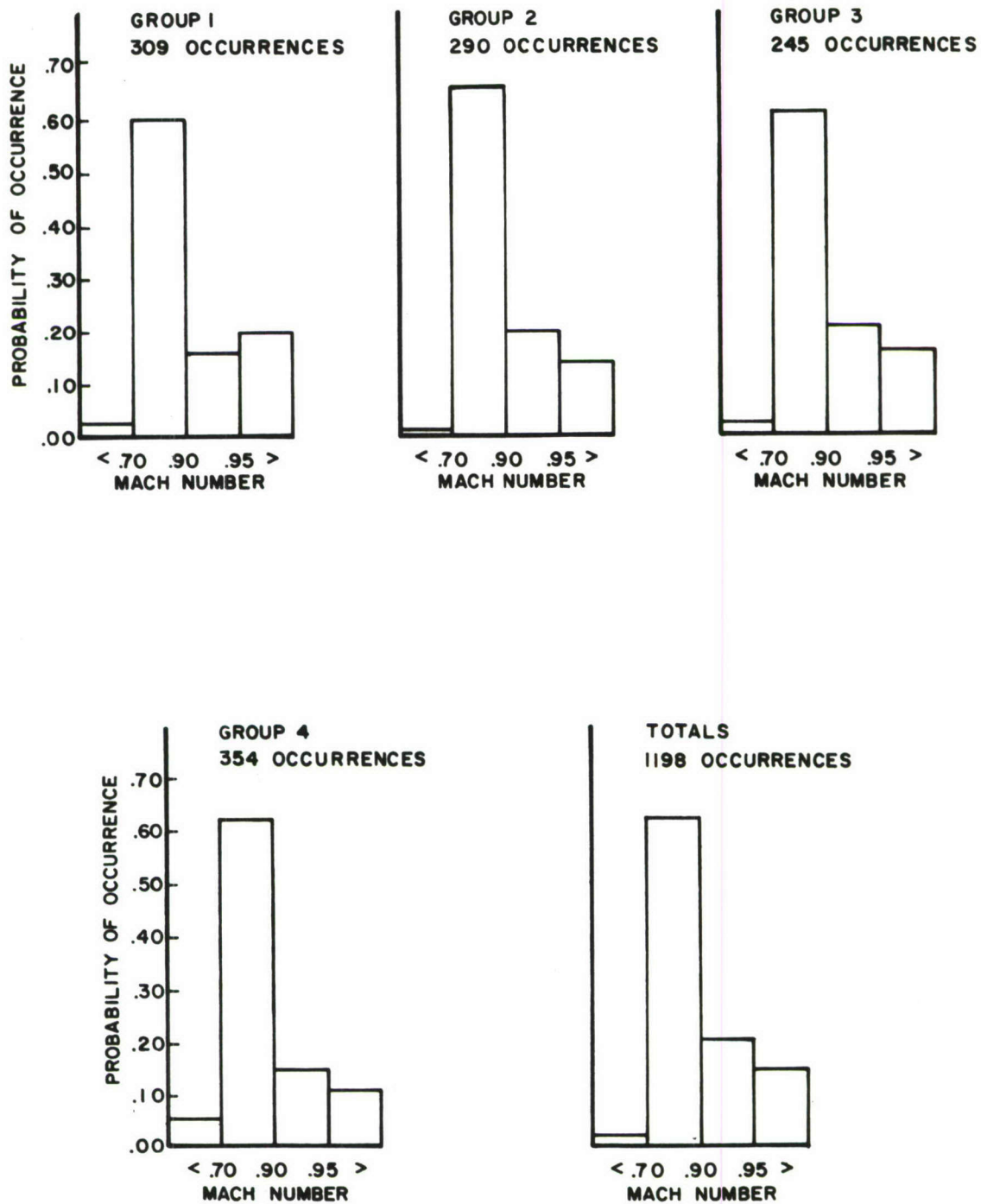
Figure 16    Mach Number Probability by Group for F-105D Pull-up
after Weapon Release, Configuration 3 Data

67
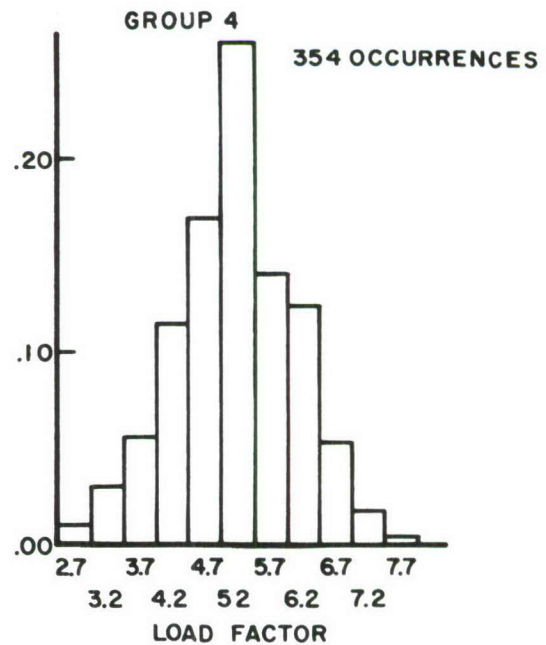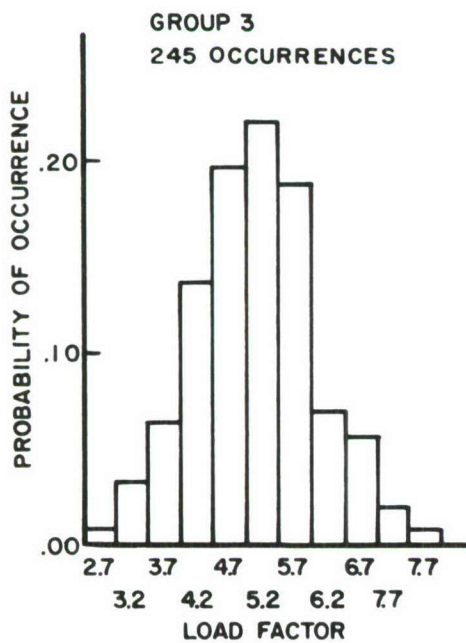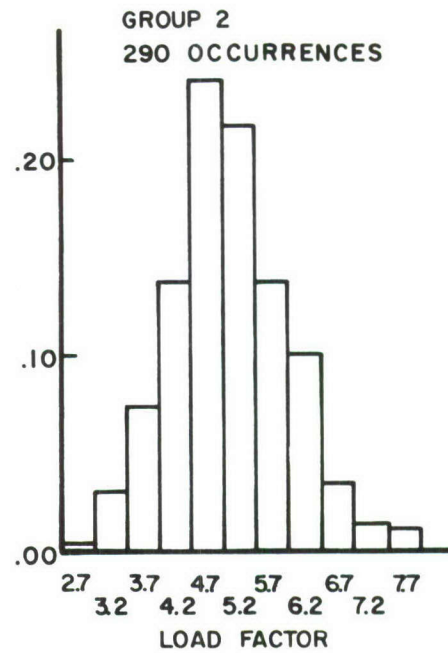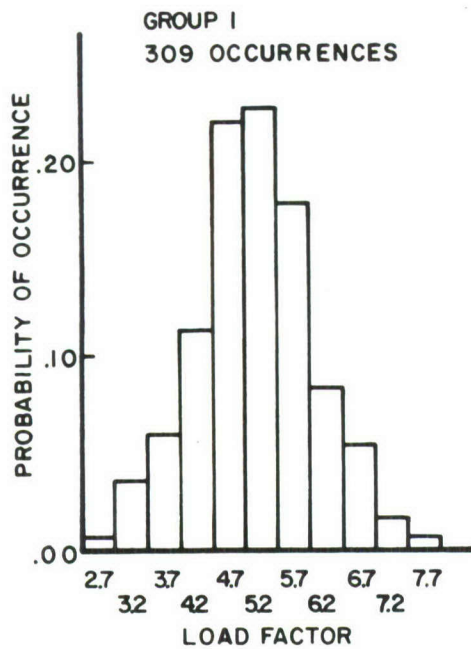
Figure 17    Load Factor Probability by Group for F-105D Pull-up
After Weapon Release, Configuration 3 Data

68
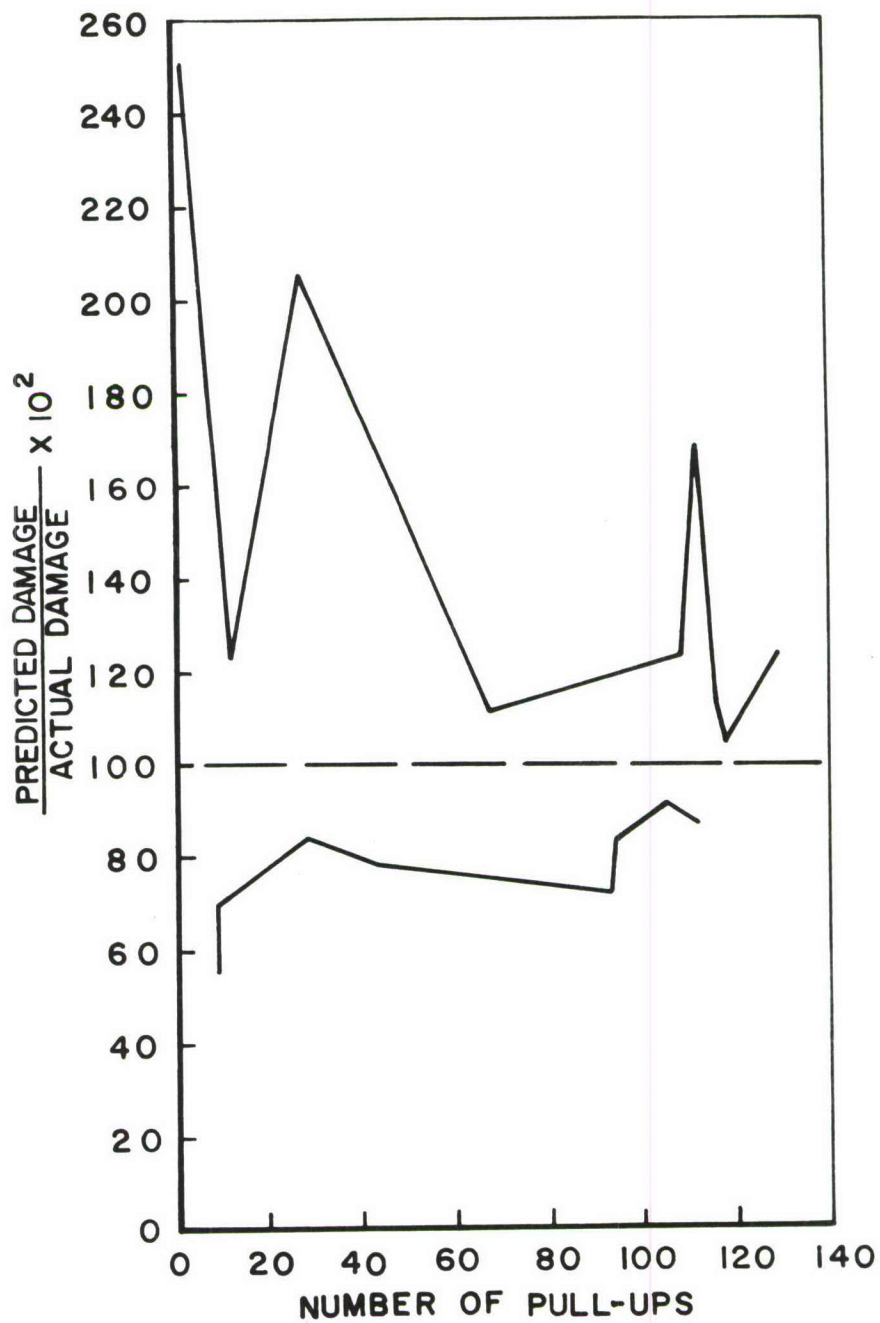
Figure 18    Damage Ratio vs Pull-up Sample Size for Mach-
Altitude Probability Damage Prediction Technique
Probability Model Based on Total Configuration 3
Pull-ups, Top Skin at Fuselage Station 509
Damage ratios from Table XXI
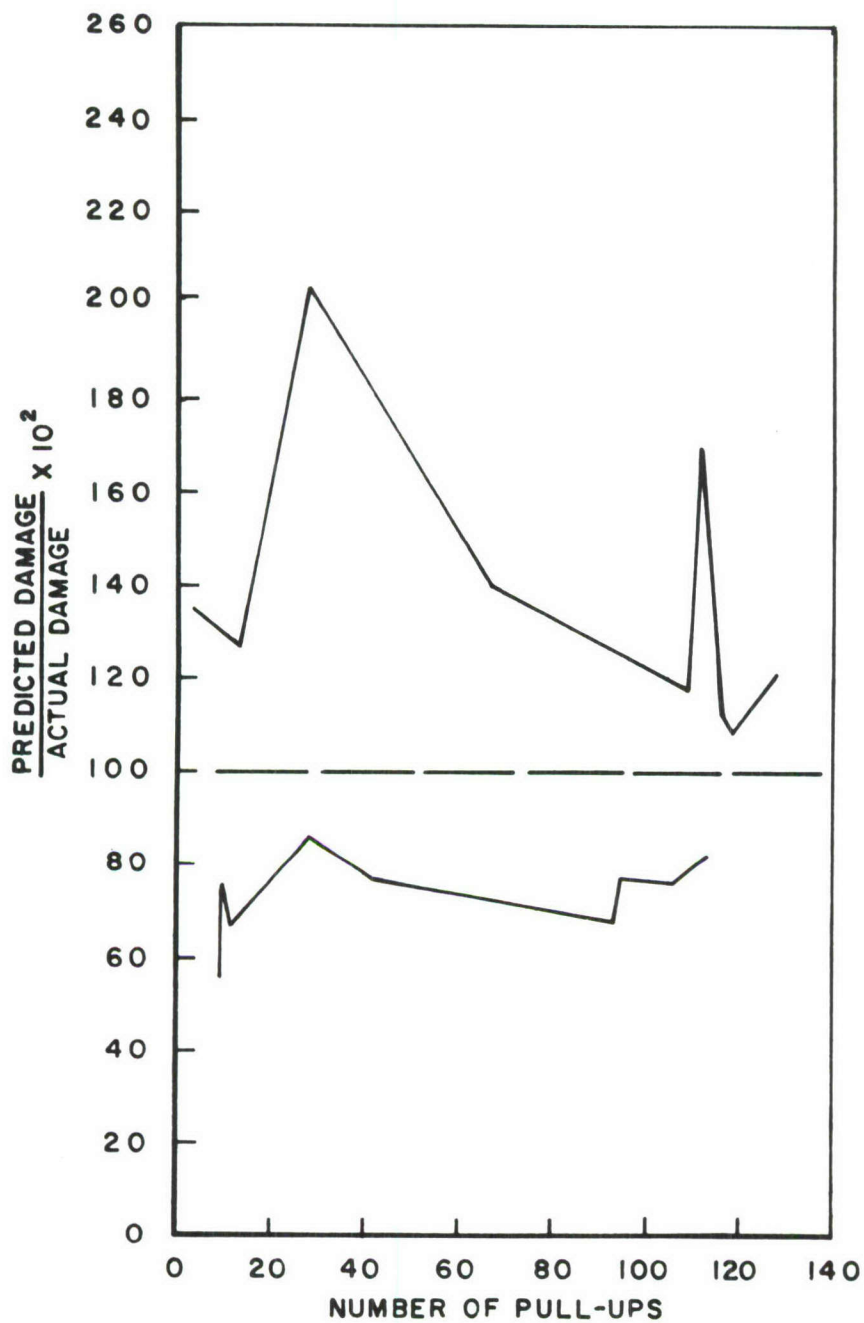
Figure 19  Damage Ratio vs Pull-up Sample Size for Mach-Altitude
Probability Damage Prediction Technique
Probability Model based on Total Configuration 3 Pull-ups,
Transfer Spar at Fuselage Station 442
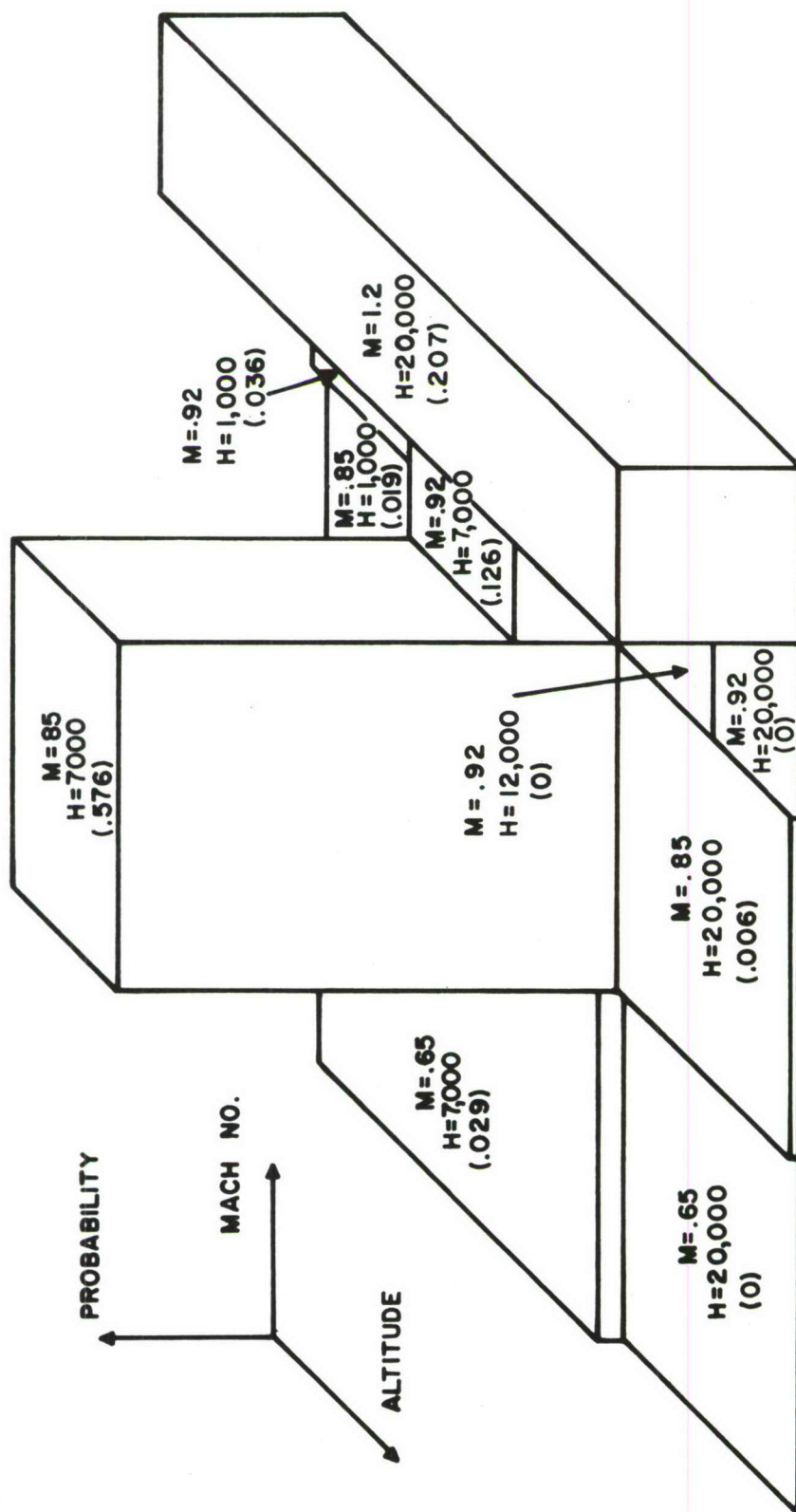Damage ratios from Table XXII
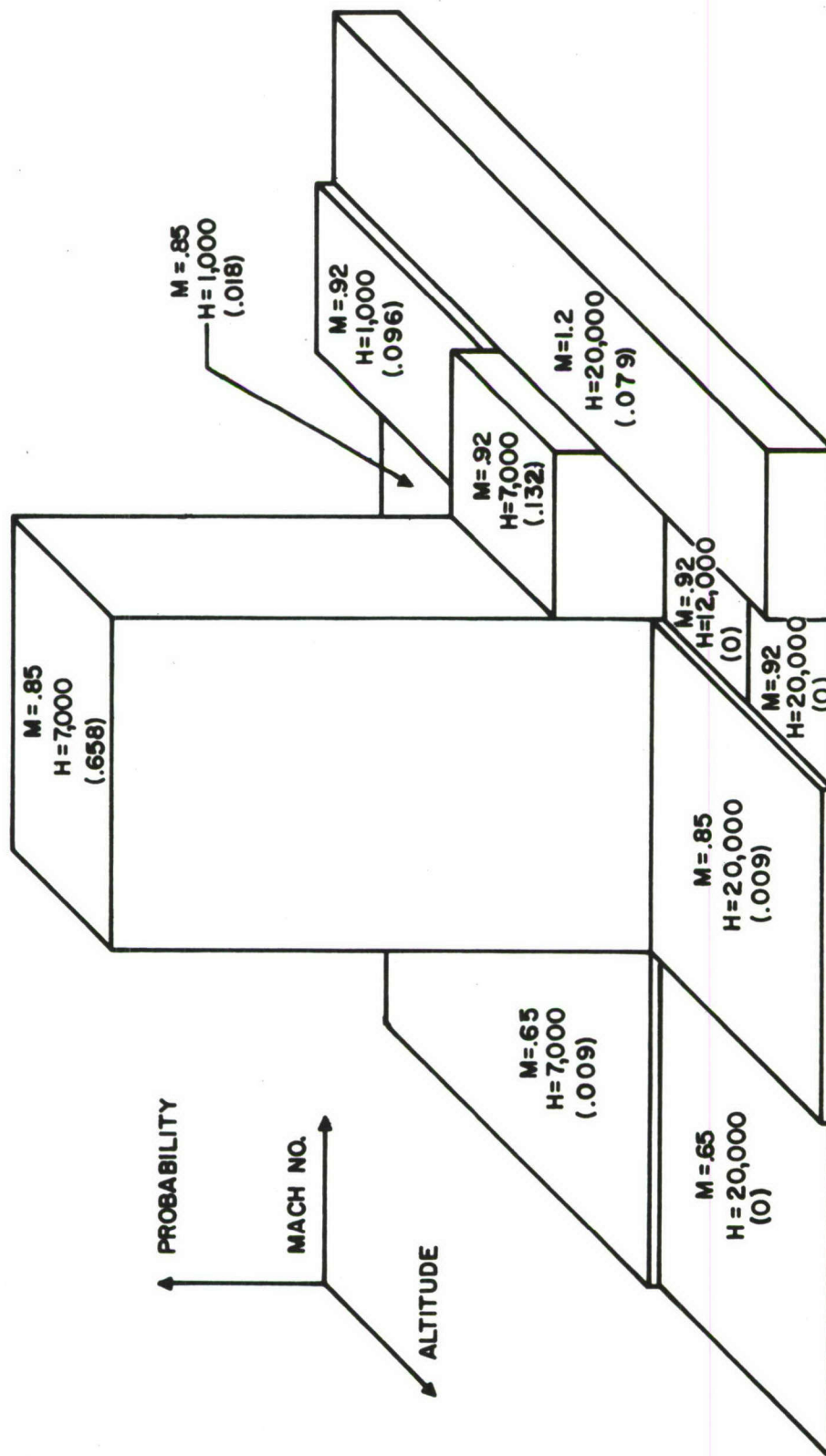
Figure 20 Mach-Altitude Probability Plot for First 114 F-105D Pull-ups after Weapon Release, Configuration 3 Data

71
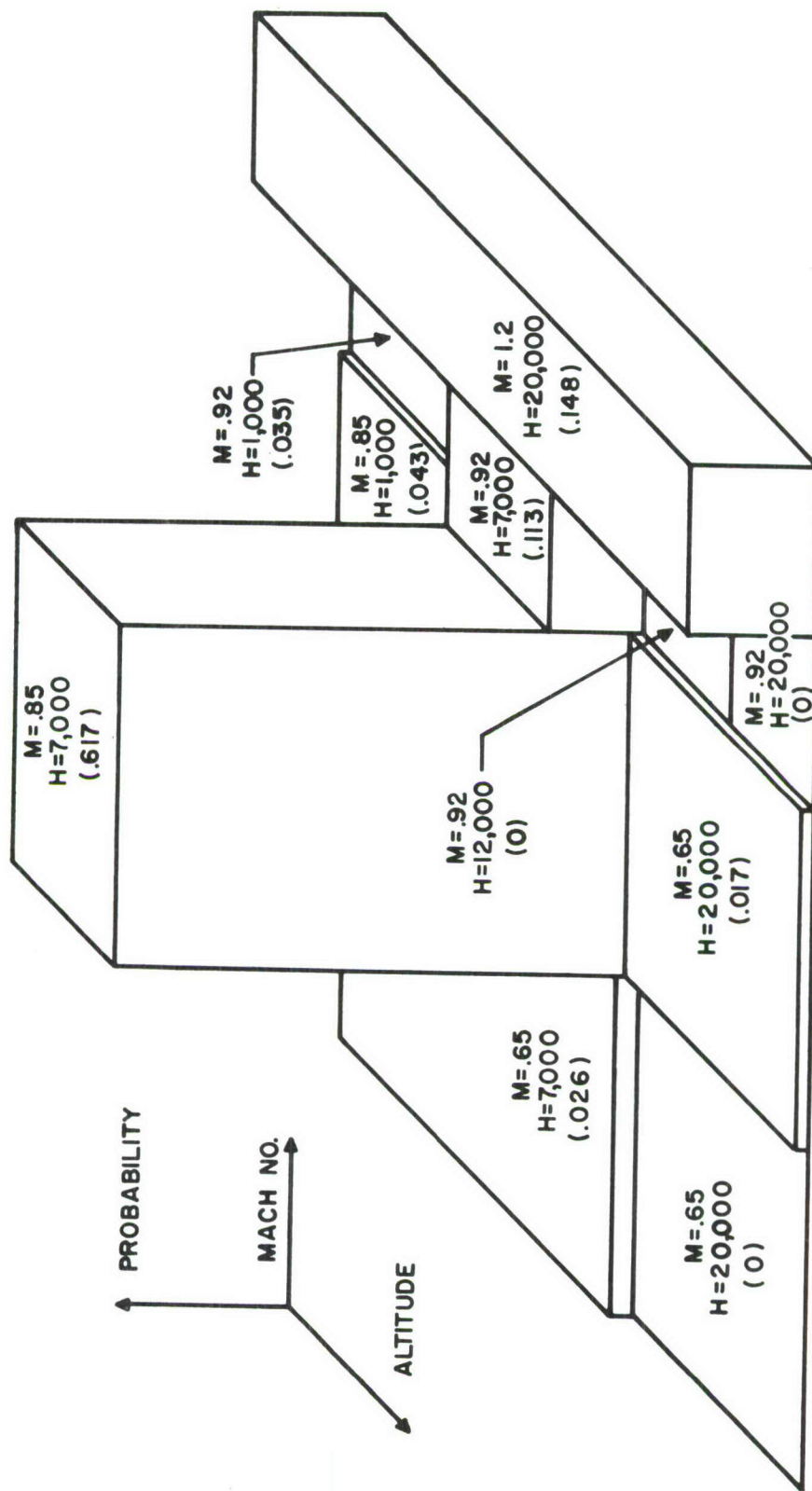
Figure 21  Mach-Altitude Probability Plot for Last 114 F-105D Pull-ups after Weapon Release, Configuration 3 Data
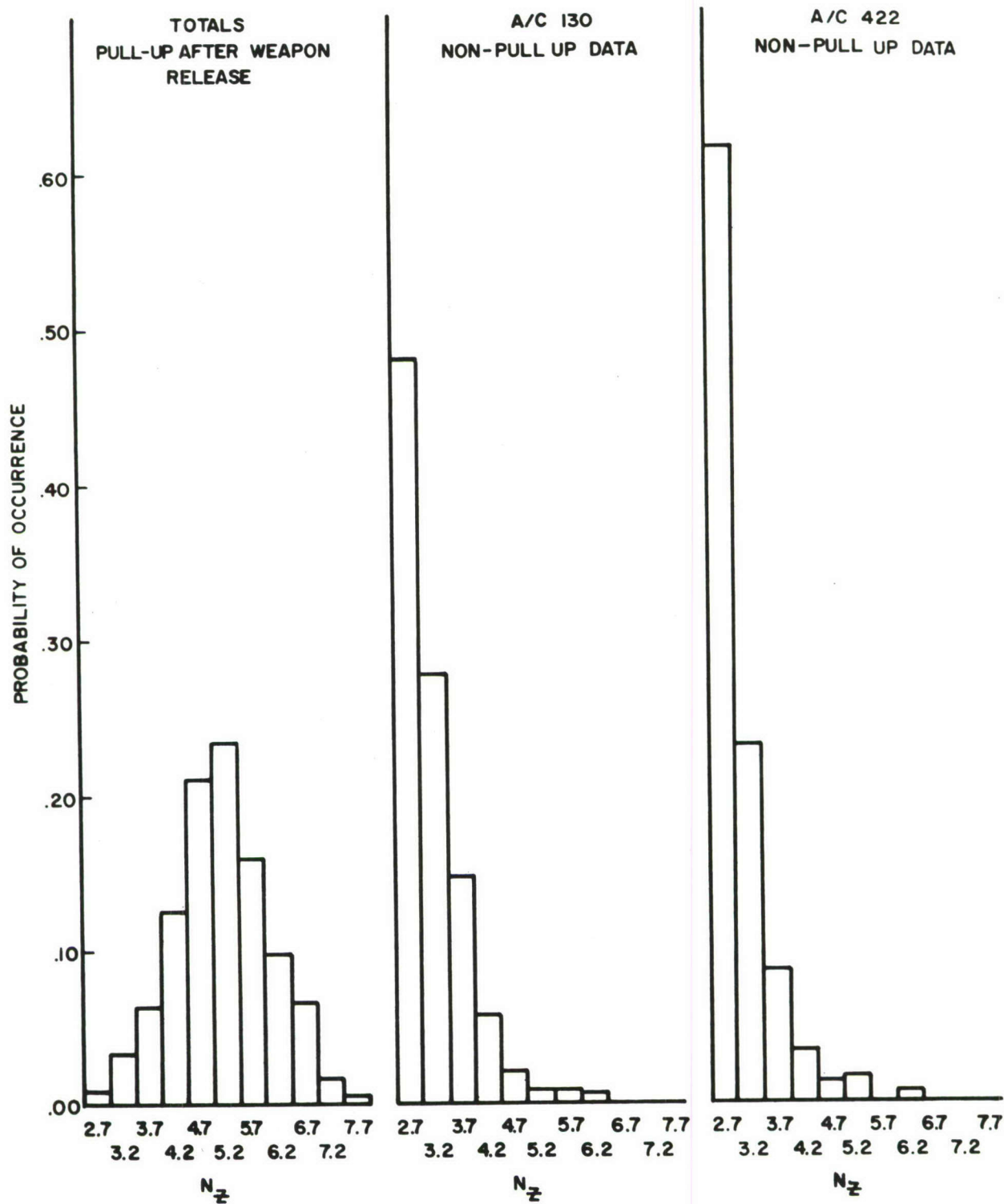
Figure 22    Comparison of Probability of Occurrence by Load Factor
for F-105D, Configuration 3 Pull-up and Non Pull-up Data

PROBABILITY

MACH NO.

ALTITUDE

M=.85
H=7000
(.588)

M=.65
H=7,000
(.007)

M=.92
H=12,000
(.007)

M=.85
H=1,000
(.010)

M=.92
H=1,000
(.051)

M=.92
H=7,000
(.165)

M=1.2
H=20,000
(.162)

M=.65
H=20,000
(.001)

M=.85
H=20,000
(.008)

M=.98
H=20,000
(0)

M=.85
H=7,000
(.742)

PROBABILITY

MACH NO.

ALTITUDE

M=.65
H=7,000
(.105)

M=.85
H=1,000
(.008)

M=.92
H=1,000
(.016)

M=.92
H=7,000
(.040)

M=1.2
H=20,000
(.040)

M=.65
H=20,000
(0)

M=.85
H=20,000
(.032)

M=.92
H=12,000
(.016)

M=.92
H=20,000
(0)
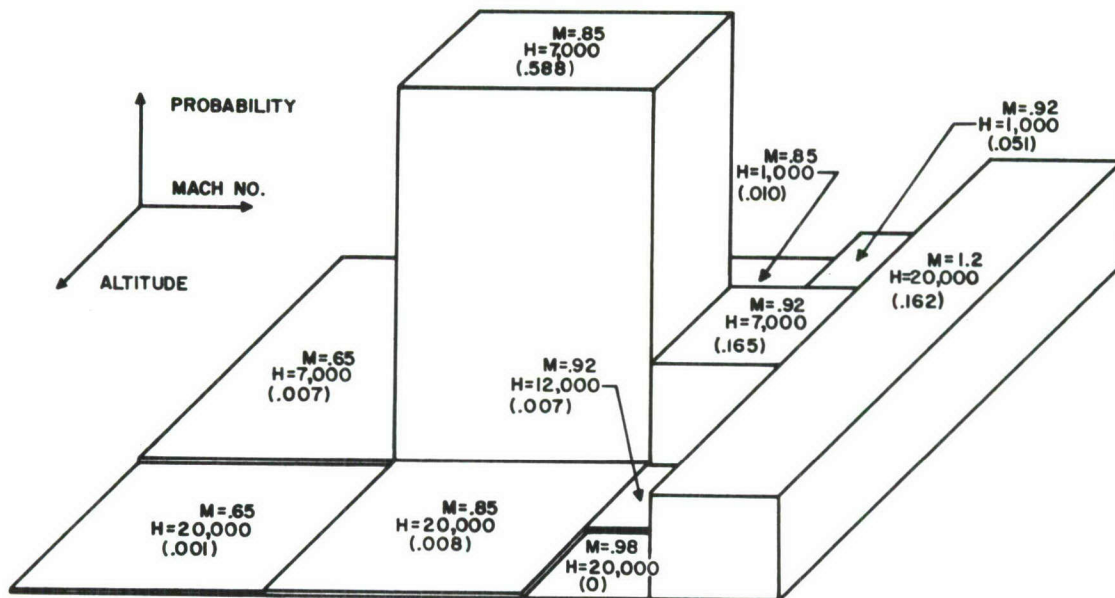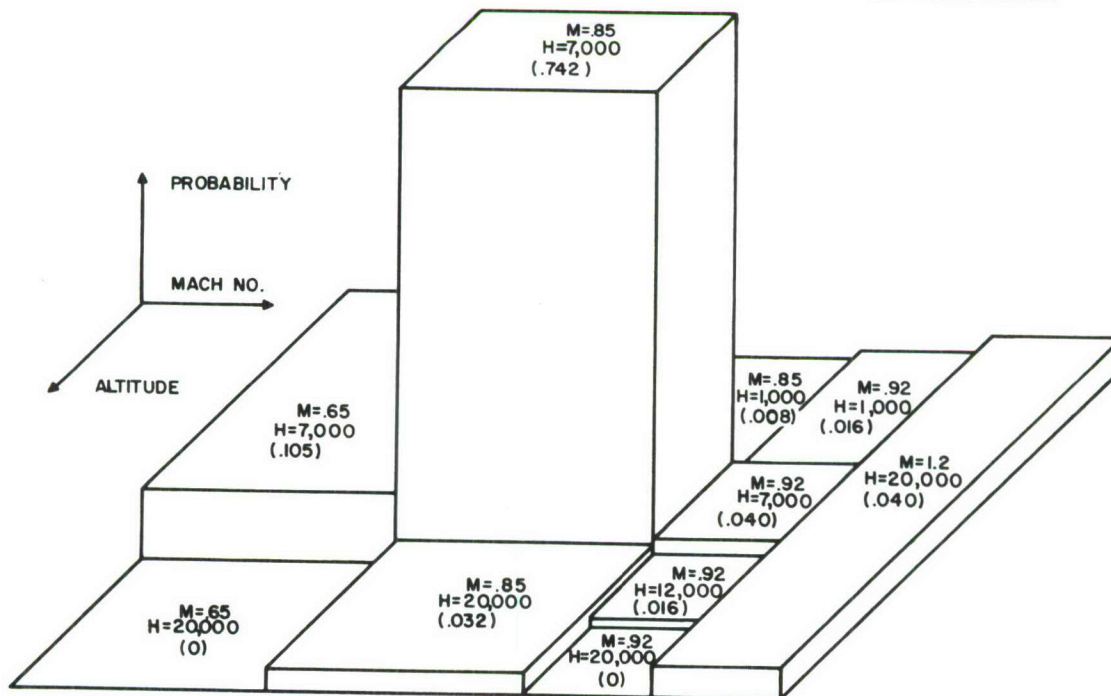
Figure 23    Mach-Altitude Probability Plot by Load Factor Magnitude
for F-105D Pull-up after Weapon Release,
Configuration 3 Data

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PROBABILITY

MACH NO.

ALTITUDE

M=.85
H=7,000
(.388)

M=.65
H=7,000
(.095)

M=.85
H=20,000
(.364)

M=.85
H=1,000
(0)

M=.92
H=1,000
(0)

M=.92
H=7,000
(.010)

M=1.2
H=20,000
(.031)

M=.65
H=20,000
(.075)

M=.92
H=12,000
(.020)

M=.92
H=20,000
(.017)
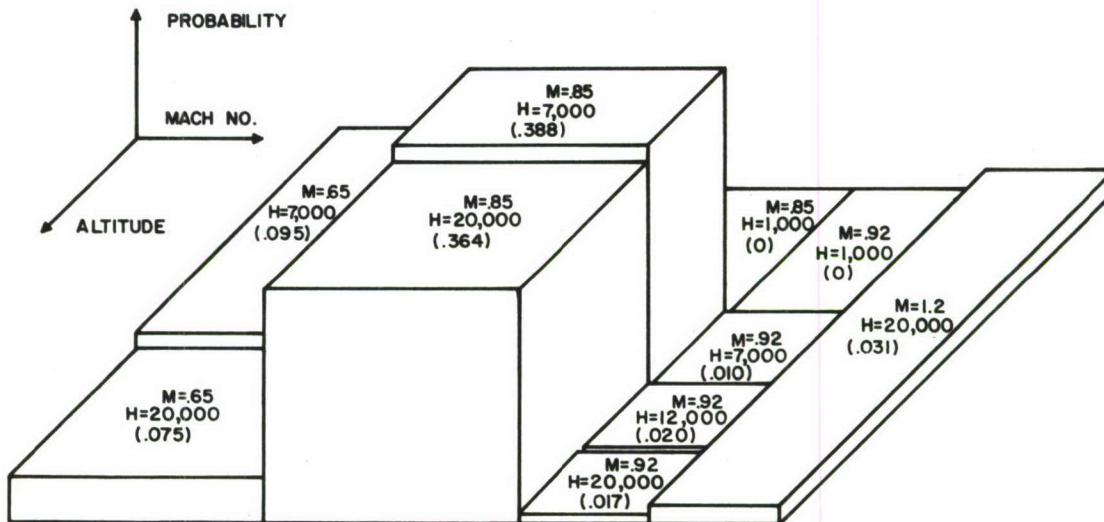
A/C   130
357   OCCURRENCES
ALL   $N_z$

PROBABILITY

MACH NO.

ALTITUDE

M=.85
H=7,000
(.515)

M=.65
H=7,000
(.081)

M=.85
H=20,000
(.157)

M=.85
H=1000
(.014)

M=.92
H=1,000
(.011)

M=.92
H=7,000
(.064)

M=1.2
H=20,000
(.090)

M=.65
H=20,000
(.020)

M=.92
H=12,000

M=.92
H=20,000
(.006)

Figure 24   Mach-Altitude Probability Plot for F-105D Non Pull-up,
Configuration 3 Data for Two Typical Aircraft

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3.      F-105F AIRCRAFT

    a.    Comparison With F-105D Aircraft Analysis

        The analysis of the F-105F aircraft was performed using the same
basic ground-rules as were employed in the analysis of the F-105D reported in
Section II-2 of this report.  There are some differences in the basic aircraft as
well as differences in the data collection and reduction criteria.  These differ-
ences, together with assumptions that were made with regard to the following
analysis are enumerated below:

        (1)   The F-105F is a two-place aircraft, whereas the F-105D aircraft
is a one-place aircraft.  In the absence of stress versus load factor data for the
F-105F, the F-105D data was used with the actual F-105F gross weights.
        (2)   The Mach-altitude subdivisions shown in Table VI of Section II-2
were used for computing fatigue damages to the F-105F.
        (3)   There was a difference in the criteria used to define the maneuver
mission segment for the two flightloads programs, on which the F-105D and
F-105F data samples were obtained.
        (4)   There was a significant variation of the data with respect to mis-
sion type for the F-105F data sample.  Therefore, it was necessary to consider
this additional variable in the F-105F parametric fatigue analysis.

    b.    Fatigue Damage Analysis

        The fatigue damage analysis reported herein is based on a 1,001 hour
VGH data sample obtained at two air bases in the Southeast Asia combat zone and
reported in Reference 7.  This data was recorded on 456 flights.  The fatigue
damage was calculated for the same fatigue critical locations as were monitored
for the F-105D and the remarks with regard to damage calculation, major con-
figuration, Mach-altitude block designation, gross weight and load factor classi-
fication contained in Section II-2a of this report are applicable.

        (1)   Parametric Analysis

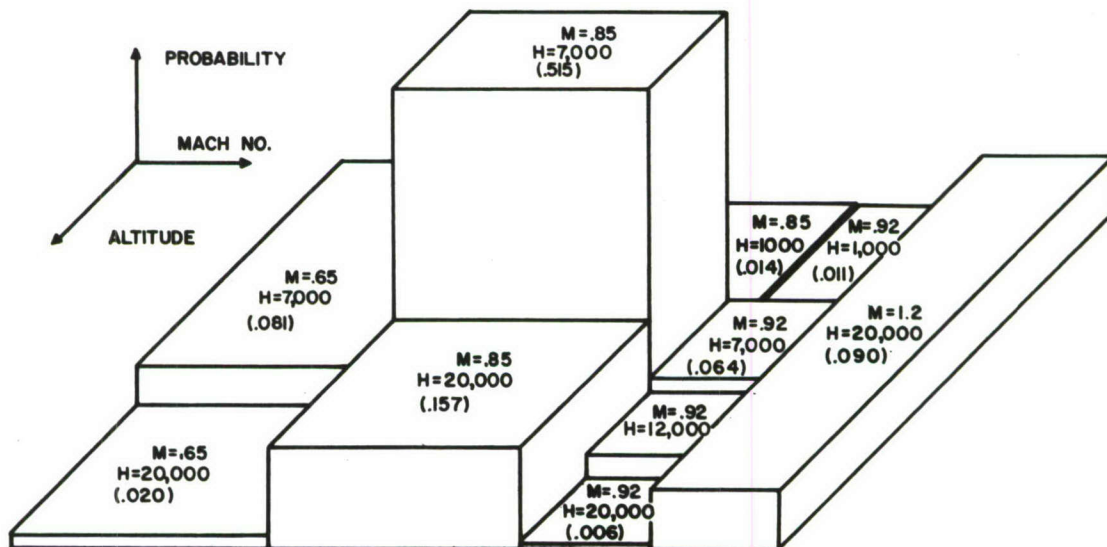        The damage sensitivity studies reported in Section II-2a(1) apply
to this F-105F analysis.  The classification of the data with respect to mission
type is defined in Reference 7 and presented in Table XXXIV of this report.  The
classification of the processed data by mission type and air base is presented in
Table XXXV.  There is considerable variation in the amount of data recorded by
both mission type and air base.

        (2)   Damage Analysis by Mission Segment

        The airborne portion of the flight was classified into the mission
segments of ascent, maneuver, cruise, refuel, and descent.  Damage was com-
puted for each of the load factor occurrences greater than 2.5 g's by mission

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segment. The results are presented in Tables XXXVI and XXXVII for fuselage stations 442 and 509, respectively. More than 99 percent of the total damage, exclusive of the ground-air-ground cycle, occurred during the maneuver mission segment at both aircraft fatigue critical locations.

(3) Analysis of Maneuver Mission Segment Data

On the basis of the data presented in Tables XXXVI and XXXVII, the parametric analysis was confined to the determination of damage in the maneuver mission segment. The damage in the maneuver mission segment was further separated into two categories: pull-up after weapon release or gunfiring, and all other maneuvers. The results of these calculations are presented in Tables XXXVIII and XXXIX for fuselage stations 442 and 509, respectively. Examinations of these figures reveal that approximately 85 percent of the total aircraft damage, exclusive of the ground-air-ground cycle, occurs during pull-up after weapon release or gunfiring for the fatigue critical points under consideration.

c. Damage Prediction Techniques

Based on the relative importance of the load factor occurrences during pull-up after weapon release or gunfiring, the primary effort was directed toward development of a method for predicting this damage.

(1) Mach-Altitude Probability Technique

The F-105F pull-ups after weapon release or gunfiring were classified according to the major exit configuration and mission type. The results are presented in Table XL by air base. These results show that 93 percent of the occurrences at Base 1 are in Major Configuration 1. At Base 2, 98 percent of the occurrences are in Major Configuration 3. This points out a very definite difference in the aircraft configuration at the two bases. However, the use of different Mach-altitude probability models by major configuration would accomplish this separation automatically.

Due to the small sample size available for analysis, and in view of the results obtained for the F-105D, the application of the Mach-altitude probability model damage prediction technique was restricted to the occurrences in exit Configuration Three. The Mach-altitude probabilities for Base 2 are presented by load factor magnitude and independent of gross weight and mission type in Table XLI. These data, with load factor magnitude eliminated as a variable, are presented in the form of a three-dimensional plot in Figure 25. The fatigue damage was predicted as described in Section II-2b(1) of this report, and the results are presented in Table XLII for fuselage stations 442 and 509, respectively.

(2) Calculation of Damages

As shown in Table XL, there is a distinct difference in the exit configuration by base for the F-105F pull-ups after weapon release or gunfiring.

Therefore, the damages based on both the total data sample and by base were computed on a per-hour, per-flight, and per pull-up basis. The resulting damage ratios are presented in Tables XLIII, XLIV, and XLV. The corresponding variances are shown at the bottom of each table. The variances were calculated as described in Section II-2b(2) for a truncated data sample formed by eliminating aircraft serial numbers 8321 and 8278. As shown by the variances, a distinct improvement is realized in the variances by calculating the damages for all three methods on a per-base basis. The improvement at fuselage station 509 is decidedly greater than at fuselage station 442.

The preceding analysis was performed independently of mission type. As was pointed out in Section II-3a(4), there exists a significant variation in the data by mission type. All of the pull-up occurrences in mission types 8 and 9 of Table XL result from night-time missions as shown in Table XXIV. Figure 26 shows the separation of the data by day-time and night-time missions. The probability of occurrences as a function of both load factor level and Mach number is shown. As would be expected, no high magnitude pull-ups were experienced during the night-time missions. Also, the Mach number experience was all in the .70 to .90 range. Therefore, it appears that the damage prediction by any of the techniques being employed would yield better results if this additional parameter were included in the analysis.

d. Discussion

The same general discussion presented for the F-105D in Section II-2c is also pertinent to the F-105F aircraft. Specifically, the F-105F data sample, although somewhat limited in size, pointed out that different utilization can result in the addition or deletion of variables in the fatigue damage analysis of the fighter aircraft. The F-105F fatigue damages were found to be quite sensitive to air base location and time-of-day usage. This serves to point up the fact that not only do the damage rates have to be revised continuously on the basis of aircraft utilization, but also that the number of parameters being considered must also be revised to compensate for different modes of utilization.

TABLE XXXIV

Definition of Mission Type for the F-105F SEA Data Sample

| Code | Type Mission |
|---|---|
| 1 | Ground Gunnery* |
| 2 | Conventional Bombing (Martin) |
| 3 | Air Patrol and Air-to-Air Gunnery |
| 4 | Special & Search & Rescue[+] |
| 5 | Escort |
| 6 | Instrumentation, Navigation & Test Hop |
| 7 | Conventional Bombing (W. W. Daytime) |
| 8 | Conventional Bombing (W. W. Nighttime) |
| 9 | Conventional Bombing (Night Raiders) |

*Includes Strafing, SAM Strike, and Shrike Launch Missions

[+]Includes Search and Rescue and SAM Search Missions

TABLE XXXV

Recorded Data by Mission Type and Air Base
for F-105F Data Sample

| Mission Code | (Base 1) Takhli AB | (Base 2) Korat AB | Total | Percent of Total |
|---|---|---|---|---|
| 1 | 194.9 | 135.9 | 330.8 | 33.0 |
| 2 | - | 131.7 | 131.7 | 13.1 |
| 3 | - | 11.8 | 11.8 | 1.2 |
| 4 | 158.9 | 103.5 | 262.4 | 26.2 |
| 5 | 41.6 | 75.3 | 116.9 | 11.7 |
| 6 | 8.8 | 9.7 | 18.5 | 1.9 |
| 7 | 17.4 | - | 17.4 | 1.7 |
| 8 | 9.8 | 31.0 | 40.8 | 4.1 |
| 9 | - | 70.9 | 70.9 | 7.1 |
| | 431.4 | 569.8 | 1001.2 | 100.0 |

## TABLE XXXVI

Tabulation of Damage by Mission Segment for
the F-105F Transfer Spar at Fuselage Station 442
by Aircraft Serial Number

| A/C | Damages x $10^5$ | | | $\dfrac{\text{Maneuver}}{\text{Total}} \times 10^2$ |
| | Maneuver Mission Segment | All other Mission Segments | Total | |
|---|---|---|---|---|
| 4436 | 648.7364 | 3.5307 | 652.2671 | 99.46 |
| 8301 | 1043.2609 | 3.2982 | 1046.5591 | 99.68 |
| 8311 | 1198.3468 | 4.7994 | 1203.1462 | 99.60 |
| 8316 | 842.7527 | 13.5657 | 856.3184 | 98.41 |
| 8321 | 82.0003 | 1.5050 | 83.5053 | 98.19 |
| Base 1 | 3815.0971 | 26.6990 | 3841.7961 | 99.30 |
| 4446 | 481.6040 | 6.0914 | 487.6954 | 98.75 |
| 8302 | 428.5441 | 2.0554 | 430.5995 | 99.52 |
| 8329 | 1813.7759 | 4.3401 | 1818.1160 | 99.76 |
| 8336 | 631.0819 | 3.7573 | 634.8392 | 99.40 |
| 8278 | 9.0285 | 4.1070 | 13.1355 | 68.73 |
| Base 2 | 3364.0344 | 20.3512 | 3384.3856 | 99.40 |
| Total | 7179.1315 | 47.0502 | 7226.1817 | 99.34 |

## TABLE XXXVII

Tabulation of Damage by Mission Segment for
the F-105F Top Cover Skin at Fuselage Station 509
by Aircraft Serial Number

| | Damages x $10^5$ | | | |
|---|---|---|---|---|
| A/C | Maneuver Mission Segment | All Other Mission Segments | Total | $\dfrac{\text{Maneuver}}{\text{Total}}$ x $10^2$ |
| 4436 | 502.3881 | 3.9671 | 506.3552 | 99.22 |
| 8301 | 1027.7868 | 2.8694 | 1030.6562 | 99.72 |
| 8311 | 1166.6276 | 4.0279 | 1170.6555 | 99.66 |
| 8316 | 918.5769 | 8.4753 | 927.0522 | 99.09 |
| 8321 | 70.8500 | 0.1325 | 70.9825 | 99.81 |
| Base 1 | 3686.2294 | 19.4722 | 3705.7016 | 99.47 |
| 4446 | 146.3457 | 2.9242 | 149.2699 | 98.04 |
| 8302 | 103.7704 | 0.7483 | 104.5187 | 99.28 |
| 8329 | 421.8694 | 1.6418 | 423.5112 | 99.61 |
| 8336 | 129.9312 | 0.9207 | 130.8519 | 99.30 |
| 8278 | 0.9992 | 0.7507 | 1.7499 | 57.10 |
| Base 2 | 802.9159 | 6.9857 | 809.9016 | 99.14 |
| Total | 4489.1453 | 26.4579 | 4515.6032 | 99.41 |

## TABLE XXXVIII

Tabulation of Damage due to Pull-up after Weapon Release
for Transfer Spar at Fuselage Station 442 on F-105F Aircraft

| | Damages x $10^5$ | | |
|---|---|---|---|
| A/C | Maneuver Mission Segment | Pull-up after Weapon Release | $\dfrac{\text{Pull-up}}{\text{Maneuver}}$ x $10^2$ |
| 4436 | 648.7364 | 568.9416 | 87.70 |
| 8301 | 1043.2609 | 970.9624 | 93.07 |
| 8311 | 1198.3468 | 1041.7746 | 86.93 |
| 8316 | 842.7527 | 714.7875 | 84.82 |
| 8321 | 82.0003 | 69.4247 | 84.66 |
| Base 1 | 3815.0971 | 3365.8908 | 88.23 |
| 4446 | 481.6040 | 329.2365 | 68.36 |
| 8302 | 428.5441 | 322.1226 | 75.17 |
| 8329 | 1813.7759 | 1665.1987 | 91.81 |
| 8336 | 631.0819 | 518.8760 | 82.22 |
| 8278 | 9.0285 | 1.0218 | 11.32 |
| Base 2 | 3364.0344 | 2836.4547 | 84.32 |
| Total | 7179.1315 | 6202.3455 | 86.39 |

## TABLE XXXIX

Tabulation of Damage due to Pull-up after Weapon Release
for Top Cover Skin at Fuselage Station 509 on F-105F Aircraft

| A/C | Damages x $10^5$ | | $\dfrac{\text{Pull-up}}{\text{Maneuver}}$ x $10^2$ |
| --- | --- | --- | --- |
| | Maneuver Mission Segment | Pull-up after Weapon Release | |
| 4436 | 502.3881 | 456.3848 | 90.84 |
| 8301 | 1027.7868 | 991.9268 | 96.51 |
| 8311 | 1166.6276 | 1063.2190 | 91.14 |
| 8316 | 918.5769 | 846.2096 | 92.12 |
| 8321 | 70.8500 | 64.6857 | 91.30 |
| Base 1 | 3686.2294 | 3422.4259 | 92.84 |
| 4446 | 146.3457 | 99.8291 | 68.21 |
| 8302 | 103.7704 | 61.7952 | 59.55 |
| 8329 | 421.8694 | 329.7180 | 78.16 |
| 8336 | 129.9212 | 89.3597 | 68.77 |
| 8278 | 0.9992 | 0.1209 | 12.10 |
| Base 2 | 802.9159 | 580.8229 | 72.34 |
| Total | 4489.1453 | 4003.2488 | 89.17 |

## TABLE XL

### Pull-up after Weapon Release or Gunfiring Occurrences
### by Configuration, Mission Type, and Air Base for F-105F Aircraft

#### Base 1

| Configuration | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
|---|---|---|---|---|---|---|---|---|
| 1 | 81 | | | 31 | | 2 | 7 | |
| 2 | 2 | | | 1 | | | | |
| 3 | 4 | | | | 2 | | | |
| 4 | | | | | | | | |
| 5 | | | | | | | | |

#### Base 2

| Configuration | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|---|---|---|---|---|---|---|---|---|---|
| 1 | | | | | | | | | |
| 2 | | | | | | | | | |
| 3 | 37 | 42 | 4 | 25 | 1 | | | 7 | 11 |
| 4 | | | | | | | | | |
| 5 | | | | 2 | | | | | |

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# TABLE XLI

## Mach-Altitude Probability Distribution for F-105F, Base 2, Configuration 3 Pull-up After Weapon Release

| Mach.<br>Alt.<br>K Ft. | .65<br>7 | .65<br>20 | .85<br>1 | .85<br>7 | .85<br>20 | .92<br>1 | .92<br>7 | .92<br>12 | .92<br>20 | 1.2<br>20 |
|---|---|---|---|---|---|---|---|---|---|---|
| 2.7 | | | | .800 | .200 | | | | | |
| 3.2 | | | | .615 | .385 | | | | | |
| 3.7 | | | | .778 | .112 | | .112 | | | |
| 4.2 | | .059 | | .588 | .118 | | .176 | | | .059 |
| 4.7 | | | | .500 | | | .273 | .091 | | .136 |
| 5.2 | .034 | | | .621 | | | .207 | | | .138 |
| 5.7 | | | | .445 | .056 | | .112 | .056 | | .334 |
| 6.2 | | | | .250 | | | .250 | | | .500 |
| 6.7 | | | | .200 | | | .400 | | | .400 |
| 7.2 | | | | | | | | | | |
| 7.7 | | | | | | | | | | |

## TABLE XLII

### Damage Predicted for Pull-ups Using Base 2, Configuration 3 Probability Model for F-105F

| A/C | Actual Damage | Predicted Damage | No. Configuration 3 Pull-ups | Predicted Damage / Actual Damage |
|---|---|---|---|---|
| | | Fuselage Station 509 | | |
| 4436 | 1.9316 | 11.3840 | 4 | 5.89 |
| 8301 | -- | -- | 0 | |
| 8311 | -- | -- | 0 | |
| 8316 | 0.0 | 0.0176 | 1 | |
| 8321 | 0.0 | 0.0 | 1 | |
| Subtotal Base 1 | 1.9316 | 11.4016 | 6 | 5.90 |
| 4446 | 99.7744 | 136.1765 | 32 | 1.36 |
| 8302 | 61.7952 | 81.9010 | 21 | 1.33 |
| 8329 | 329.7180 | 150.5767 | 21 | 0.46 |
| 8336 | 89.3597 | 205.6577 | 42 | 2.30 |
| 8278 | 0.1209 | 0.0465 | 11 | 0.38 |
| Subtotal Base 2 | 580.7682 | 574.3584 | 127 | 0.99 |
| Totals | 582.6998 | 585.7600 | 133 | 1.01 |
| | | Fuselage Station 442 | | |
| 4436 | 13.3438 | 32.5681 | 4 | 2.44 |
| 8301 | -- | -- | 0 | |
| 8311 | -- | -- | 0 | |
| 8316 | 0.5862 | 0.6515 | 1 | 1.11 |
| 8321 | 0.0847 | 0.1576 | 1 | 1.86 |
| Subtotal Base 1 | 14.0147 | 33.3772 | 6 | 2.38 |
| 4446 | 328.4312 | 452.1126 | 32 | 1.38 |
| 8302 | 322.1226 | 298.3727 | 21 | 0.93 |
| 8329 | 1665.1978 | 768.3214 | 21 | 0.46 |
| 8336 | 518.8760 | 878.6898 | 42 | 1.69 |
| 8278 | 1.0218 | 1.0572 | 11 | 1.03 |
| Subtotal Base 2 | 2835.6494 | 2398.5537 | 127 | 0.85 |
| Totals | 2849.6641 | 2431.9309 | 133 | 0.85 |

## TABLE XLIII

### Predicted Damage Ratios per Flight Hour
### for F-105F Data Sample

| | | Predicted Damage Actual Damage | | | |
| | | Fuselage Station 509 | | Fuselage Station 442 | |
| A/C | Flight Time (hrs) | Total | By Base | Total | By Base |
|---|---|---|---|---|---|
| 4436 | 77.44 | 0.69 | 1.31 | 0.86 | 1.06 |
| 8301 | 56.55 | 0.25 | 0.47 | 0.39 | 0.48 |
| 8311 | 109.17 | 0.42 | 0.81 | 0.65 | 0.81 |
| 8316 | 164.00 | 0.80 | 1.52 | 1.38 | 1.71 |
| 8321 | 24.19 | 1.54 | 2.93 | 2.09 | 2.58 |
| Subtotal Base 1 | 431.35 | 0.53 | 1.00 | 0.81 | 1.00 |
| 4446 | 135.01 | 4.08 | 1.29 | 2.00 | 1.64 |
| 8302 | 112.69 | 4.86 | 1.53 | 1.89 | 1.55 |
| 8329 | 113.86 | 1.21 | 0.38 | 0.45 | 0.37 |
| 8336 | 131.68 | 4.54 | 1.43 | 1.50 | 1.23 |
| 8278 | 76.69 | 197.41 | 62.21 | 42.08 | 34.63 |
| Subtotal Base 2 | 569.83 | 3.17 | 1.00 | 1.22 | 1.00 |
| Totals | 1001.18 | 1.00 | | 1.00 | |
| $S^2 =$ | | 4.0295 | .2213 | .4066 | .2694 |

$$S^2 = \frac{n\Sigma(X_i)^2 - (\Sigma X_i)^2}{n(n-1)}$$

|  | Damage Rates | |
|---|---|---|
|  | Station 509 | Station 442 |
| Base 1 | .0000859 | .0000891 |
| Base 2 | .0000142 | .0000594 |
| Total | .0000451 | .0000722 |

TABLE XLIV

Predicted Damage Ratios per Flight for F-105F Data Sample

| A/C | Number of Flights | Predicted Damage / Actual Damage | | | |
| | | Fuselage Station 509 | | Fuselage Station 442 | |
| | | Total | By Base | Total | By Base |
|---|---|---|---|---|---|
| 4436 | 29 | 0.57 | 1.22 | 0.70 | 0.98 |
| 8301 | 24 | 0.23 | 0.50 | 0.36 | 0.51 |
| 8311 | 49 | 0.41 | 0.89 | 0.65 | 0.90 |
| 8316 | 62 | 0.66 | 1.42 | 1.15 | 1.60 |
| 8321 | 10 | 1.40 | 3.00 | 1.90 | 2.64 |
| Subtotal Base 1 | 174 | 0.47 | 1.00 | 0.72 | 1.00 |
| | | | | | |
| 4446 | 68 | 4.51 | 1.31 | 2.21 | 1.67 |
| 8302 | 51 | 4.83 | 1.40 | 1.88 | 1.42 |
| 8329 | 52 | 1.22 | 0.35 | 0.45 | 0.34 |
| 8336 | 61 | 4.62 | 1.34 | 1.52 | 1.15 |
| 8278 | 50 | 282.95 | 82.06 | 60.32 | 45.68 |
| Subtotal Base 2 | 282 | 3.45 | 1.00 | 1.32 | 1.00 |
| | | | | | |
| Total | 456 | 1.00 | | 1.00 | |
| $S^2$ = | | 4.4494 | .1797 | .4786 | .2362 |

$$S^2 = \frac{n\Sigma(X_i)^2 - (\Sigma X_i)^2}{n(n-1)}$$

| | Damage Rates | |
| | Station 509 | Station 442 |
|---|---|---|
| Base 1 | .000213 | .000221 |
| Base 2 | .000029 | .000120 |
| Total | .000099 | .000158 |

## TABLE XLV

### Predicted Damage Ratio per Pull-up for F-105F Data Sample

| A/C | Number of Pull-ups | Predicted Damage / Actual Damage — Fuselage Station 509 Total | By Base | Fuselage Station 442 Total | By Base |
|---|---|---|---|---|---|
| 4436 | 20 | 0.68 | 1.15 | 0.84 | 0.91 |
| 8301 | 18 | 0.28 | 0.48 | 0.44 | 0.48 |
| 8311 | 36 | 0.52 | 0.89 | 0.83 | 0.89 |
| 8316 | 50 | 0.91 | 1.56 | 1.68 | 1.81 |
| 8321 | 6 | 1.43 | 2.44 | 2.07 | 2.24 |
| Subtotal Base 1 | 130 | 0.59 | 1.00 | 0.92 | 1.00 |
| 4446 | 34 | 5.26 | 1.53 | 2.47 | 2.27 |
| 8302 | 21 | 5.25 | 1.53 | 1.56 | 1.43 |
| 8329 | 21 | 0.98 | 0.29 | 0.30 | 0.28 |
| 8336 | 42 | 7.26 | 2.12 | 1.94 | 1.78 |
| 8278 | 11 | 1406.31 | 409.65 | 257.80 | 236.71 |
| Subtotal Base 2 | 129 | 3.43 | 1.00 | 1.09 | 1.00 |
| Total | 259 | 1.00 | | 1.00 | |
| $s^2 =$ | | 7.8107 | .3769 | .5926 | .4919 |

$$s^2 = \frac{n\Sigma(X_i)^2 - (\Sigma X_i)^2}{n(n-1)}$$

| | Damage Rates Station 509 | Station 442 |
|---|---|---|
| Base 1 | .000263 | .000259 |
| Base 2 | .000045 | .000220 |
| Total | .000155 | .000239 |

PROBABILITY

MACH NO.

ALTITUDE

M=.85
H=1,000
(.017)

M=.92
H=1,000
(.107)

M=.92
H=7,000
(.157)

M=1.2
H=20,000
(.215)

M=.85
H=7,000
(.455)

M=.92
H=12,000
(.017)

M=.92
H=20,000
(0)

M=.85
H=20,000
(.025)
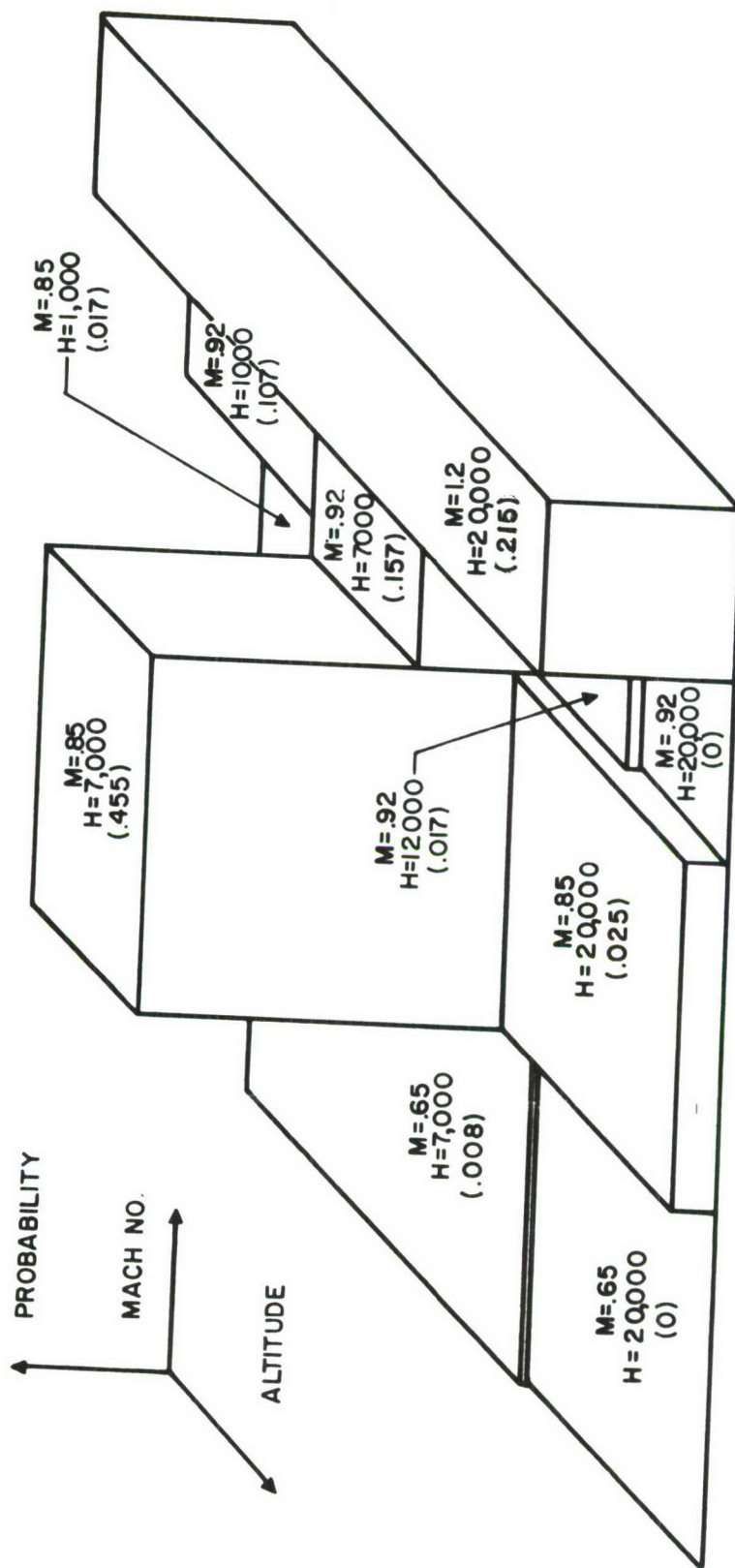
M=.65
H=7,000
(.008)

M=.65
H=20,000
(0)

Figure 25  Mach-Altitude Probability Plot for F-105F Configuration 3,  Base 2 Pull-ups
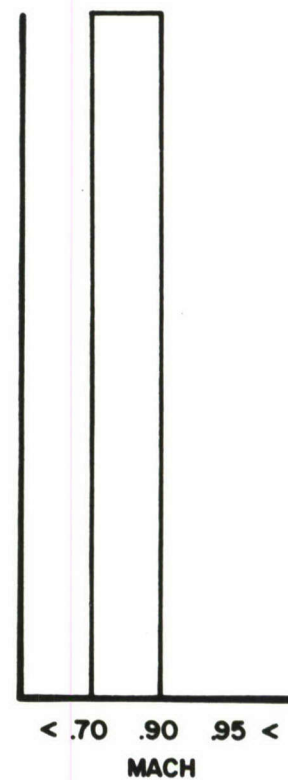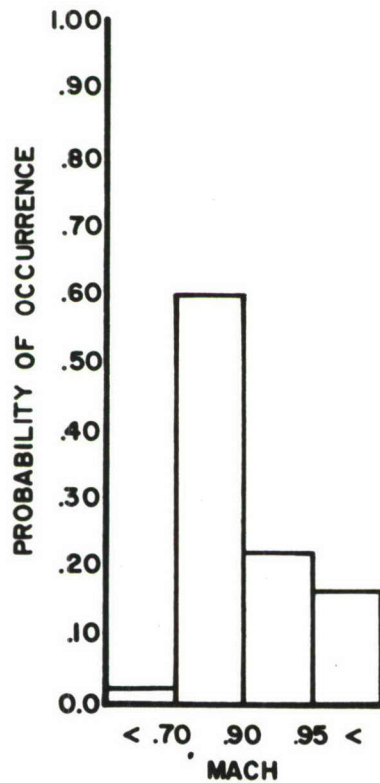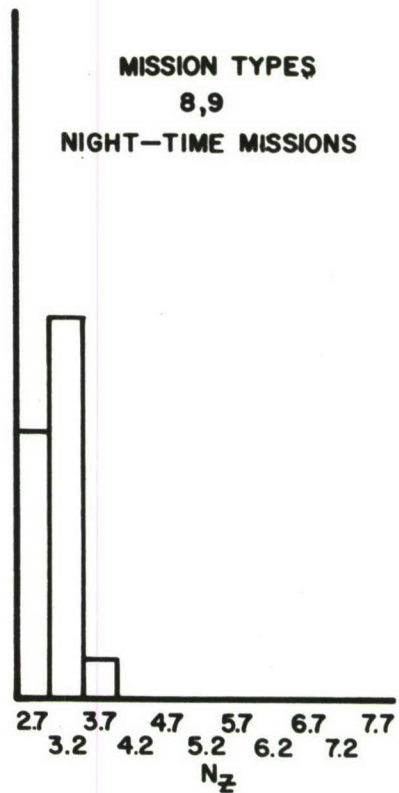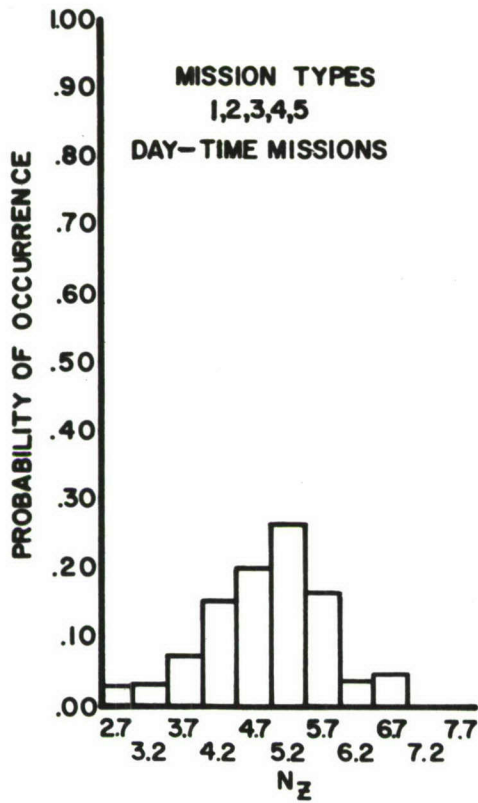After Weapon Release or Gunfiring

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Figure 26   Probability of Occurrence by Load Factor Magnitude and
Mach Number for F-105F, Base 2, Configuration 3
Pull-ups

# SECTION III

## RECORDER DESIGN

### 1. BACKGROUND

The cumulative fatigue monitoring of fighter-type aircraft presents a very definite challenge to a parametric type of analysis. This analysis is different from that of a bomber or cargo aircraft because the parameters change so rapidly that it is impossible to obtain them from a pilot's log sheet; and equally important is the fact that for fighter aircraft the source of damaging loads is maneuvering rather than gust encounters. Since the damage is a result of pilot-initiated maneuvers, and since the pilot has so much freedom in how he pulls-out after a weapon pass, there is a great amount of variability in the load factor spectrum from aircraft to aircraft. The analysis is further complicated by the large number of combinations of external stores and fuel pods that can be used.

In order to improve on the prediction of the fatigue damage beyond the prediction based on either a per-hour or per-flight average, it will be necessary to use some type of recorded data. The analysis of the F-5A data indicates that a counting accelerometer which segregates the load factor data by stores configuration would provide a more accurate estimate of the damage. The F-105D data indicates that there is little similarity among the various individual aircraft on the basis of Mach number, altitude, or load factor spectra, even for the same weapon configuration. Therefore, to make an accurate calculation of the fatigue damage, a record of the load factor as a function of Mach number, altitude, configuration and gross weight should be made. The measurement of all of the parameters is required so that the stress peaks can be calculated; however, if the stress peaks were to be measured, no other measurements would be required.

Some other observations about the data also warrant the installation of a recording device on each aircraft. For example, on the F-5A: the average damage rates were different for the five recording phases; the data from the first phase (where the gun was being evaluated) should not be included in the overall damage rate; and the period of VGH recording in any one phase was not long enough to establish a good average rate, even though the recordings were made for the duration of the phase. On the F-105F the data from the two bases show a significant difference, primarily due to different external stores, so that the two bases should be handled separately. Also, there was a very significant difference between day and night flights.

The above examples lead to the conclusions that due to the rapid change in mission assignments or usage, it would be necessary to update the usage model very frequently; and also that several models would be in use at any one time.

This would require an elaborate bookkeeping system and a continual analysis of the instrumented fleet to determine when the damage model changed and what the new model should be.

A much simpler system, from an analysis and bookkeeping viewpoint, would be a peak counting strain recorder. Presented below are design concepts of a counting accelerometer and two types of strain recorders.

2.    PEAK COUNTING ACCELEROMETER

Peak counting accelerometers have been used by the British Aircraft industry and the United States Navy for some time. The early installations recorded in registers the number of times that a given load factor was equaled or exceeded. These counts were independent of flight condition or aircraft configuration. Recently a new concept in counting accelerometers (References 8 and 9) was introduced for use with the F-111 aircraft. This new counting accelerometer separated the load factors by certain combinations of Mach number and wing sweep angle. This concept allows the calculation of different stresses for the same load factor level, depending on the aircraft's environment and configuration. The following presentation is a discussion of the design of a discriminating counting accelerometer.

A discriminating counting accelerometer can be visualized as an onboard data processing system. Its purpose is to provide a low-cost reliable system for accumulating load factor data and correlating it to other variables. In performing a fatigue analysis of an aircraft fleet, the following calculations are performed: (1) simultaneous time history recordings are obtained of load factor, Mach number, and latitude, (2) these parameters are then blocked into class intervals and a report is prepared that presents the number of times that the load factor peak reached a certain value for each combination of class intervals of Mach number and altitude, along with other parameters such as weight and configuration, and (3) from the calculated curves or tables of stress peak counts and the S-N data for a point on the aircraft, the fatigue damage is calculated.

An onboard counting accelerometer can be designed so that it has a series of accumulating registers which count the number of times that the load factor exceeds a certain value, with all the other parameters constant. This, in effect, is then a stress peak count. The principal disadvantage of this system is the large number of storage registers required to sort the load factor data by combinations of Mach number, altitude, weight, and configuration. In the illustrated system (Figure 27), provision is made for sorting the g-data into three sub-groups according to pre-defined conditions of other variables such as weight or configurations. The components required for this unit are conventional and commercially available; and the circuitry, namely the latching, sorting and dropout circuitry, is well developed and reliable. The cost of the system hinges primarily on the choice of counters, which runs from $20 per unit to $70 per unit. Fifteen counters are needed. In high quantity (10,000 counters) the price quoted by one manufacturer drops from $70 to $10 per unit.

The counting accelerometer operates as follows: as the acceleration level is increased from the normal 1 - g level, contact is made by the acceleration transducer's wiper to successively increasing level contactors. Such contact, even only momentary, brings the live supply voltage from the wiper to a given contact line and causes the latching relay for that level to momentarily operate. Operation of the latching relay closes a contact on the relay which connects the contact line to the live supply voltage by a route other than the accelerometer wiper. (This other route, for reset purposes, passes through the normally closed contacts of relay R.) Once this alternate route is established the latching relay is "latched on" and the contact line is live even after the accelerometer wiper leaves it. All levels operate in this manner.

To sort g occurrences with respect to weight or configuration, the five lines whether energized or not are routed to three counter banks through three banks of ganged switches (three 5-pole relays). These operate from external commands shown here as configuration command buttons. The buttons would be replaced by two or three logic relays once the desired sorting function is established.

Upon return to the normal g - level or any established threshold, the reset contact is touched by the wiper contact, causing the reset relay R to de-energize all five latching relays, and re-establish the circuits to receive the next g-level signal.

Vibration and/or oscillation of the accelerometer are not counted and neither are cycles in the g value which do not increase from the normal g level position or the established threshold level. This is accomplished by the latching relay mechanism, which holds any given tripped counter in the energized position until the reset contact is touched and relay R de-energizes all five latching relays. When a counter is held energized it is effectively locked, since it is during dropout of the counter solenoid that ratchet action occurs to permit counter advance upon the next energizing pulse. The counters, in effect, store the cumulative frequency of g levels equal to or greater than the level for that register.

3.   PEAK COUNTING ELECTRO-MECHANICAL OPTICAL STRAIN TRANSDUCER

The use of a peak counting accelerometer would still require calculations of the response of the aircraft structure to convert load factor magnitudes to stresses at various points on the aircraft. A more direct approach would be to record the number of times that a given strain level was equaled or exceeded at a particular point on the aircraft structure. If the exceedence spectrum of the stresses at a point could be known, it would not be necessary to know anything about the aircraft configuration, weight, or flight environment provided a constant 1 - g trim stress could be assumed.

The components of a system to provide such knowledge can be grouped into three areas: (1) the accumulating registers; (2) the mechanical or electronic logic to sort the signal levels into bands; and (3) the strain transducer. The accumulating registers would be the same for all of the systems but the banding mechanisms would be dependent on the type of strain transducer.

One possible type of system would use a conventional dial indicator as the strain transducer with the indicating hand replaced by a drum with a small aperture and a light source inside the drum. Spaced around the outside of the drum would be photocells that would sense the amount of rotation of the drum, which would be proportional to the strain. Each photo cell would be connected to a storage register so that every time a certain magnitude of strain was equaled, the counter would index one count. A schematic drawing of such a system is shown in Figure 28. The wiring diagram of the system is shown in Figure 29. The mechanism of the dial indicator is a rack and pinion with one set of step-up gears, so that for a rack travel of .0001 inches the dial rotates 1.8°. For a two-inch gage length, a stress of 1000 psi would therefore cause a rotation of 3.6° and 36,000 psi would produce 129.6° of rotation.

If five class intervals were used to represent the stress exceedence curve from 12,000 to 36,000 psi, each class interval would be represented by 21.6° of rotation. This sensitivity would give a good resolution for positioning the photocells to distinguish one class interval from another. Assuming that only a peak count of the strains would be necessary, one additional photocell would be located at a threshold level. The strain level would have to decrease below this threshold level before a second peak could be recorded.

One strain channel of such a system is shown on the diagram. As strain increases the aperture slit rotates to illuminate successive photo-resistive cells which then energize their corresponding relay $K_1$----$K_5$. Energizing such a relay $K_1$----$K_5$ closes the contact on that relay which brings current to the corresponding counter. This contact also brings an alternate current to the relay over a path other than through the photocell. This alternate current remains after the photocell is not longer illuminated and serves to latch the relay. This current, however, also passes through the normally closed contact of the reset relay $K_0$ and de-energizes any and all given relays $K_1$----$K_5$, which had been latched. Reset occurs below the level of any desired strain level and hence there is never any conflict of the reset with the energizing and latching of any relay $K_1$----$K_5$. Of course, each strain level could be provided with its own reset level with the addition of four more relays. These new reset levels could be placed anywhere other than coincident with the level of the circuit that they are to reset.

There are several advantages of this type of instrument over a load factor recorder. The first and most important is that the accuracy of the fatigue analysis is not dependent on any usage parameters of the aircraft. No pilot log is required.

The storage registers do not have to be read after each flight, but instead perhaps only once a month. The fatigue analysis performed with the strain data is independent of whether the loading was symmetric or asymmetric provided the location of the sensor is such that the transfer factor is a constant for all types of loadings.

At the present time there are a few possible shortcomings of this system, mainly related to the strain transducer. The fatigue life and airworthiness of the dial indicator is unknown; however, any deficiencies should be minor and correctable with a minor effort. There may be some difficulties with transient temperature changes which could cause a differential thermal expansion between the aircraft structure and the dial indicator push rod. Another disadvantage is that one complete system would be required for each fatigue critical location on the structure. This would still require fewer storage registers than an accelerometer system.

The remaining components of the system employ conventional and commercially available counters and relays. Cost of one channel would depend primarily on the price of the counters and the results of the dial indicator tests. The counters could run as high as $70 each and the latching relays up to $15 each. However, in large quantity these costs are expected to be more like $10 and $3, respectively.

4. RESISTANCE STRAIN GAGE

Another method of monitoring the strain cycles is to use the analog output signal of a conventional resistance strain gage bridge to operate relays at different signal levels. A circuit which would compare the output signal to reference levels is shown in Figure 30, along with a complete circuit diagram of the system.

The counting electrical resistive strain gage is essentially a system which blocks analog strain signals into five preset digital class intervals and then registers the occurrence of each strain level into a counter as it occurs. The proposed system employs a resistive strain gage whose output signal is amplified and thus scaled up by a stable gain but low cost closed loop operational amplifier. The output of this amplifier is compared to a staircase of five voltage levels which are created by an appropriate stack of zener diodes. An alternative voltage staircase could be obtained by use of a resistive divider string. When the output of the amplifier exceeds the voltage level of a given tap on the staircase, the rectifier diode on that branch would become conductive and current would pass through the corresponding relay. A counter could be connected in parallel with this relay, as shown, or energized through a second contact on the relay (not shown) for more reliability if required.

Energizing any given relay also closes the contact on that realy which connects the relay to a current from the staircase string. This latches it and holds it on, even if the amplifier output level changes to a lower level. When the output

level drops to the reset level, the reset relay, which has contacts that are normally open, de-energizes and resets all latched relays. The reset relay is connected to the amplifier output and de-energizes only at near-zero levels of amplifier output and hence at near zero strain levels. This threshold level would be set near the 1 - g trim stress level.

The components suggested in this system require some design considerations and in this regard the system is not as straightforward as an all-relay or electro-mechanical system. However, a logical system is feasible and once designed and tested it should be in every respect as reliable as an all electro-mechanical system.

5.     MECHANICAL SCRATCH GAGE

A commercially available scratch strain gage has been evaluated by the USAF for potential use in monitoring fatigue damage for maneuver sensitive aircraft (Reference 10).

The device is a self-contained mechanical extensometer capable of measuring and recording total deformation (and thus average strain) over the effective installed gage length of the member to which it is attached. The gage contains its own brass recording disc and provides a permanent record of each strain excursion above the installation sensitivity threshold limit. During flight tests on a jet trainer (Reference 11) it was determined that the disc capacity would be on the order of 30 hours.

This device is inexpensive (approximately $100 per installation), requires little maintenance and is self compensated for temperature. The recorded trace is permanent and may be retained for future use once it has been removed from the aircraft.

The discs must be removed and processed to extract the data. Methods of data retract vary from simple, but time consuming manual reading with a calibrated microscope to complex optical scanning equipment. Automated equipment to handle large amounts of discs is considered necessary to successfully warrant the use of the device in service.
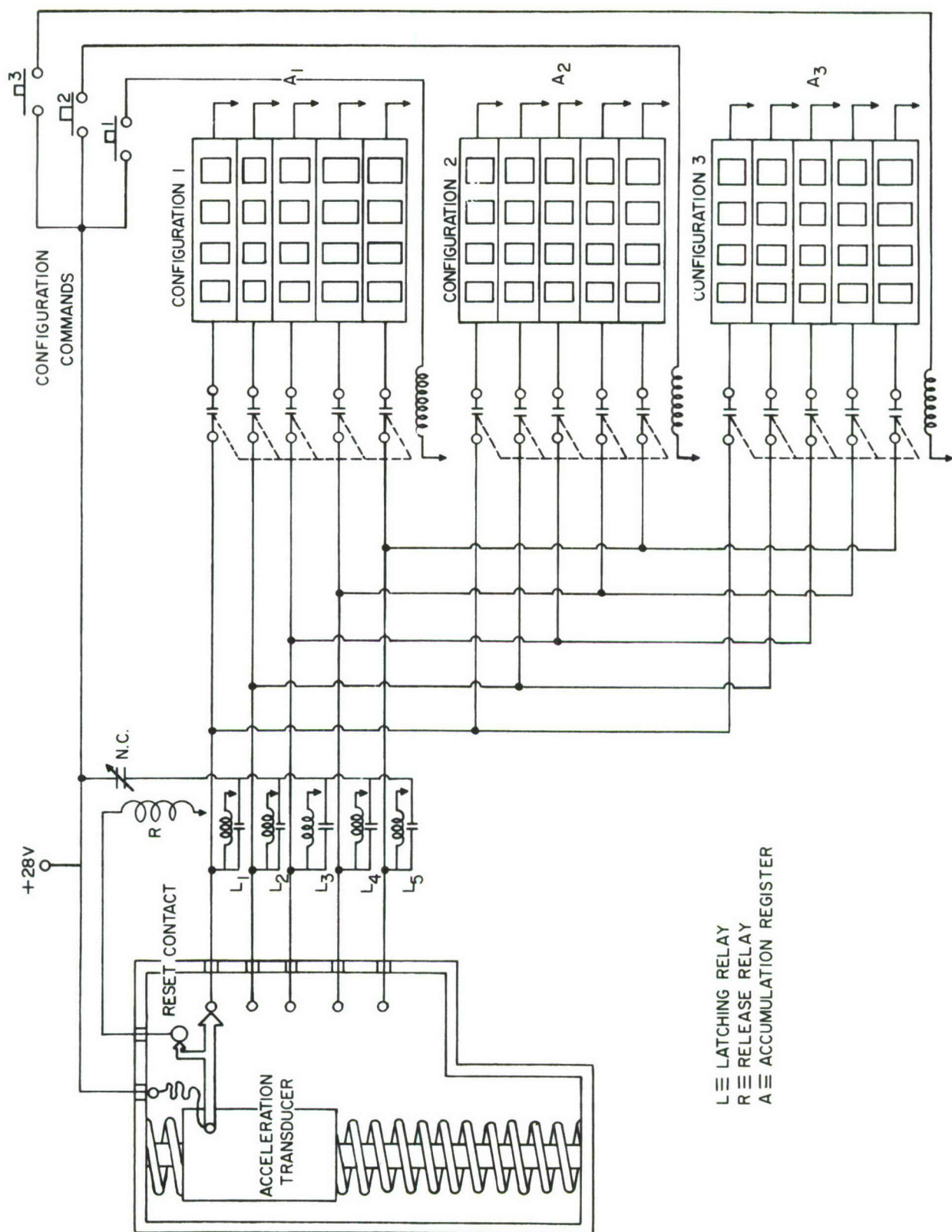
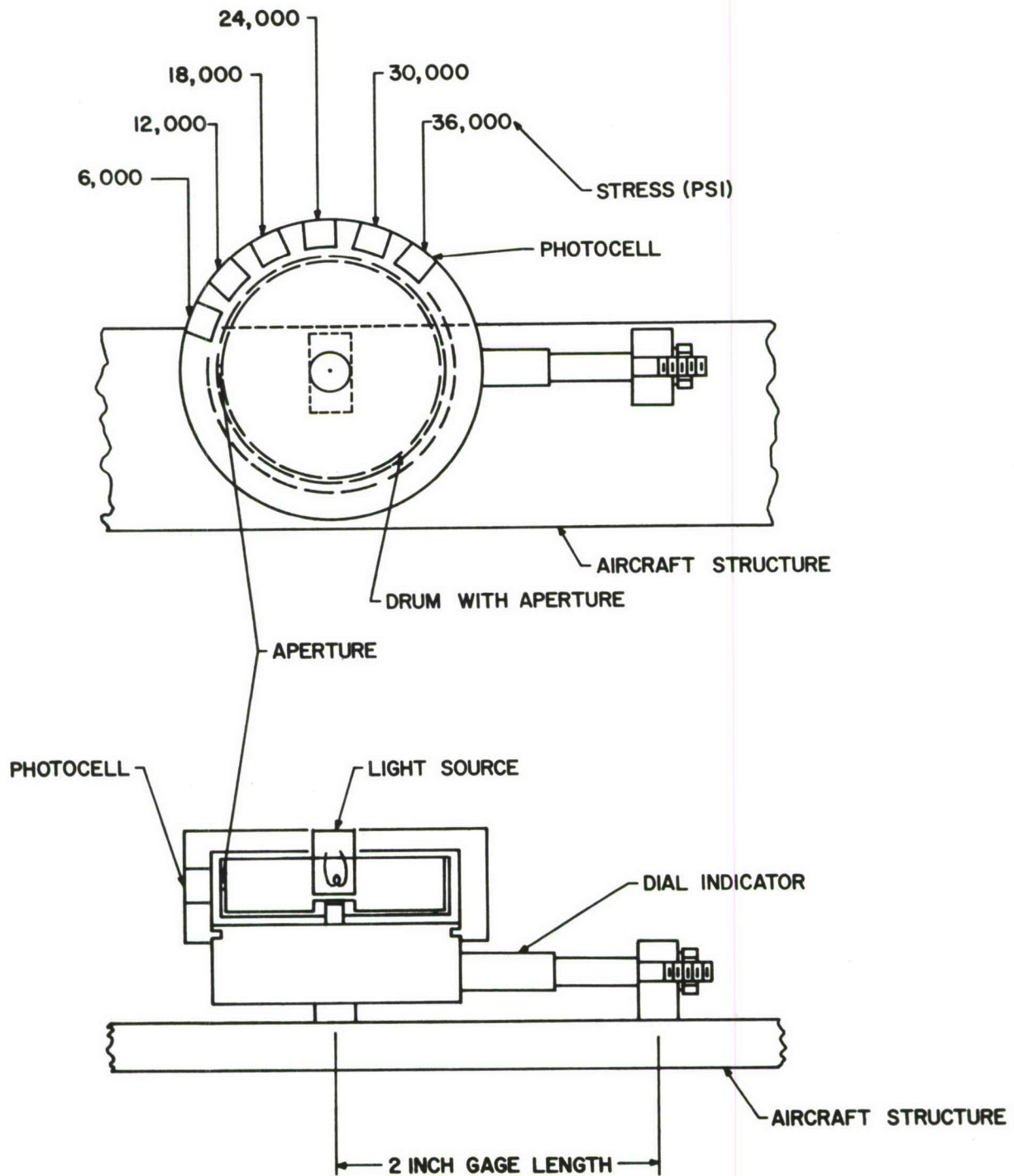Figure 27   Schematic Diagram of Counting Accelerometer System

L ≡ LATCHING RELAY
R ≡ RELEASE RELAY
A ≡ ACCUMULATION REGISTER

Figure 28    Design Concept of Electro-Mechanical-Optical Peak
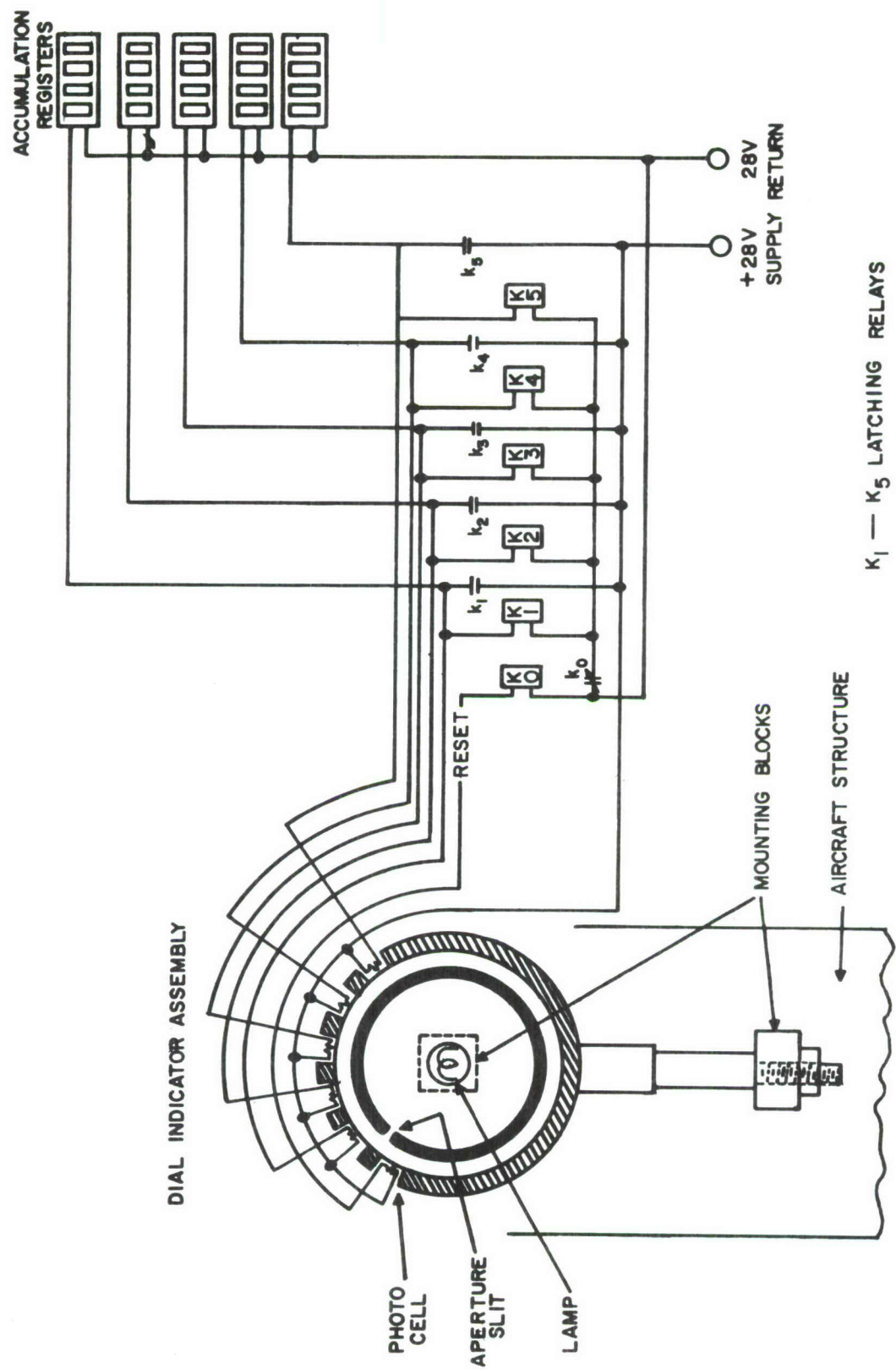Strain Transducer

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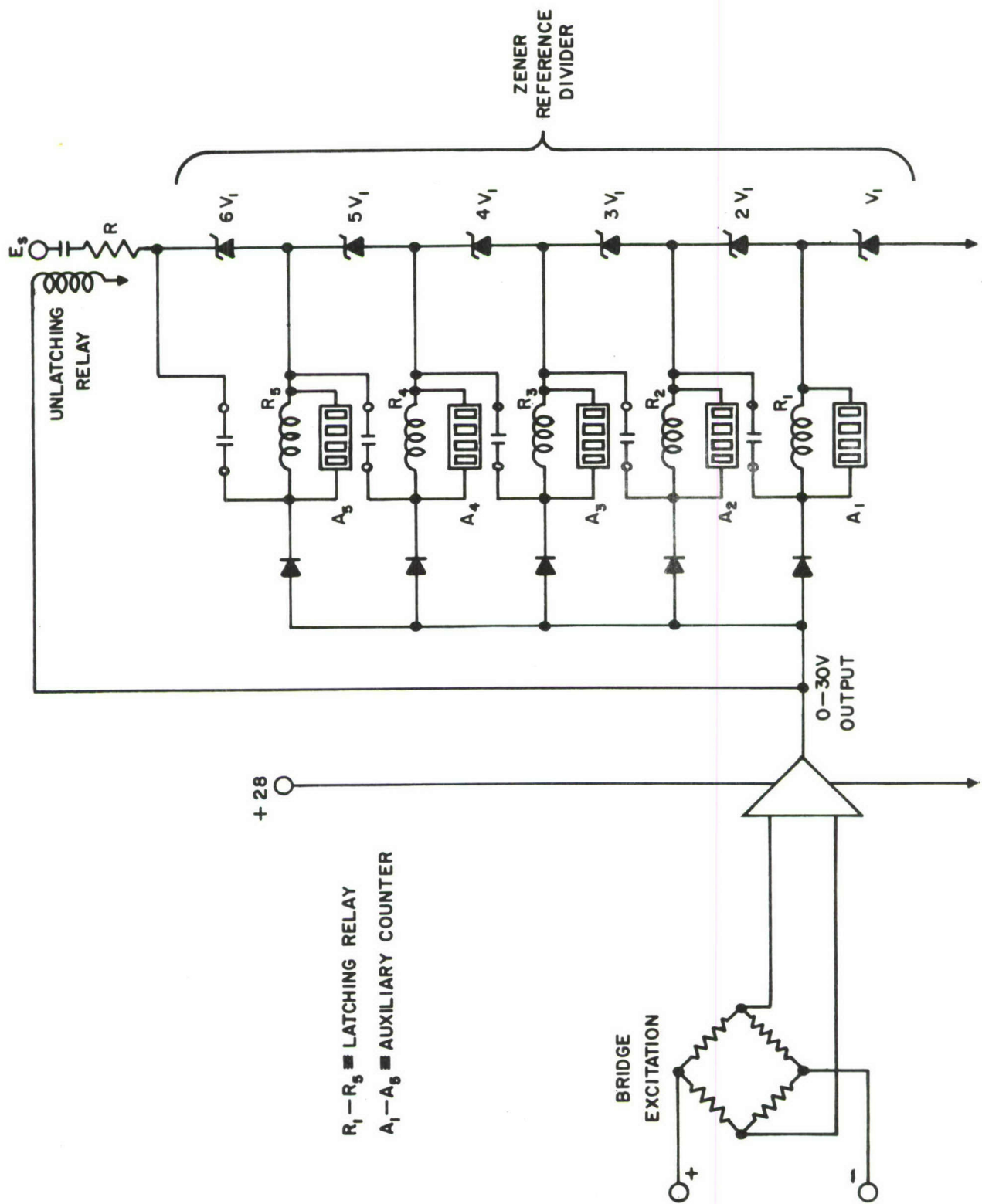Figure 29   Schematic Diagram of Electro-Mechanical-Optical Peak Strain Counting System

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Figure 30   Schematic Diagram of Resistance Strain Gage Peak Strain Counting System

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SECTION IV

DISCUSSION

The analysis of the parameters that affect the magnitude of the fatigue damage indicates that for most fighter aircraft, the load factor, gross weight, stores configuration, Mach number and altitude are all important and independent variables. The fact that the magnitude of each variable is independent of each other, and in many cases independent of the type of mission, places a burden on statistics that prevents the construction of any damage model which will accurately predict the damage to individual aircraft. This is true even when the individual aircraft's experience was included in the construction of the model. It is logical to think that for aircraft whose experience is not included in the model, the deviation from the model would be greater than for aircraft which were included in the model.

It has been shown that if the significance of the variables were to be ranked in order of importance, a mean value used for the least important, a probability distribution for the next most important, and the two most important variables were to be measured; then the prediction of the damage naturally was improved. However, the results were still not acceptable.

A comment about the predicted damage based on the Mach-altitude probability model is in order. Referring to Table XLI, it can be seen that at the 6.7 g level for example, there were five occurrences. These five occurrences could have been on five different aircraft. When the model is applied in the prediction of the damage, it would be assumed that 20% of the occurrences were at Mach .85 and 7000 ft. altitude and 40% at Mach .92 and 7000 ft. altitude, etc. The expected average damage rate for a 6.7 g maneuver is then 20% of the damage for an occurrence at Mach .85 altitude 7000, plus 40% of the damage for an occurrence at Mach .92 altitude 7000, plus 40% of the damage for an occurrence at Mach 1.2 altitude 20,000. However, when one applies the model to an individual aircraft there may be only one occurrence of 6.7 g's in the data sample. The true damage is the damage for one of the Mach-altitude combinations listed but the predicted damage is the above described average damage. Therefore, the model cannot be expected to predict the correct damage unless the individual aircraft has enough occurrences of a given load factor level that it has a chance of having a distribution like that used to construct the model.

It appears to the authors that since there are five important variables, it is very unlikely for each aircraft to experience the same number of occurrences of each combination of these variables; and, therefore, some measured data will be required. Now, if it is conceded that a recorded measurement is required, why measure load factor, Mach number, altitude, weight, and

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configuration, for fleet tracking of fatigue damage by AFLC, since damage is only indirectly related to these? Why not measure the strain at a point, since damage is a function of only the strain? If a reliable peak strain counter is developed, it will provide data for a more accurate fatigue analysis at a lower cost.

# SECTION V

## CONCLUSIONS

Fighter aircraft deployed in a combat zone experience an almost random stress spectrum. This is due to the large number of parameters (weight, Mach number, altitude, configurations, and load factor) which determine the magnitude of the stress.

Damage rates based on a per-hour or per-flight average may cause errors as large as a factor of 3. Also, the averages depend on the type of mission which changes over a short period of time so that a continual updating of the averages is required.

The Mach-altitude probability model when used with measured load factor data was a better predictor than gross averages but the improvement was not significant.

Due to the variety of missions flown which result in different environmental spectra and weapon configurations, several damage models will be required at any one time.

The use of a peak counting accelerometer that segregates the load factor counts by Mach number, altitude, configuration and gross weight would permit an accurate calculation of fatigue damage but the number of storage registers would be prohibitive.

A peak counting strain indicator would eliminate the requirement for a special pilot's log sheet. This would require the assumption of a constant 1 - g trim stress.

A peak counting strain indicator is the most economical and accurate method of monitoring fatigue damage on fighter aircraft, and to monitor a fleet effectively, each aircraft in the fleet should contain this instrumentation.

# REFERENCES

1. G. J. Roth, J. P. Ryan, J. C. Sliemers; Parametric Fatigue Analysis of USAF Aircraft AFFDL TR-67-89, 1967.

2. W. W. Morton, C. G. Peckham; Structural Flight Loads Data From F-5A Aircraft. SEG-TR-66-51, November, 1966.

3. A. P. Berens; Load Factor Data for F-5A and F-105D Aircraft in Weapon Passes AFFDL-TR-68-47, March, 1968.

4. C. M. Kantershi, T. Ishimine; Maneuver Spectra and Fatigue Life from Measured Combat Data. Northrop Corporation, NOR67-28, April, 1967.

5. F-105D Combat Statistical Flight Loads Program. SMNE 68-910, February, 1968.

6. H. Axkrod; F-105 Fatigue Analysis Based on VGH Data. ESAR 105-4 December, 1965.

7. Joseph Militello; F-105F Combat Statistical Flight Loads Program, Technical Report (EFR) 82.4.1, May, 1969 (In Publication).

8. J. R. Sturgeon; Fatigue Load Meters. Mechanism Limited, Croydon, England.

9. Maintenance Manual No. 61, Fatigue Recording System Type 25. Mechanism Limited, Croydon, England.

10. T. L. Haglage, H. A. Wood; Scratch Strain Gage Evaluation. AFFDL-TR-69-25, July 1969.

11. T. L. Haglage; Flight Test Evaluation of a Scratch Strain Gage. AFFDL-TR-69-116, November 1969.

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**13. ABSTRACT**

This report contains the results of a study of the significant parameters that contribute to the fatigue life of USAF fighter aircraft. The variability of the parameters from one aircraft to another was determined in an attempt to use a mean value or a most probable distribution of some parameters so that they could be eliminated from the log sheet or recorded data. The analysis suggests that there is such a wide variation in the load factors, Mach numbers, altitudes and configurations experienced by the F-105D and F-105F aircraft that an average damage model cannot be used to predict damage to individual aircraft. A peak strain cycle counting recorder is suggested as the most practical method of monitoring fatigue damage to individual fighter aircraft. Design concepts of a counting accelerometer and two types of peak strain counters are presented.

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| 14. KEY WORDS | LINK A | | LINK B | | LINK C | |
|---|---|---|---|---|---|---|
| | ROLE | WT | ROLE | WT | ROLE | WT |
| Fatigue Analysis | | | | | | |
| Maneuver Loads | | | | | | |
| Parametric Fatigue Analysis | | | | | | |
| Fatigue Meters | | | | | | |

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